



# 時空觀念的錯愕：黑洞

辜品高  
師大地科系  
中研院天文所

# Black hole: metaphor of loss and despair?

摘自鄭立三、錢誌恩：  
《宇宙的百慕達三角 -- 黑洞》



藥價黑洞  
高鐵黑洞  
卡債黑洞  
國防黑洞  
退休金黑洞

# Look out for the wording

金剛經：

所謂佛法者，即非佛法，是名佛法。

道德經：

道可道，非常道；名可名，非常名。

# stellar evolution depends on mass

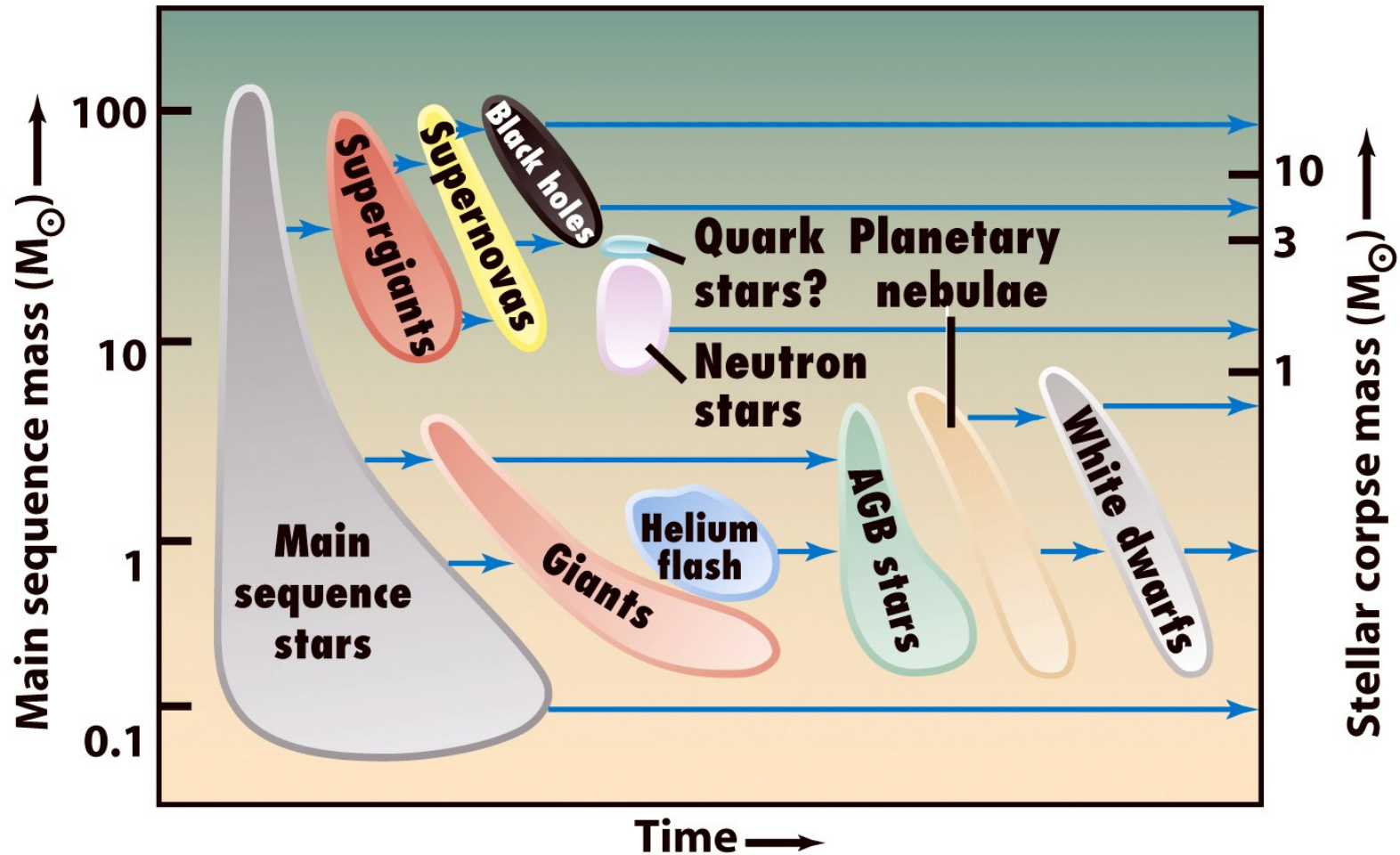


Figure 13-27a  
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# Planetary nebulae 行星狀星雲 leave a white dwarf behind

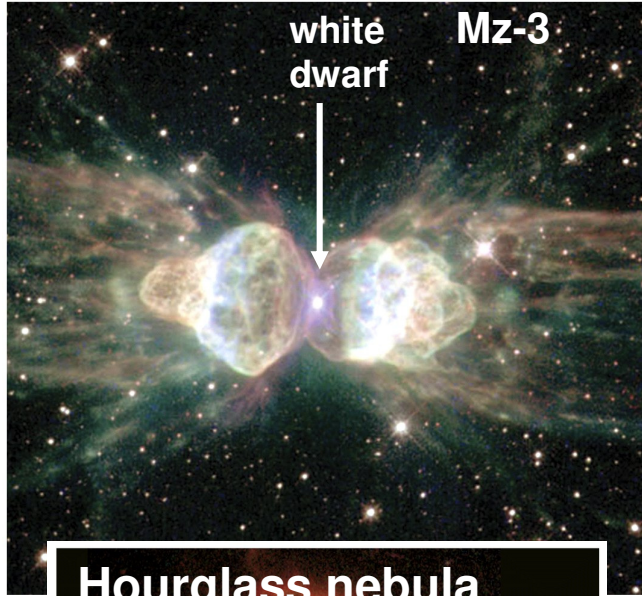


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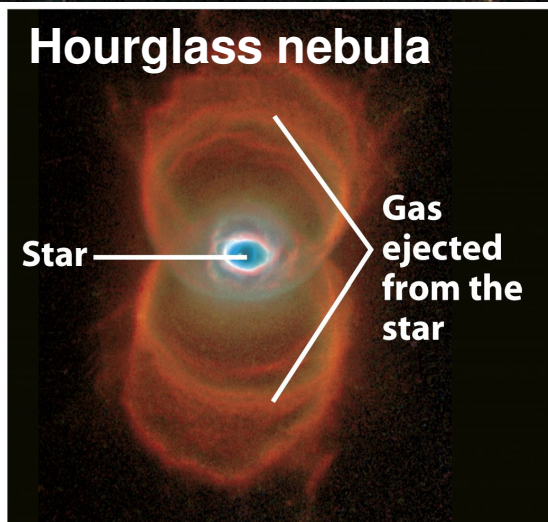


Figure 13-5c  
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...nce tell us that their radii  
...n 0.2 to 3 light-years.  
...nce of emission  
...eir spectra  
...s they are  
...w-density  
...ler shifts  
...y are  
...g at  
...m/s. If  
...radius  
...y, we find  
...nebulae  
...ore than  
...ars old.  
...etary  
...vidently  
...ixed into  
...stellar

IC3568 Visual

This nearly spherical planetary nebula has a low-luminosity outer envelope and a highly excited inner region.

He<sup>+</sup> (blue)  
O<sup>+</sup> (green)  
N<sup>+</sup> (red)

white dwarf (白矮星)

dust

Hubble Heritage Team, AURA/STScI/NASA

...out 1500  
...nebulae in our  
...se planetary  
...re short-lived  
...e, we can conclude  
...ust be a common  
...llar evolution. All stars  
...n, up to a mass of about  
...asses, are destined to die  
...g planetary nebulae.

Visual

Slow stellar wind from a red giant

Fast wind from exposed interior

The Ring Nebula in the constellation Lyra is visible even in small telescopes. Note the hot blue star at its center and the radial texture in the gas, suggesting outward motion.

The gases of the slow wind are not easily detectable.

We see a planetary nebula where the fast wind compresses the slow wind.

...ocess that produces planetary  
...e involves two stellar winds. First,  
...aging giant, the star gradually  
...away its outer layers in a slow  
...e of low-excitation gas that is not  
...visible. Once the hot interior of the  
...exposed, it ejects a high-speed  
...that overtakes and compresses the  
...f the slow wind like a snowplow,  
...ultraviolet radiation from the hot  
...ins of the central star excites the  
...s to glow like a giant neon sign.

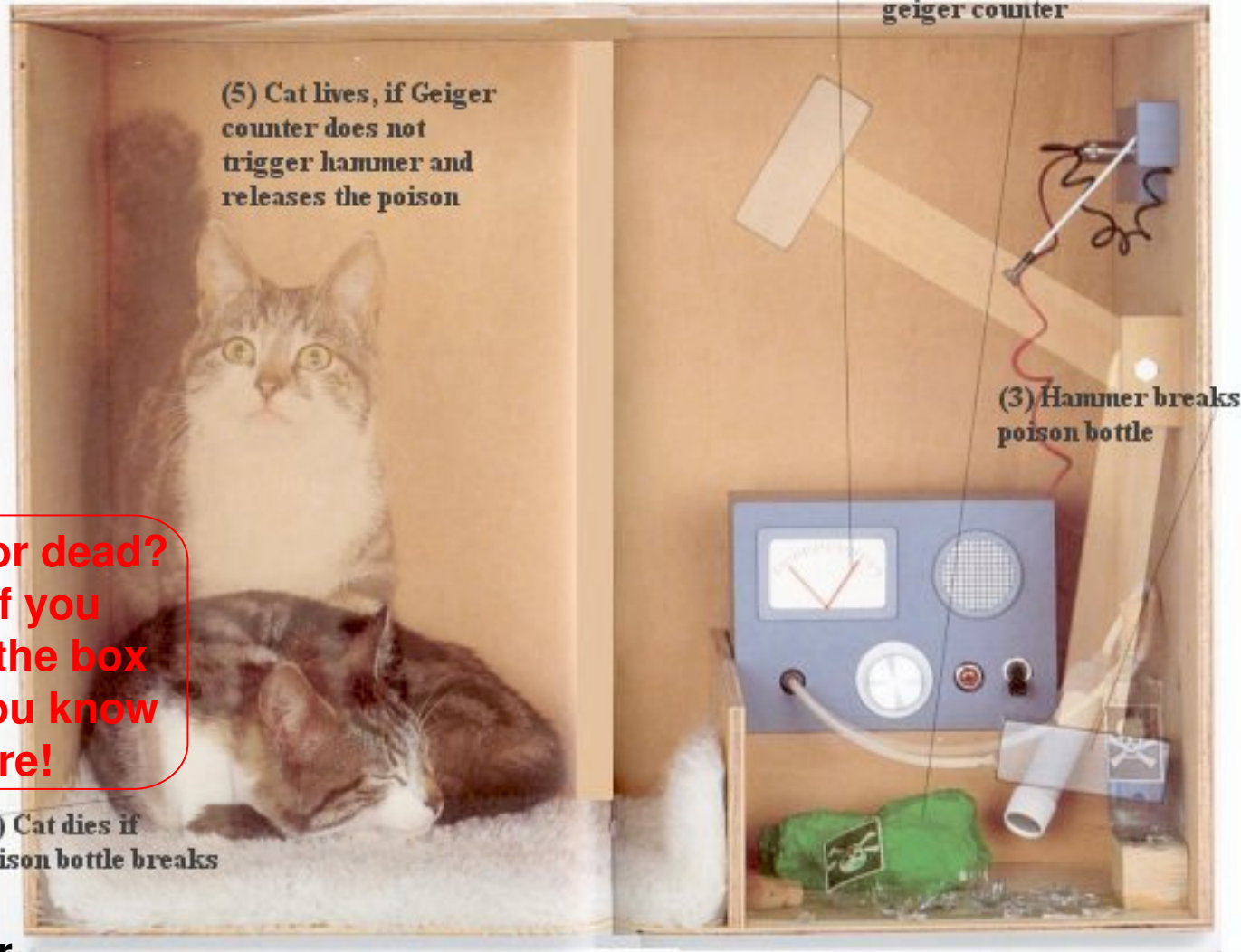
# 薛丁格之貓 (1935)



Erwin Schrodinger  
Nobel Prize in 1933

alive or dead?  
Only if you  
open the box  
will you know  
for sure!

## Schrodinger's Cat



(5) Cat lives, if Geiger counter does not trigger hammer and releases the poison

(2) If geiger counter is triggered, hammer falls

(1) Radioactive material has a 50:50 chance of triggering geiger counter

(3) Hammer breaks poison bottle

(4) Cat dies if poison bottle breaks

<http://universe-review.ca/l12-21-cat.jpg>

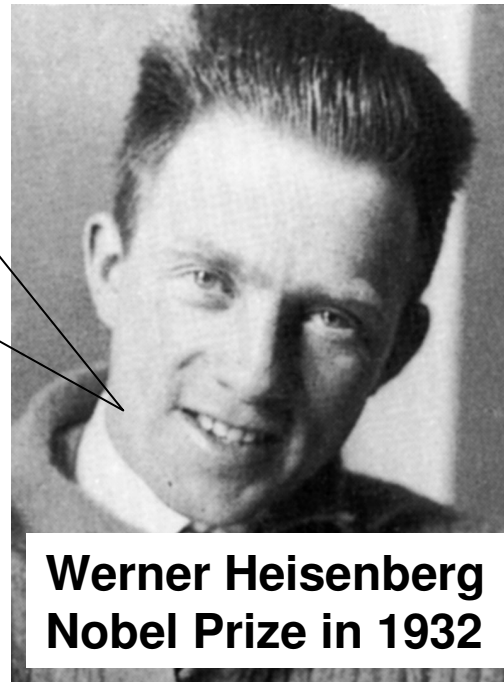
# 量子力學(quantum mechanics)的基石： 測不準原理(uncertainty principle)

基本粒子(質子、中子、電子...)是一種機率波

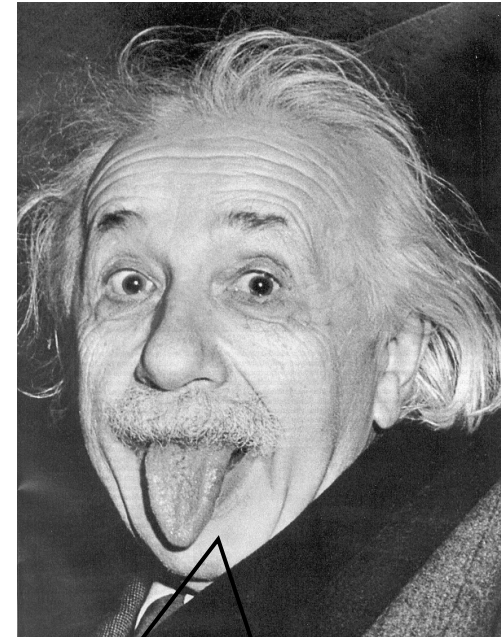
$$\Delta x \Delta p \geq \hbar / 2$$

$$\Delta E \Delta t \geq \hbar / 2$$

理工學院的同學可從  
Fourier Analysis去了解



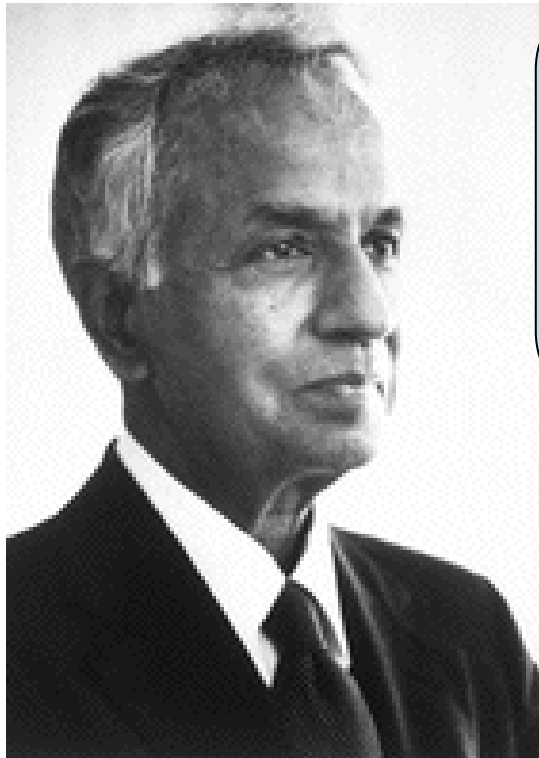
Werner Heisenberg  
Nobel Prize in 1932



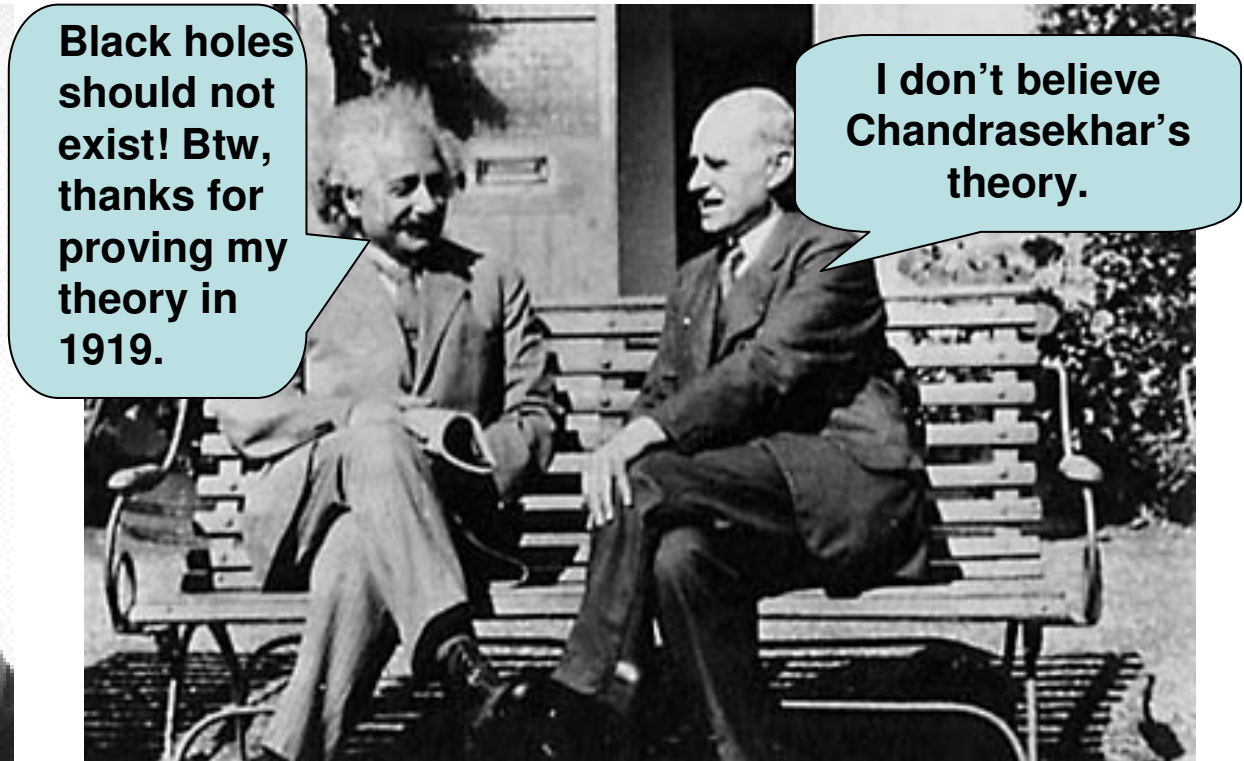
I don't believe it.  
God does not play  
dice!

## 阻擋重力塌縮的防線：Chandrasekhar Limit

當白矮星質量大於1.44太陽質量(Chandrasekhar Limit)，電子簡併壓力將無法抵抗重力，於是開始重力塌縮。



**S. Chandrasekhar  
Nobel Prize in 1983**

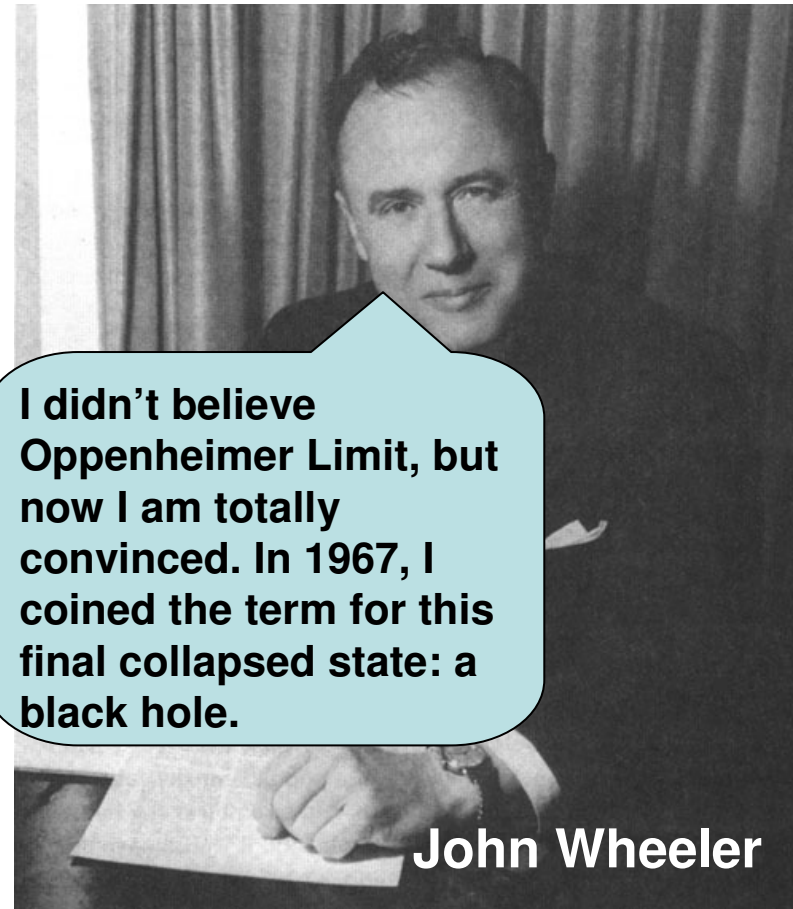
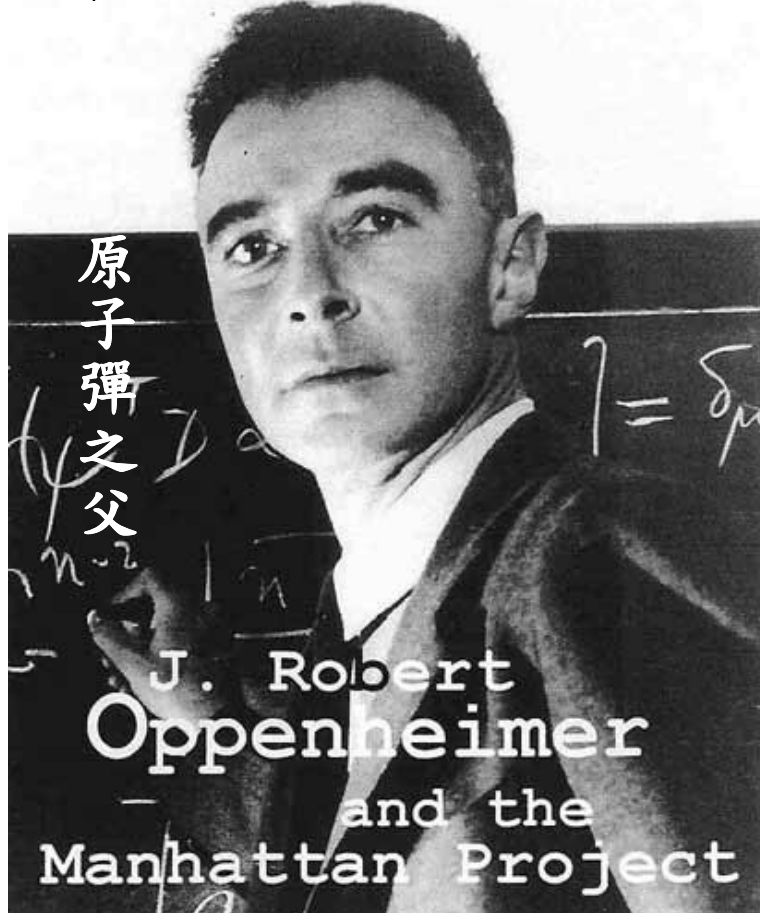


**Albert Einstein & Sir Arthur Eddington  
at Cambridge**



## 阻擋重力塌縮的防線：Oppenheimer Limit

當中子星質量大於3個太陽質量(Oppenheimer Limit)，中子簡併壓力將無法抵抗重力，於是開始重力塌縮。



# Old high-mass stars ( $>8 M_{\text{sun}}$ )

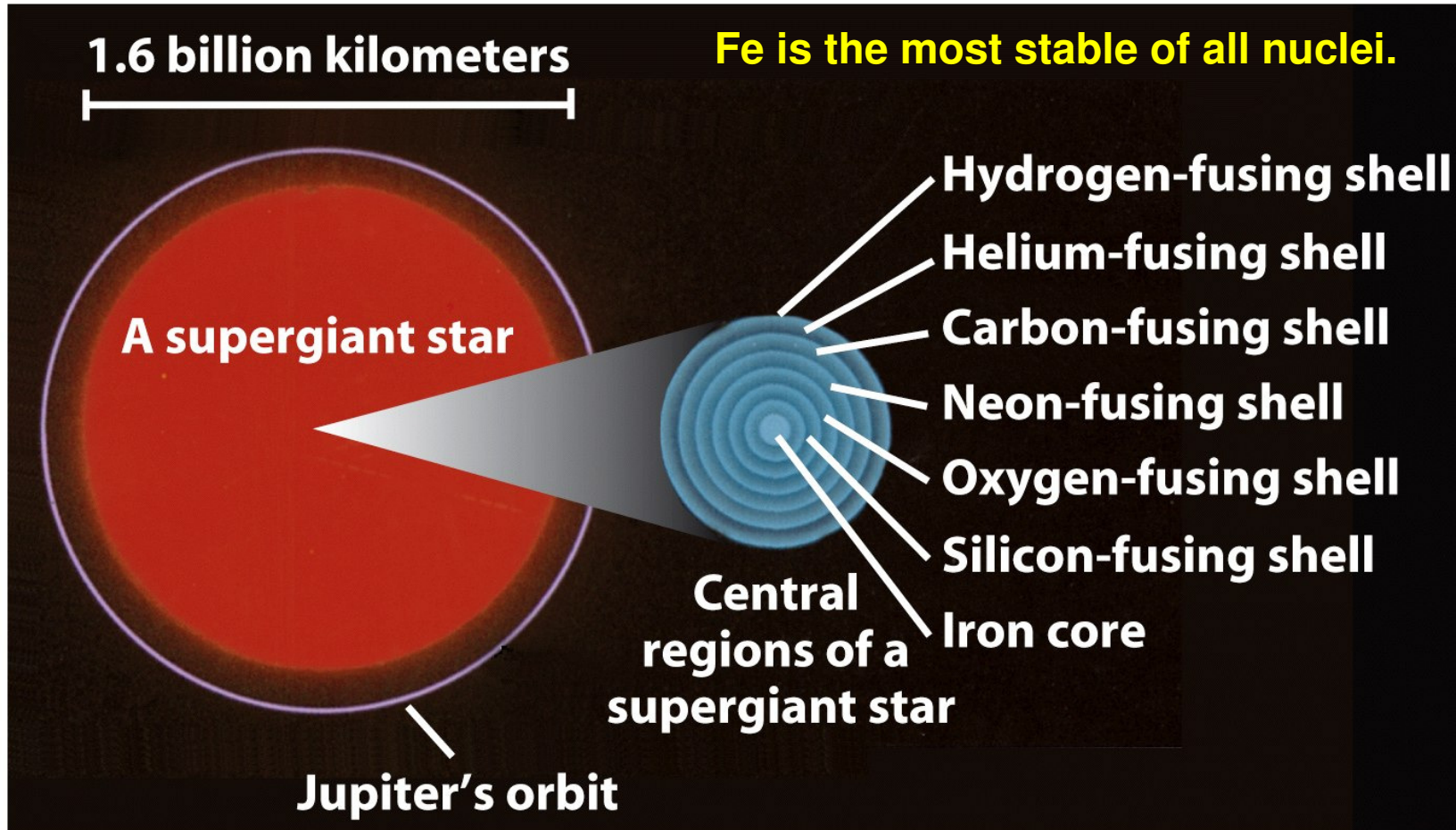
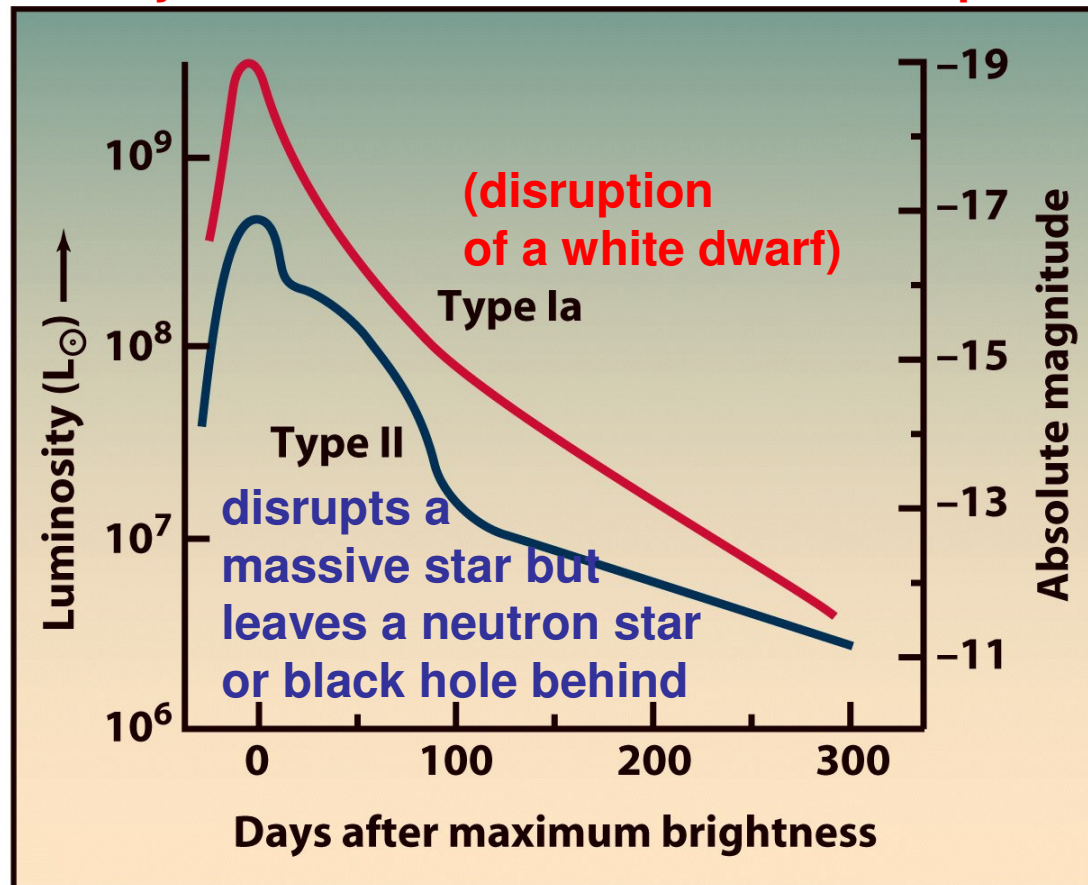


Figure 13-9  
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# Supernovae 超新星

core of a massive supergiant collapse → neutron star/black hole  
outer layer hits the core and rebound → supernova



Note that about 99% of released energy goes to neutrino!

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# supernova remnants



Figure 13-11  
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**Gum Nebular in Vela (visible)**  
**Occurred about 11000 years ago**  
**Size: 2300 ly in diameter**

**Cassiopeia A (X-ray)**

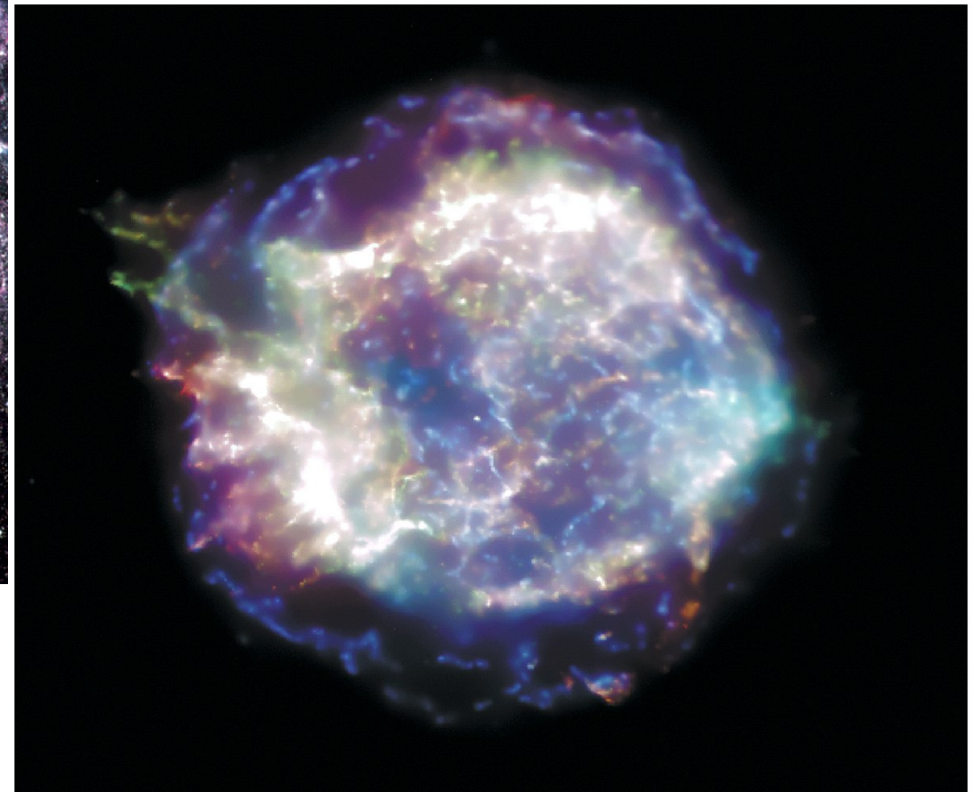
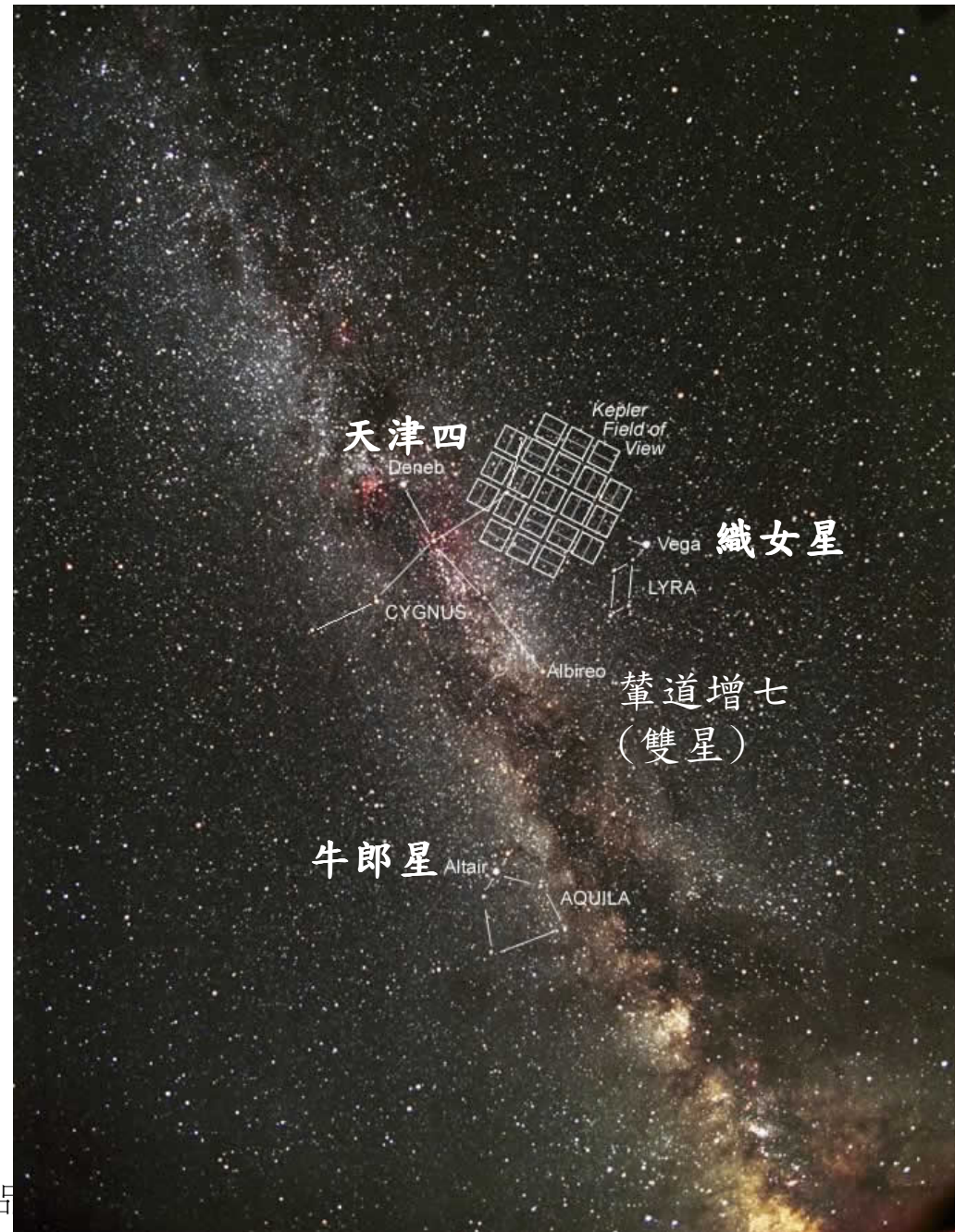


Figure 13-12a  
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# 天津四 可能會變成 黑洞

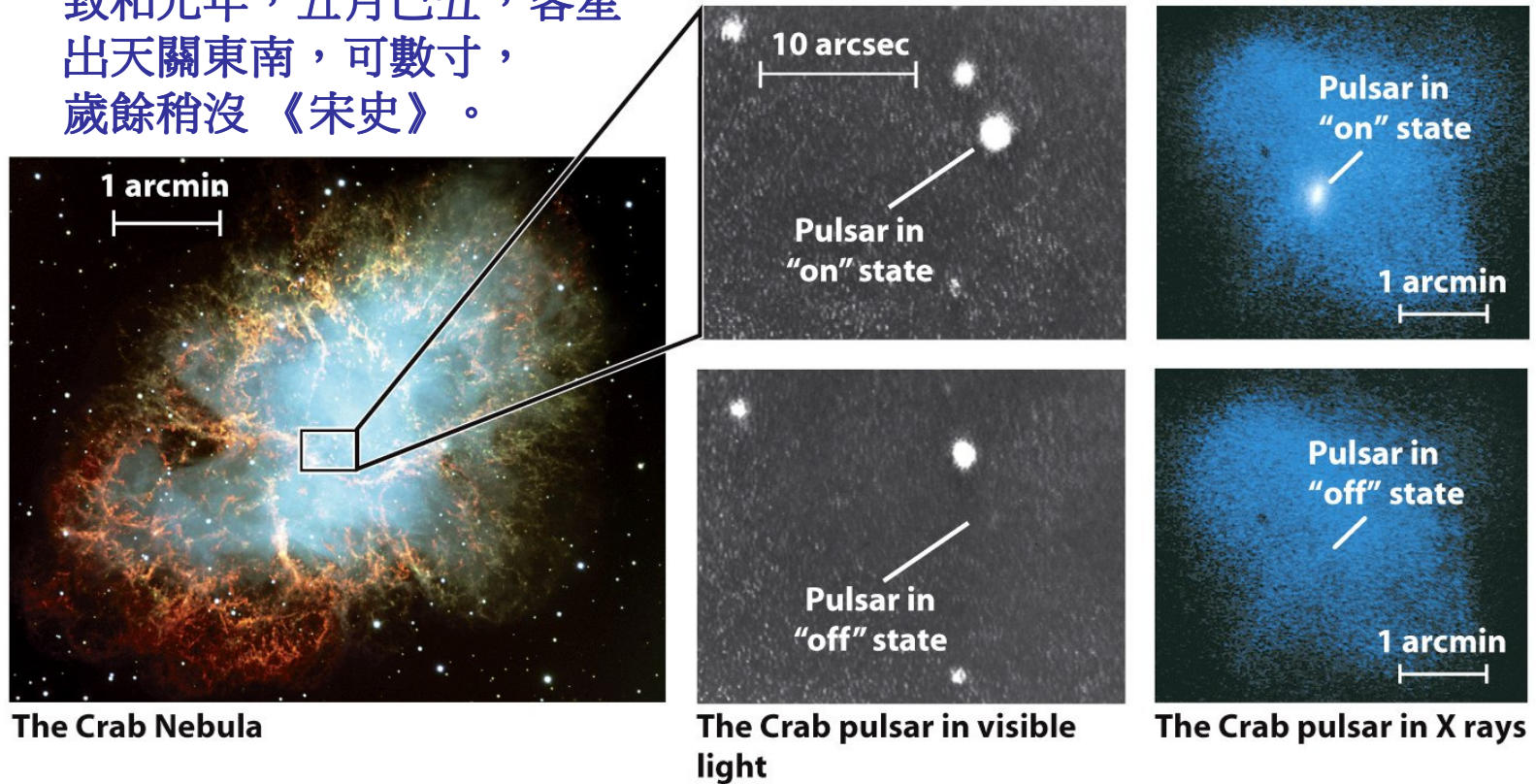


2006/12/27

辜品

# Crab Nebula (蟹狀星雲, M1)

致和元年，五月己丑，客星出天關東南，可數寸，歲餘稍沒 《宋史》。



The Crab Nebula

The Crab pulsar in visible light

The Crab pulsar in X rays

Figure 13-18b  
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**Pulsar (波霎) was thought to be a signal from an advanced alien civilization 😊**

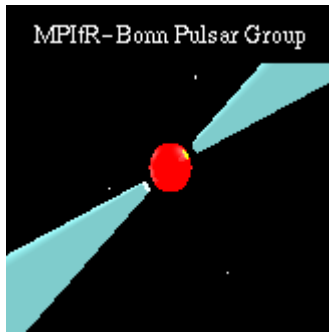
# Crab Nebula

<http://chandra.harvard.edu/photo/2002/0052/movies.html>



**X-ray (Chandra telescope)**

**visible (Hubble telescope)**



# Pulsar (波霎) & Neutron star (中子星)

<http://astronomy.swin.edu.au/pulsar/reduction/p2.html>

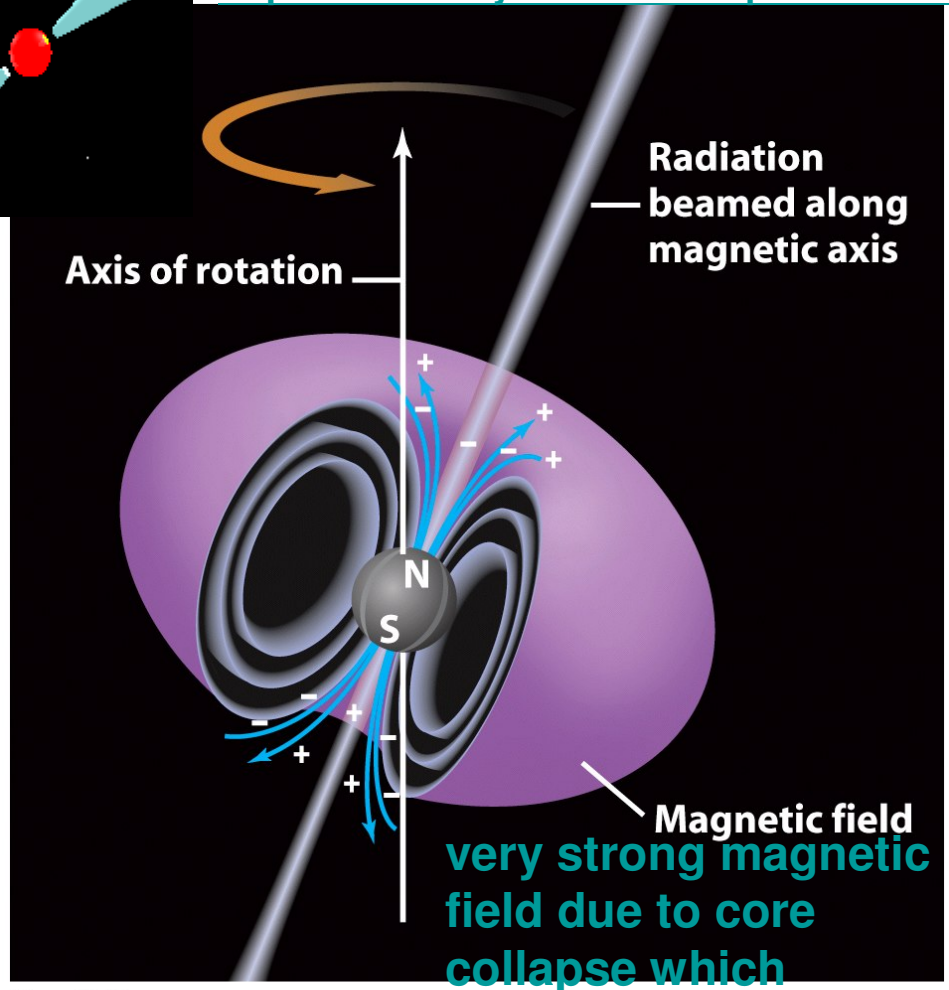


Figure 13-20  
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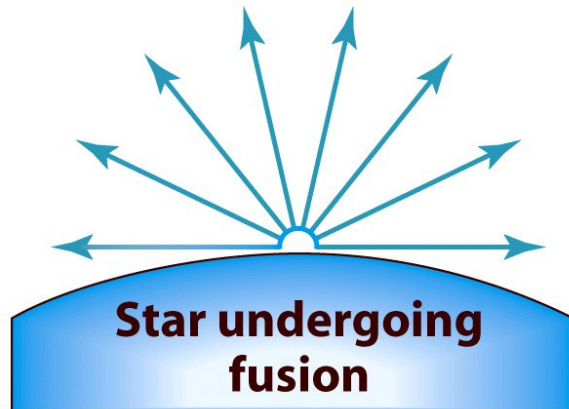
White dwarf mass >  
 1.4 solar masses →  
 $p^+ + e^- \rightarrow n + \text{neutrino}$

Neutron star (a  
 city-size dying star):  
 Made of closely packed  
 neutrons (density is  
 as high as a nucleus!)  
 →  
 gravity is balanced  
 by the **neutron  
 degenerate pressure**  
**(the final defense against  
 gravitational collapse)**

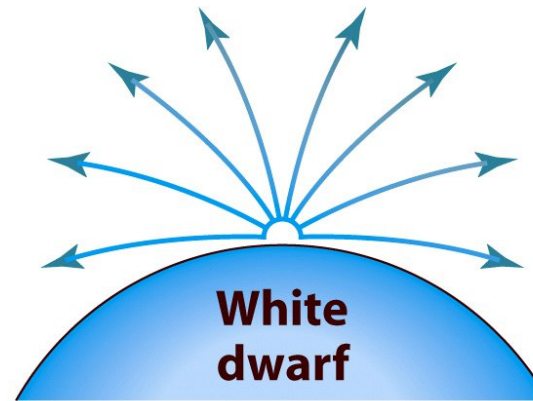
Pulsar is the evidence  
 of a neutron star!



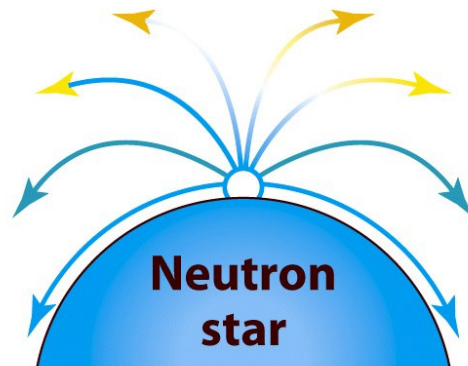
# Black Holes have no hair



a

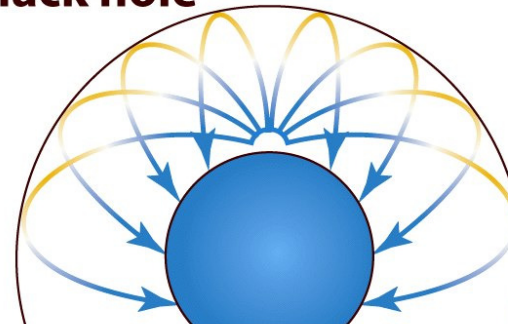


b



c

Boundary of black hole



d

If **density is high** enough

→ Very strong gravity

→

**Event horizon:**

escape velocity = speed of light

Figure 14-8  
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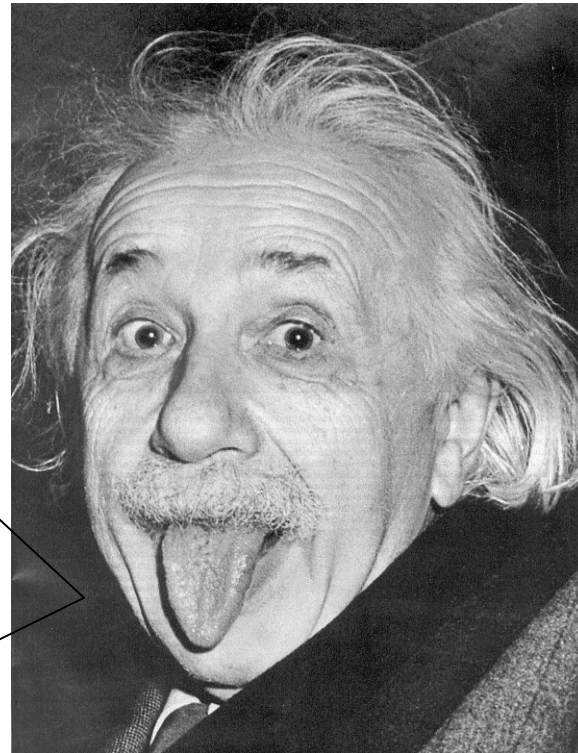
# 狹義相對論(special relativity)

相對中的絕對：

在互相做等速運動的觀測者來說，光速是一樣的。

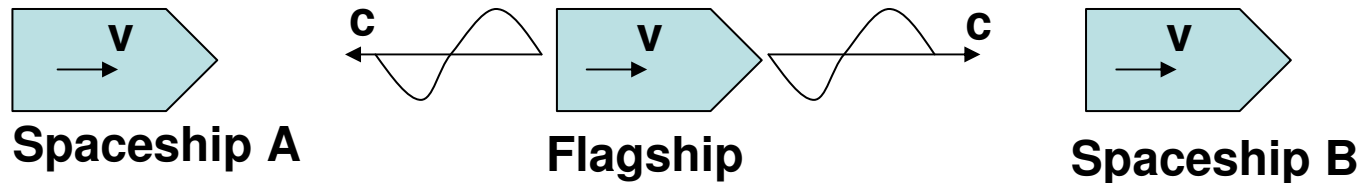
**速度 = 距離 / 時間**

如果「速度」這一個量出了問題，我大膽在此假設：我們傳統對距離與時間的觀念，可能在我們運動速度接近光速的時候，發生嚴重的謬誤。

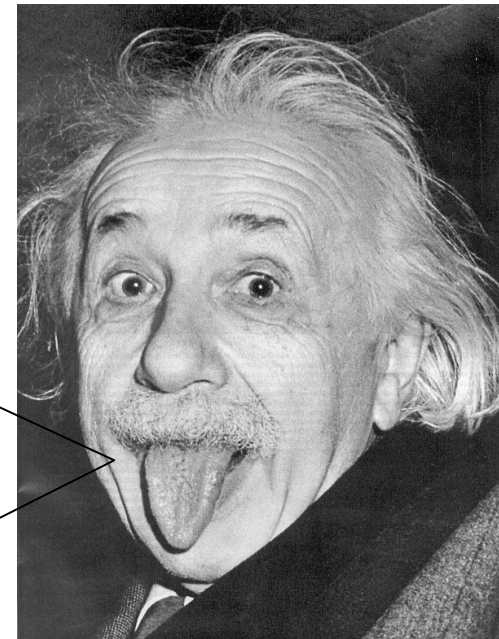


# 不同時性：時間是相對的

為了遷就光速是固定的，新的時間觀念產生了。



Flagship, Spaceship A, 和 Spaceship B 都相對我向右做等速移動。Spaceships A & B 都說**同時**接收到來自 Flagship 的無線電波訊號。但是我認為 Spaceship A **先**收到 Flagship 的訊號！



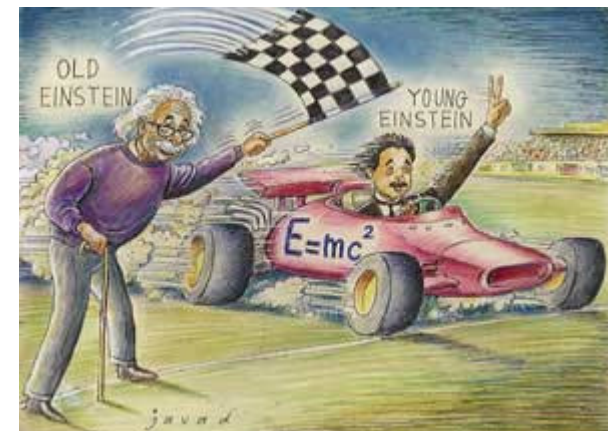
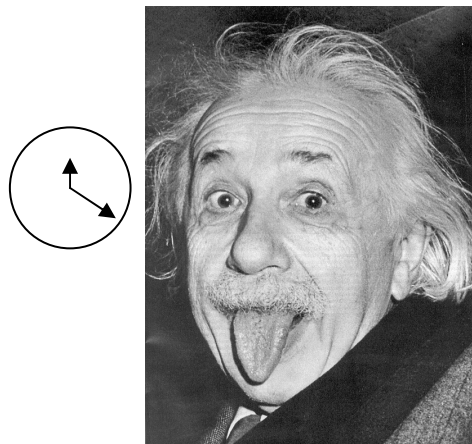
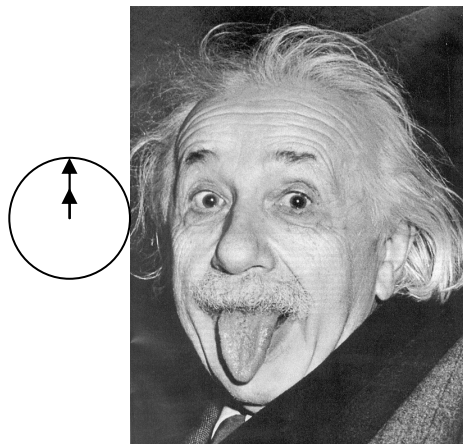
# 時間和空間是相對的

## Time Dilation & Space Contraction

運動的鐘走得慢；運動的尺縮短了



When  $v=c$  (ie light),  
剎那即永恆！



The twin paradox:  
has been tested  
using atomic clocks.

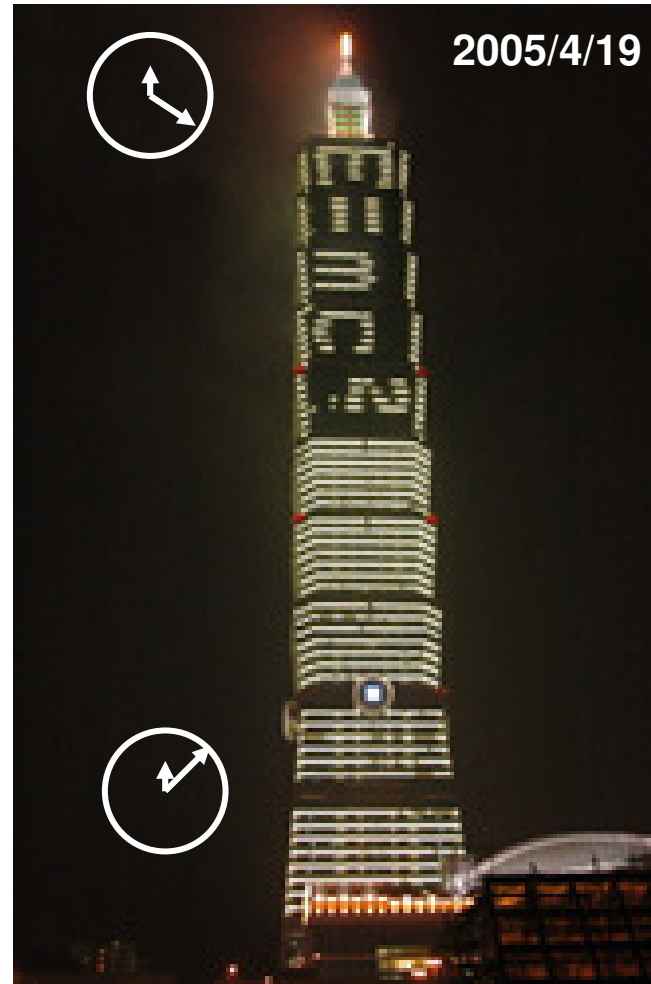
# 相對論的神話

人總是喜歡神話 …

我們無時無刻都以光速在時空中運動。  
所以靜止時，老得最快；  
如光般運動的時候，剎那即永恆！

# 廣義相對論 General Relativity (mass $\rightarrow$ time dilation)

重力紅移  
Gravitational Redshift



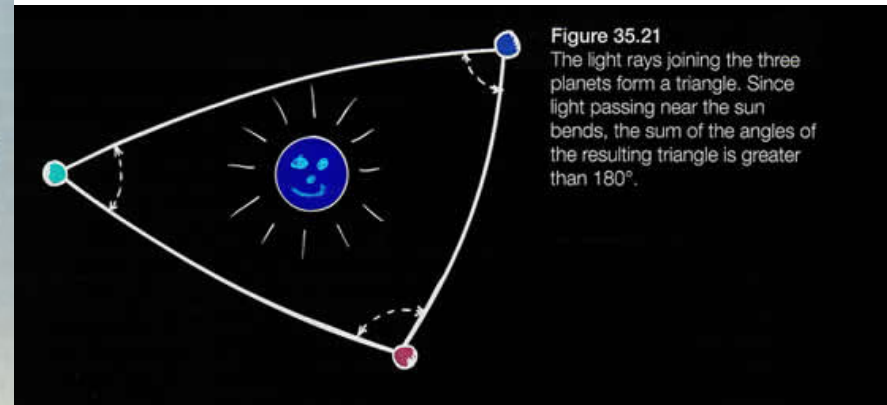
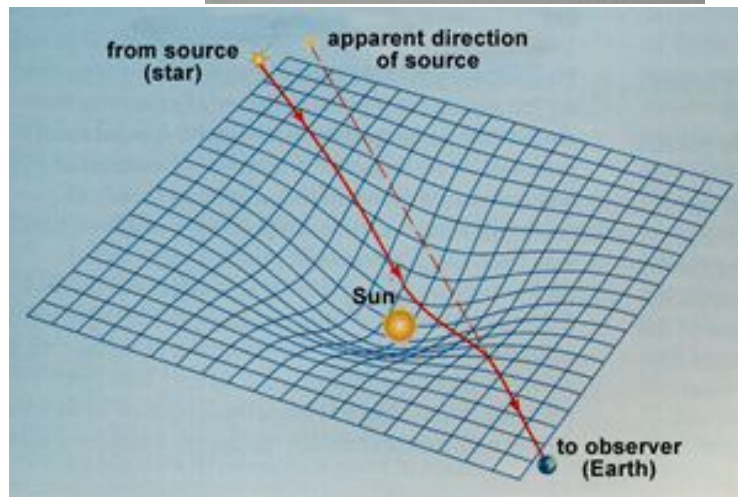
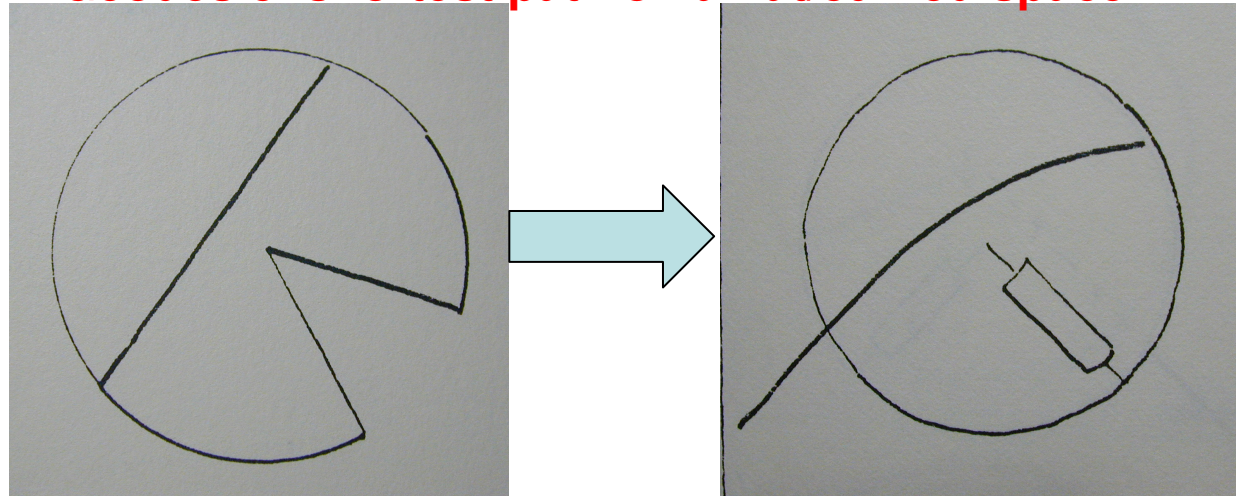
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辜品高：星星·月亮·太陽

22

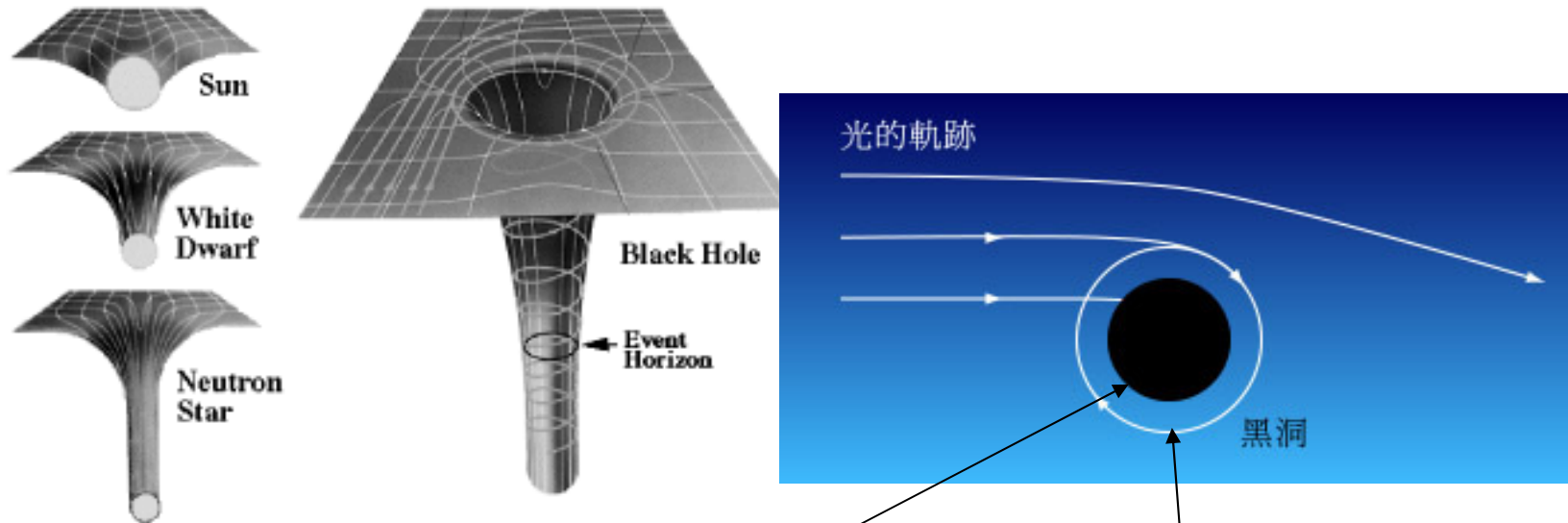
# 廣義相對論 General Relativity (mass $\rightarrow$ space warps)

Geodesic: shortest path on a flat/curved space



# Space warps & density

<http://imagine.gsfc.nasa.gov/docs/teachers/blackholes/imagine/page11.html>



Event Horizon (事件的穹界)

Photon Sphere (光子球層)



# General Relativity (mass $\rightarrow$ space warps)

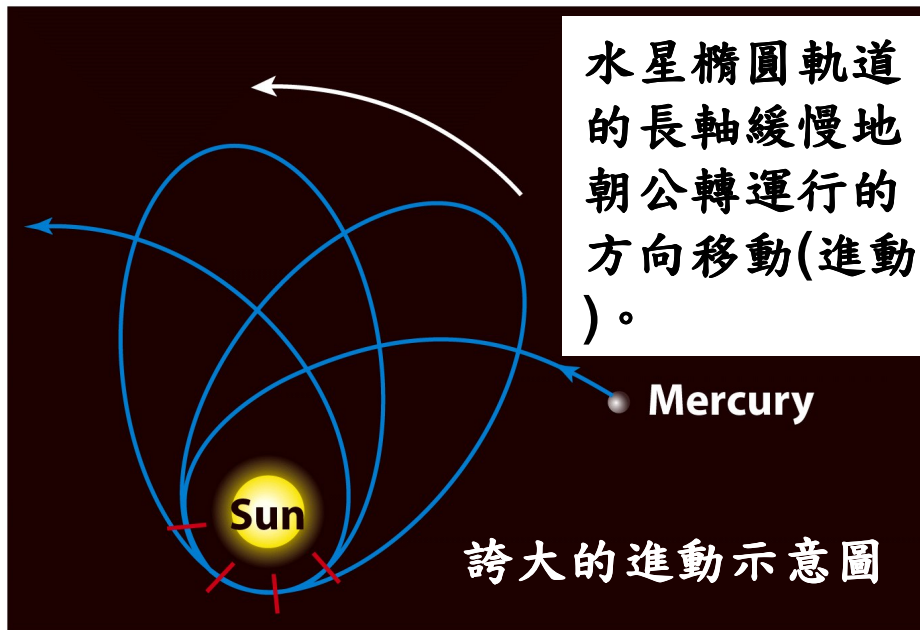
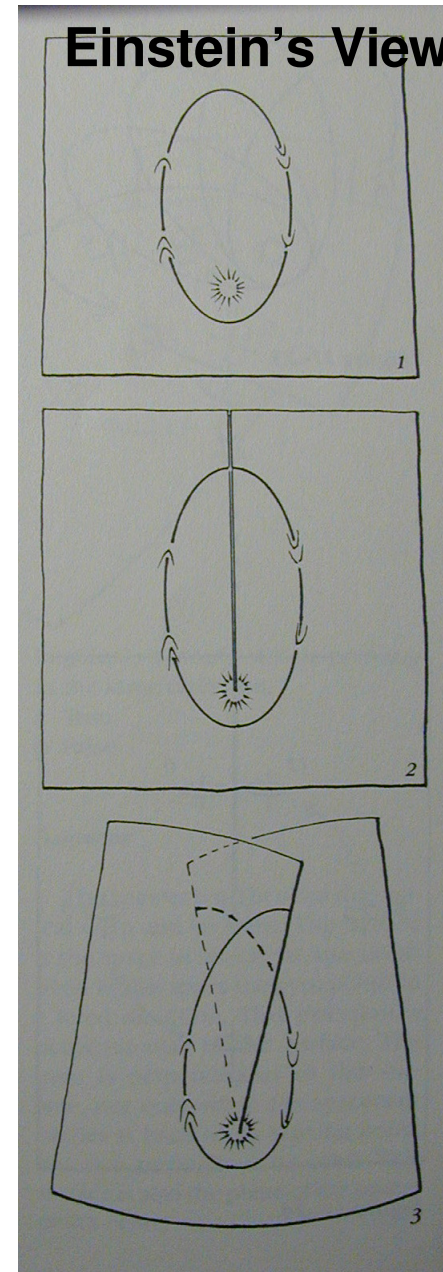


Figure 14-7  
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在19世紀，有大約10%的水星進動速度無法用牛頓力學來解釋。

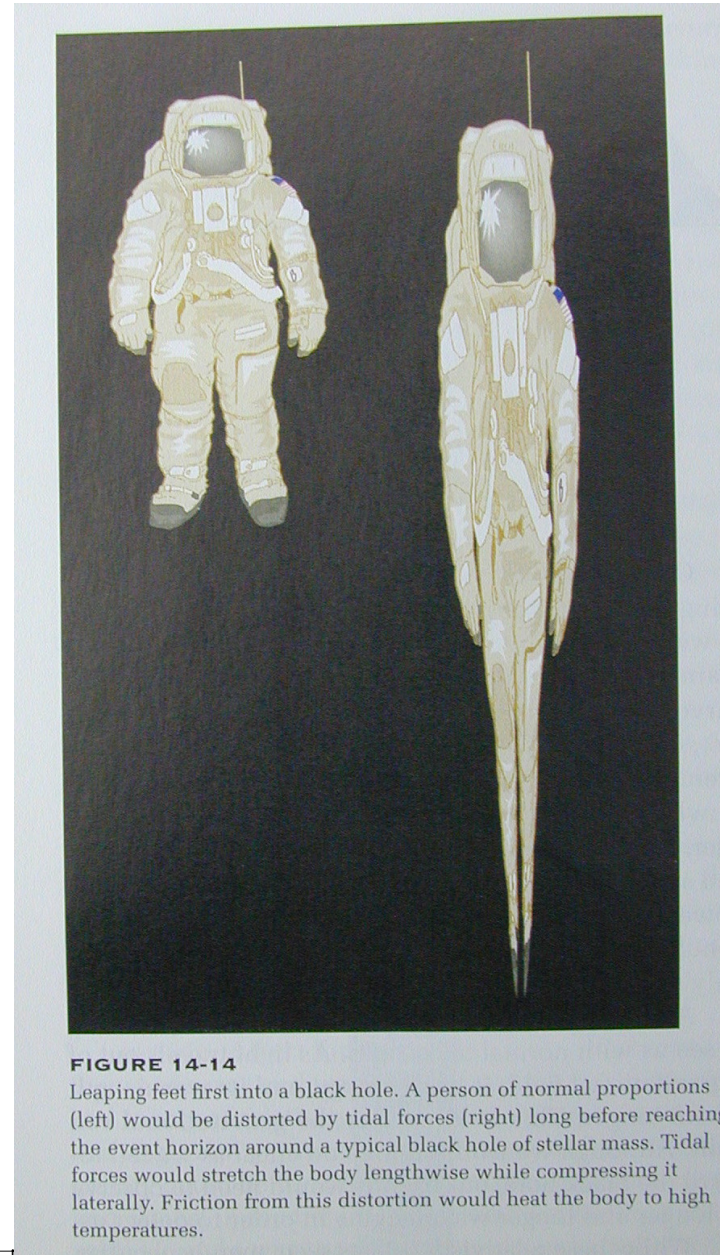


# Strong tidal force

As an astronaut is falling  
into a black hole, we  
(outside observers) will  
see

- 1) terrible tidal tearing
- 2) the astronaut falls more and more slowly (time dilation)
- 3) harder and harder to see the astronaut (gravitational redshift)

So my point about this is...  
**bloody but not very  
interesting**



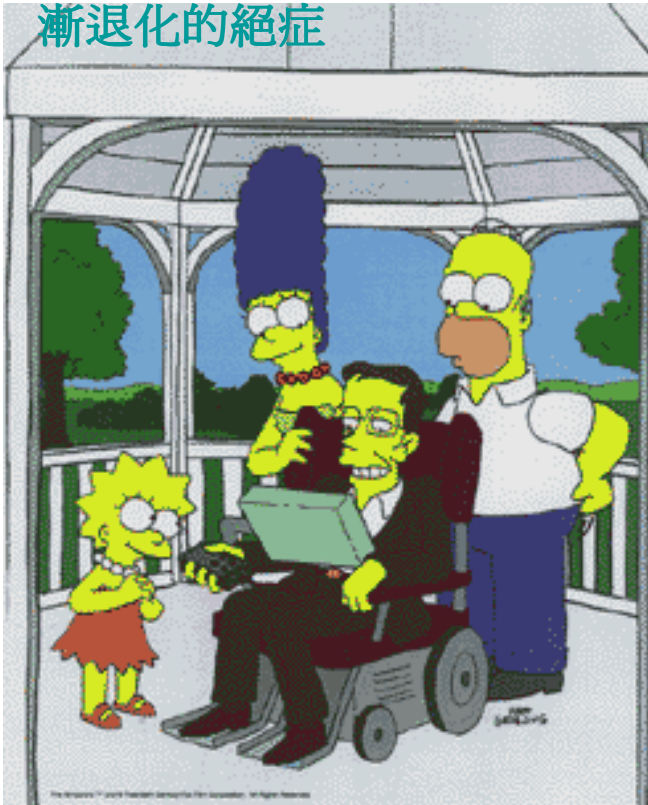
# Black Hole has no hair

**Price's theorem: whatever can be radiated is radiated. After collapsing to a black hole, there are only three properties left: mass, spin, & charge.**

**But a black hole can wear a toupee. 😊**

# Stephen Hawking (1942-)

Lucasian Professor of Mathematics, University of Cambridge  
Amyotrophic Lateral Sclerosis 肌肉萎縮側索硬化症(ALS)又叫 Lou Gehrig's Disease, 或在台灣稱為漸凍人, 是控制自主運動的神經細胞逐漸退化的絕症



Hawking was born 300 years to the day after Galileo died.

<http://www.hawking.org.uk/about/mgallery3.html>

# Hawking Radiation: black holes are not so black ☺

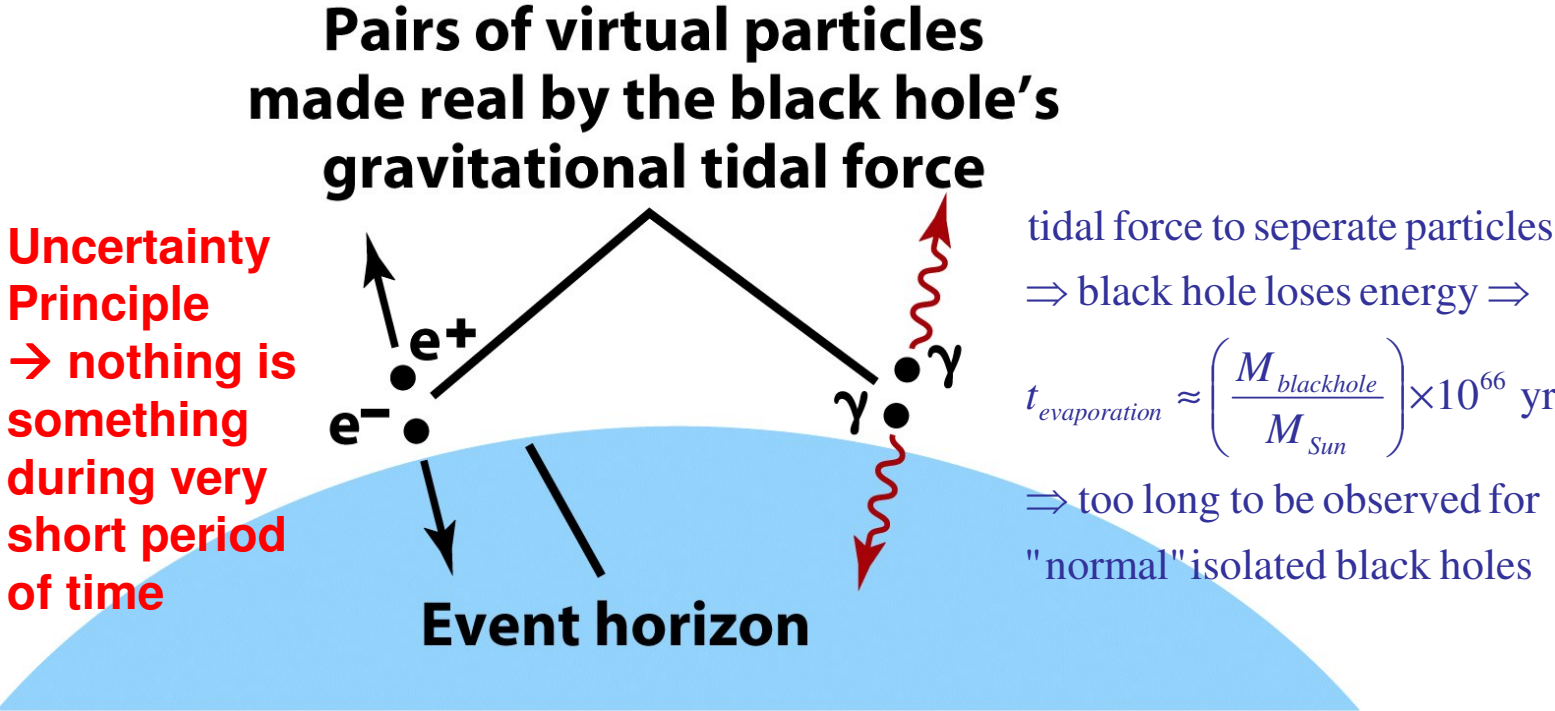
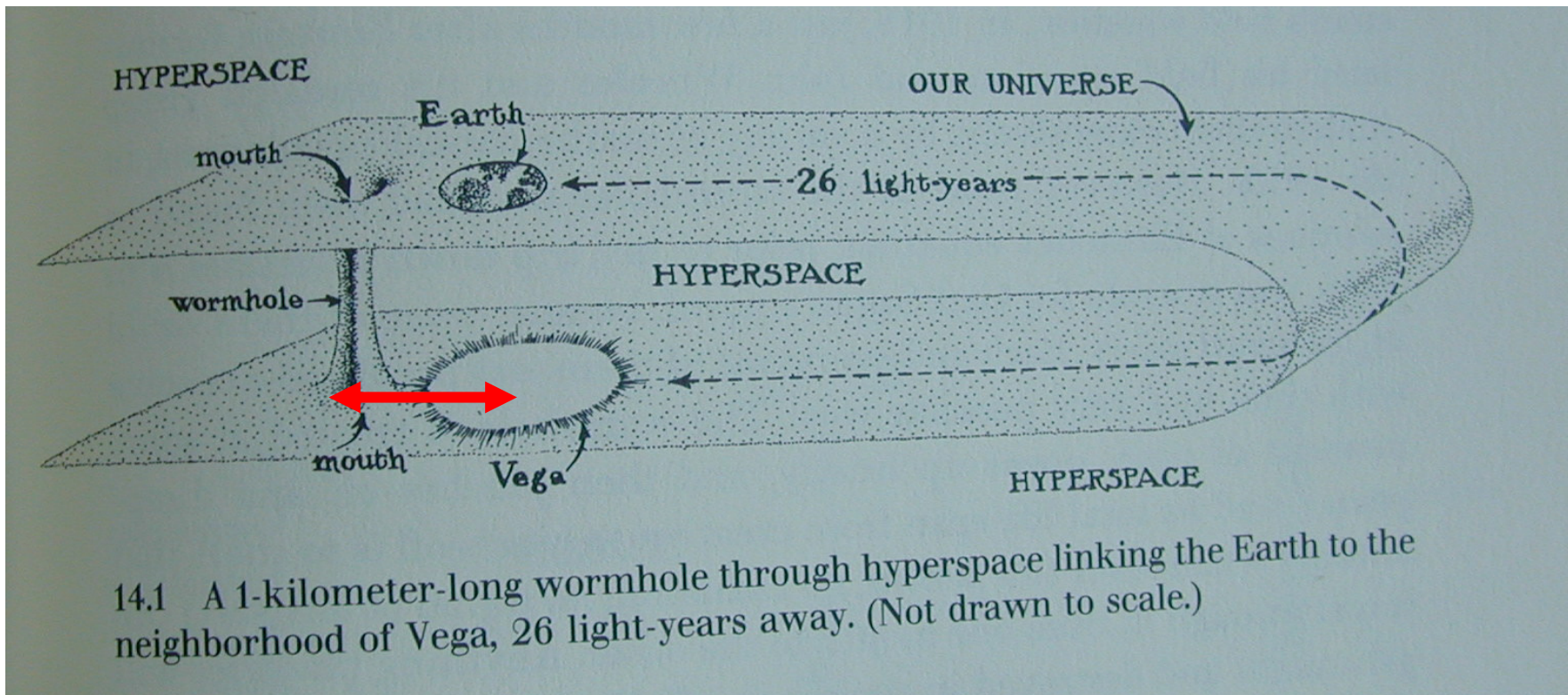


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# 蟲洞(wormhole) & Time Machine

摘自於 Kip Thorne: Black Holes & Time Warps

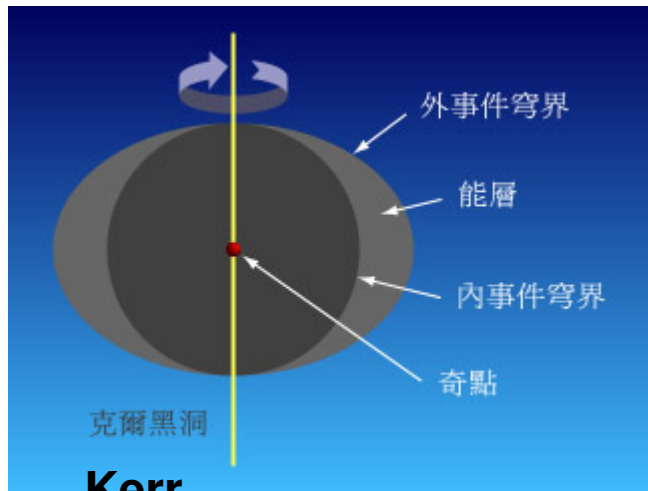


**Three puzzles need to be explained:**

- 1) tidal disruption (to survive),**
- 2) “anti-gravity” energy (to open the wormhole),**
- 3) Causality (to make us feel better!)**

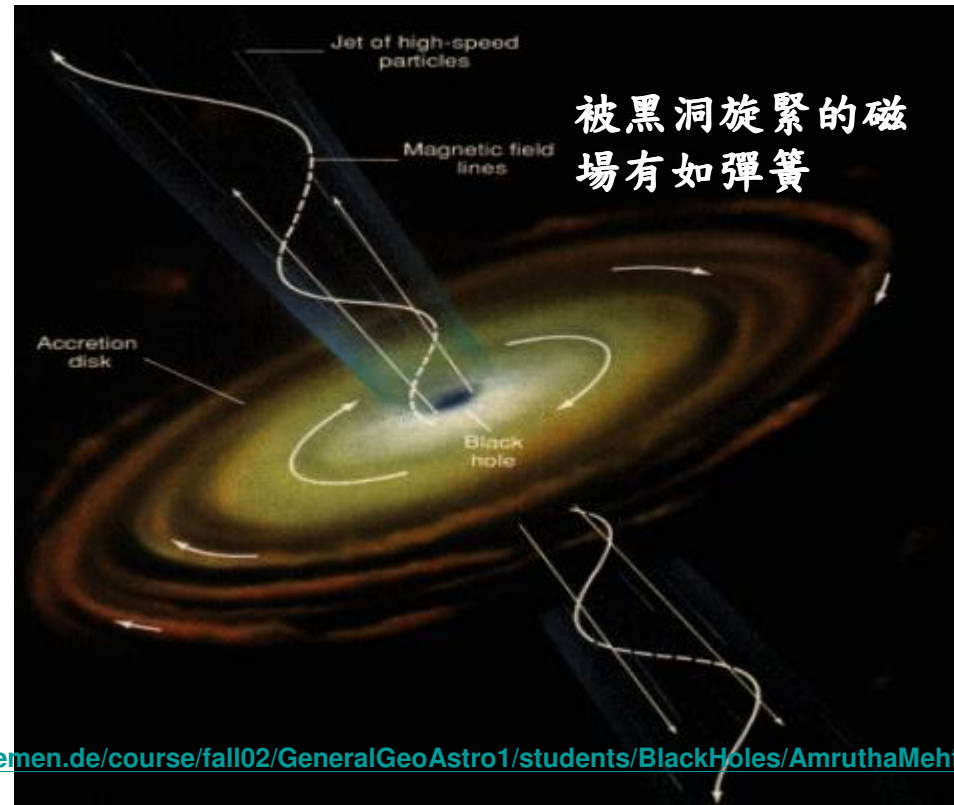
# Kerr Black Hole & Ergosphere (能層)

- Frame-dragging (空間跟著黑洞轉), tap black hole's rotational energy



**Kerr  
Black Hole**

<http://www.faculty.iu-bremen.de/course/fall02/GeneralGeoAstro1/students/BlackHoles/AmruthaMehta.html>



**讓我們務實一點吧**

# **How to find/see a black hole?**

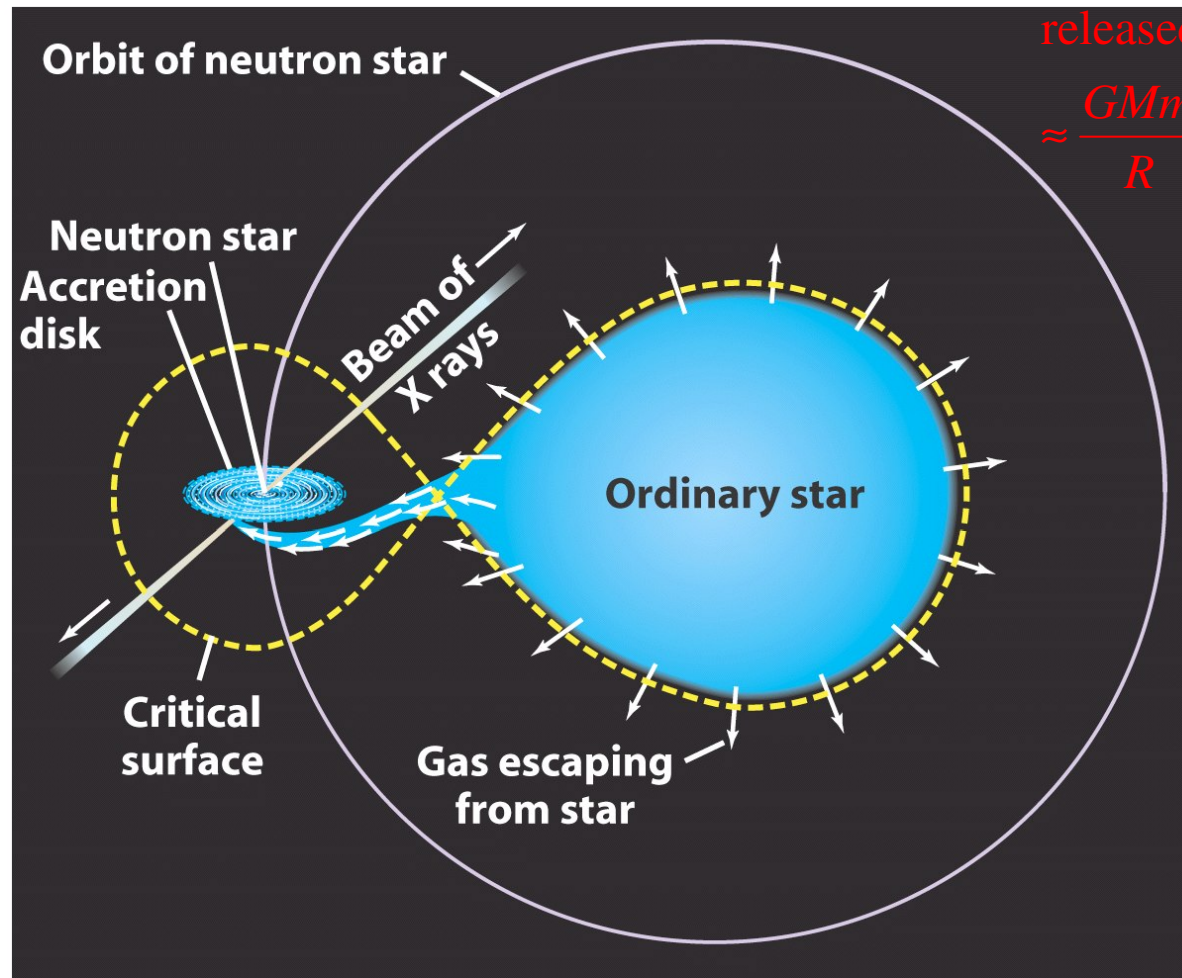
我們無法在黑暗中找一隻黑貓…

1. Hawking radiation is no use: too weak (no Nobel Prize for him ☹).
2. If a black hole is not alone, we may observe its influence on its nearby objects to imply its existence.

- stellar-mass black holes (collapsed stars)
- super-mass black holes (at the center of a galaxy)



# X-ray from an accretion disk (吸積盤) around a neutron star/black hole in a binary system



released gravitational energy

$$\approx \frac{GMm}{R} \propto \frac{1}{R} \Rightarrow \text{heat(X-ray)}$$

Neutron stars and black holes have a small radius  $R$ .

An indirect way to find a black hole (black holes have no hair).

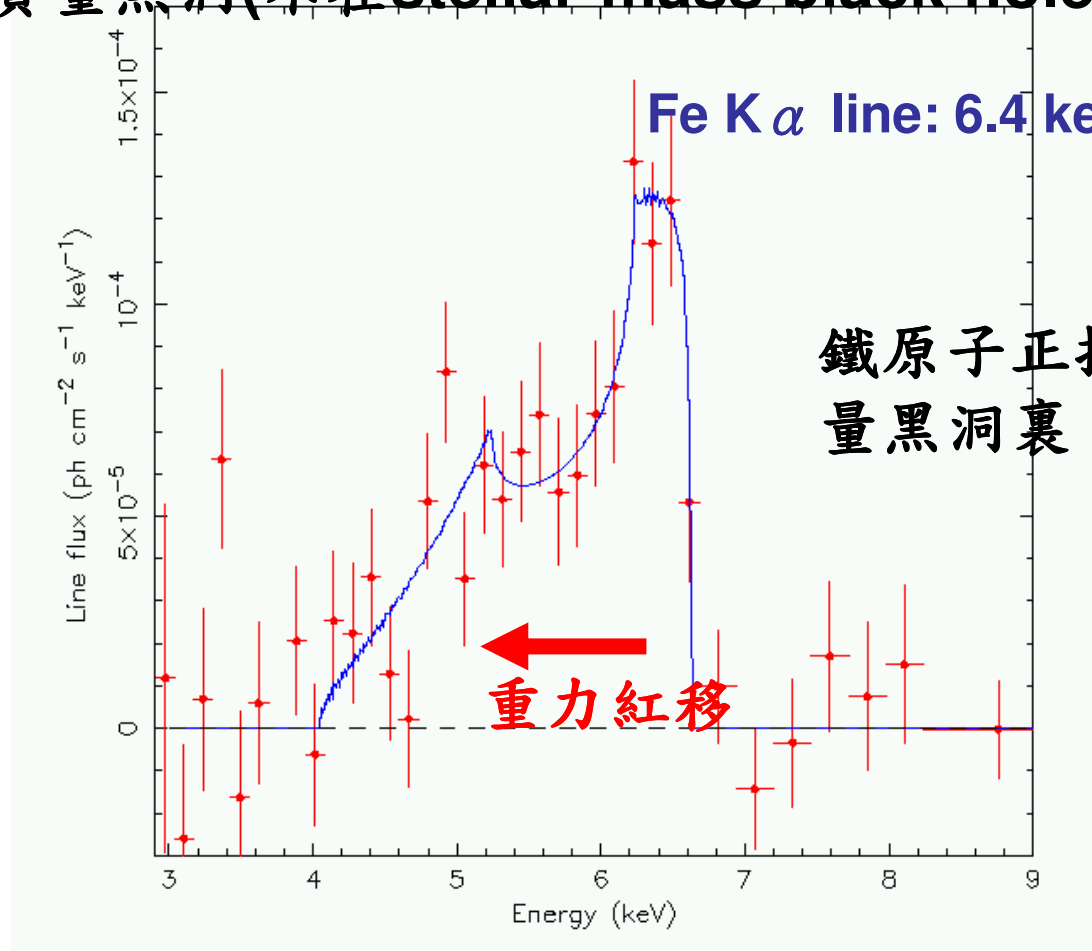
neutron star mass  $> 3$  Solar masses  $\rightarrow$  collapse

Figure 13-25  
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# 鐵原子x-ray線光譜的重力紅移

<http://heasarc.gsfc.nasa.gov/docs/asca/gallery/mcg6.html>

只會在超質量黑洞(不在stellar-mass black hole)附近發生

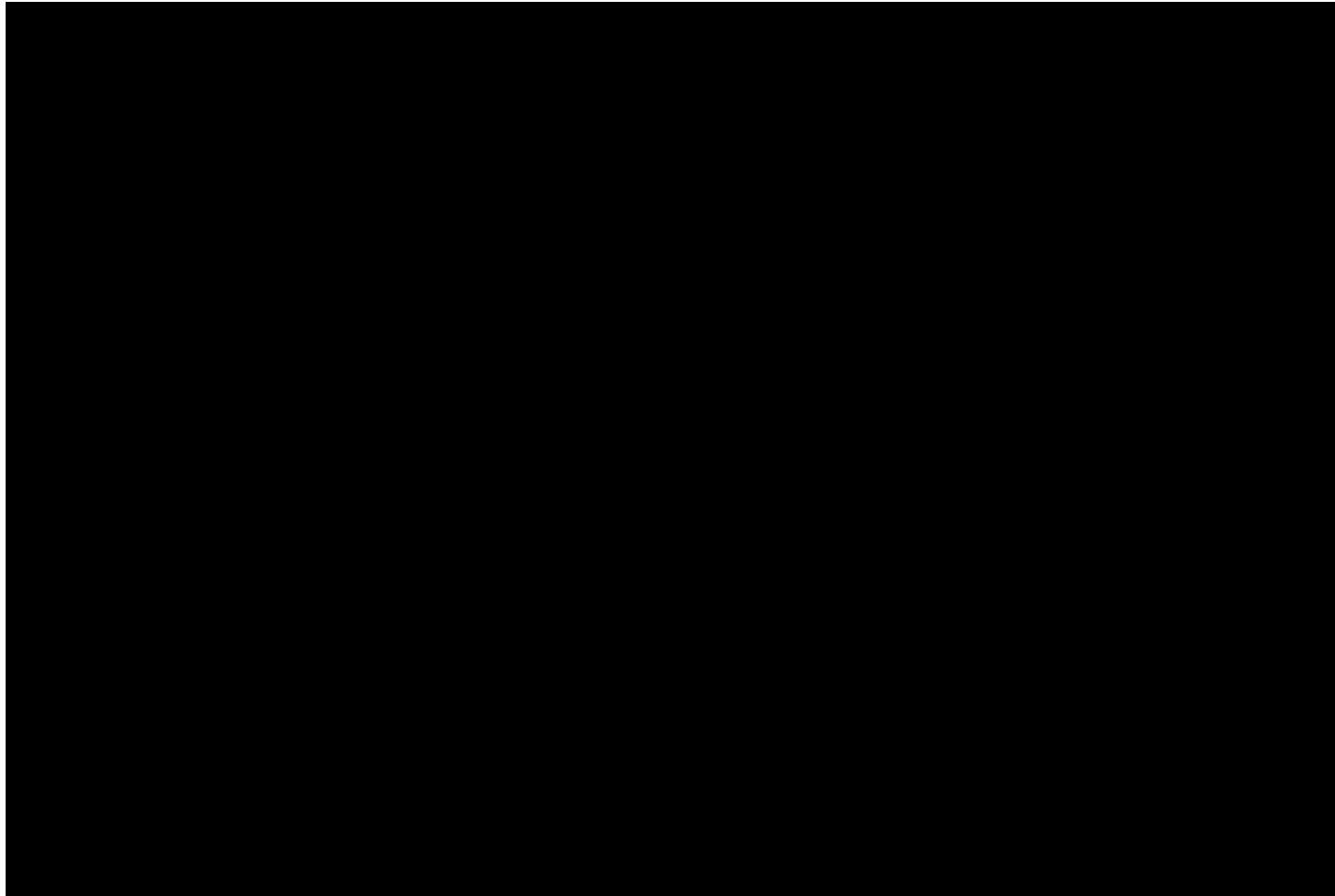


鐵原子正掉入超質量黑洞裏！

# NGC 6240: two galaxies are merging

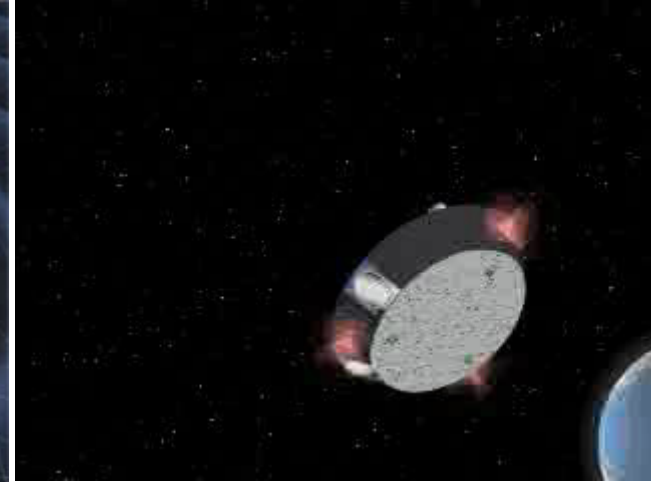
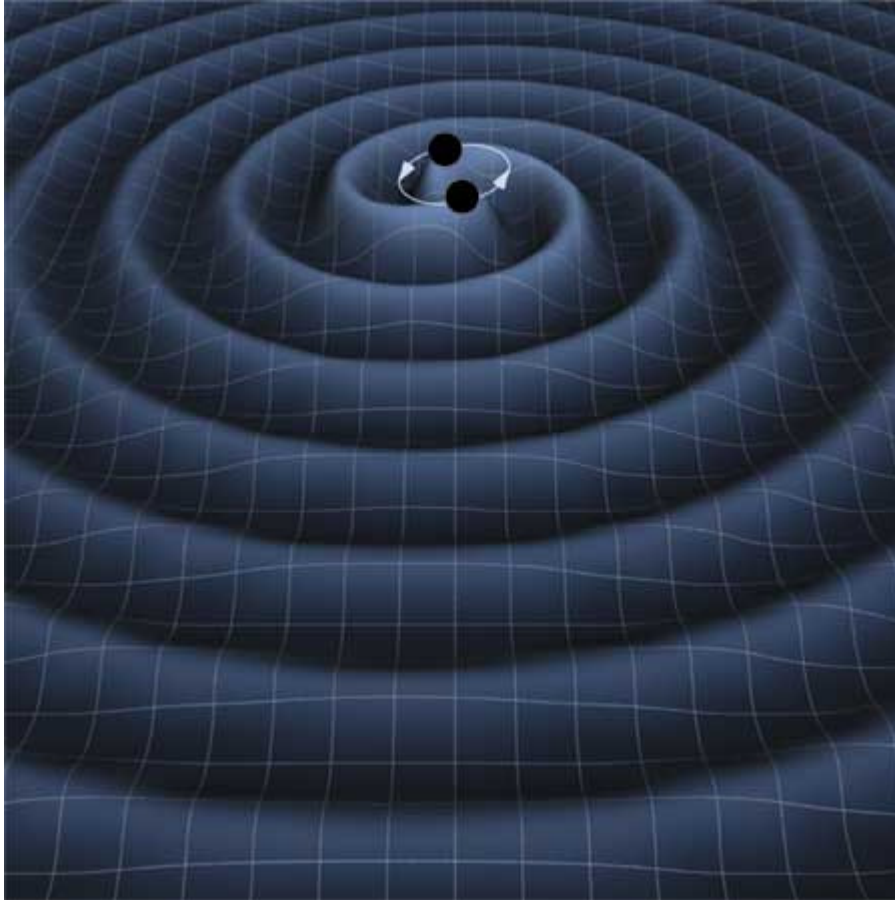
<http://chandra.harvard.edu/photo/2002/0192/animations.html>

**Chandra X-ray image:  
two black holes?**



# Merging black holes → “strong” gravitational waves (重力波)

<http://lisa.jpl.nasa.gov/>



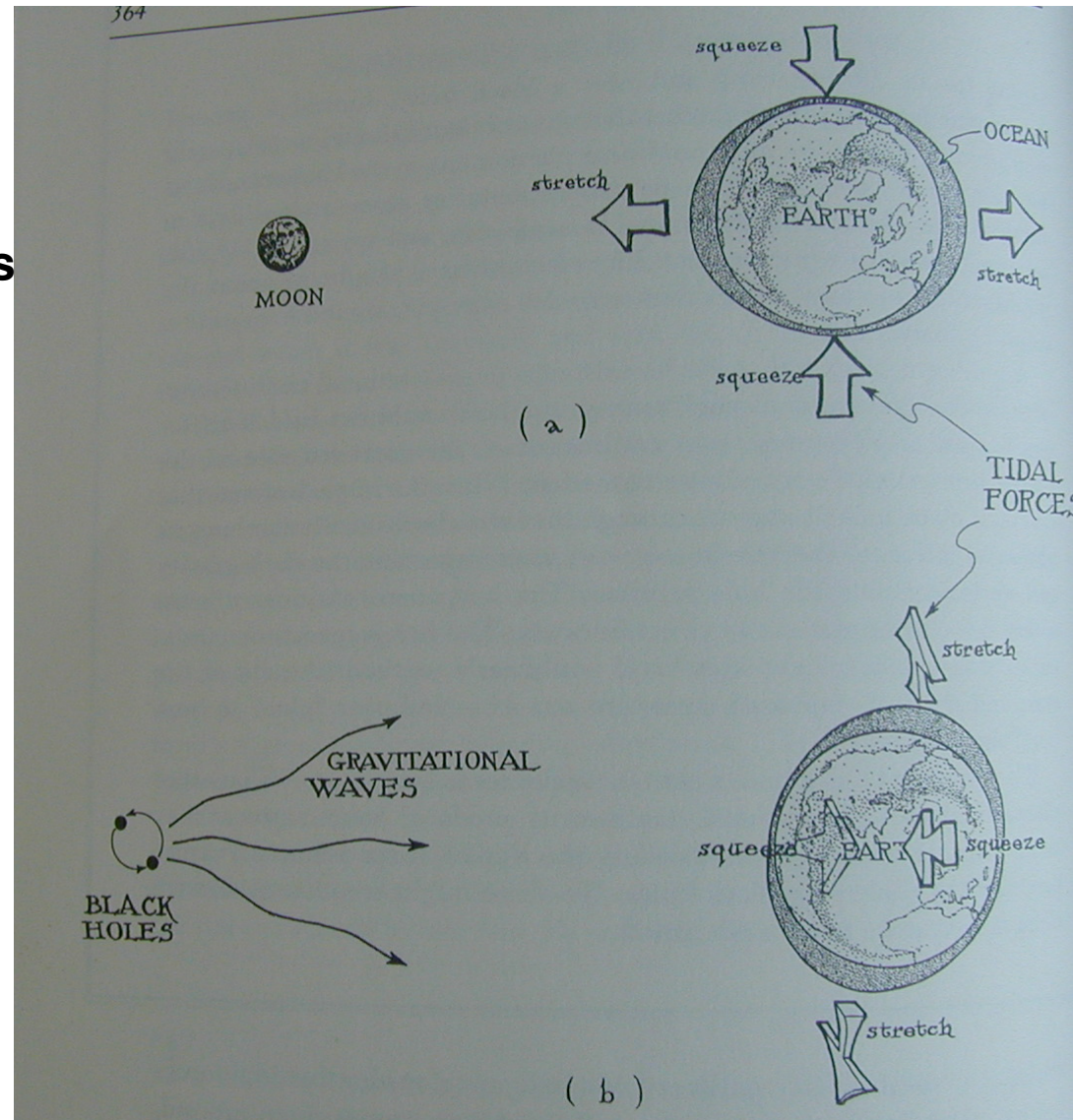
**Gravitational wave is still a million times less energetic than that in the cosmic microwave background radiation which, itself, is a billion times weaker than that in a household oven .**

**As the gravitational waves pass by, the change in distance between two**

**detectors will be as small as a size of proton!**

# 重力波的作用有點兒像潮汐作用

Kip Thorne:  
Black holes  
& time warps





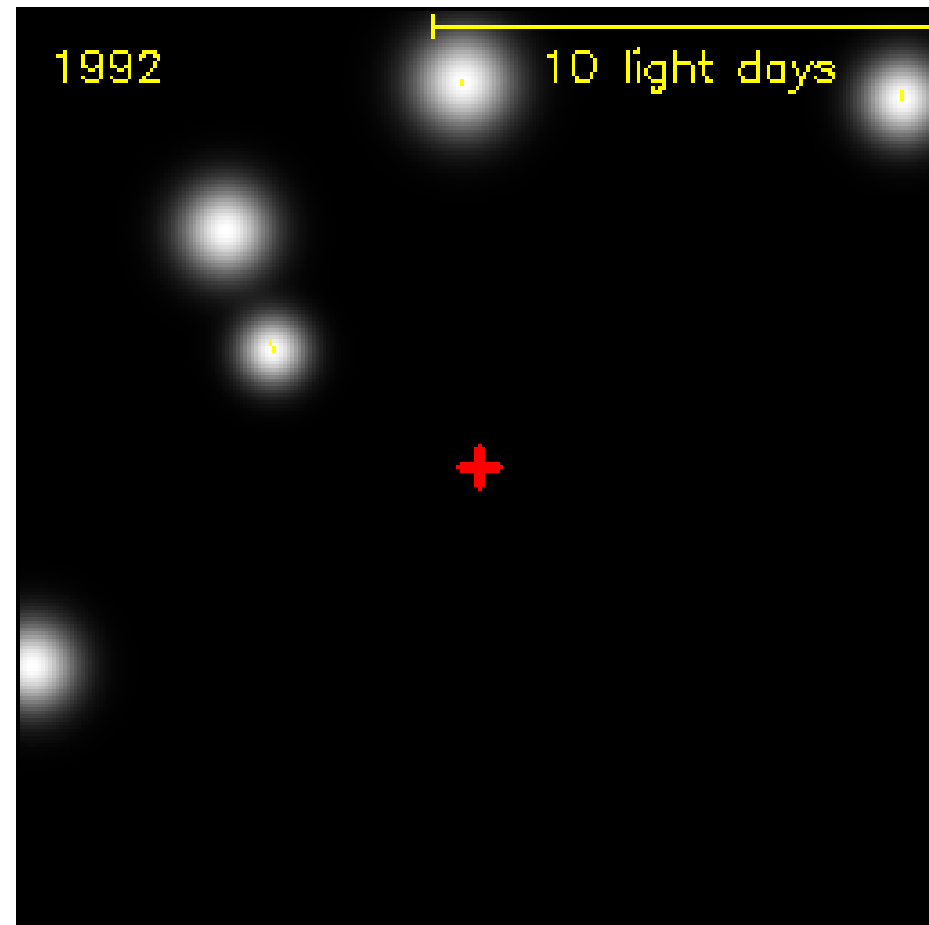
# Measuring the mass of a super massive black hole at the center of the Milky Way

<http://www.cfa.harvard.edu/~narayan/NJP/>

**Fast motion of stars**

→ **Mass of Sagittarius A\***  
≈  $2.5 \times 10^6$  solar masses  
→ Impossible to be stars  
→ the only known object  
we know of to explain this  
is...

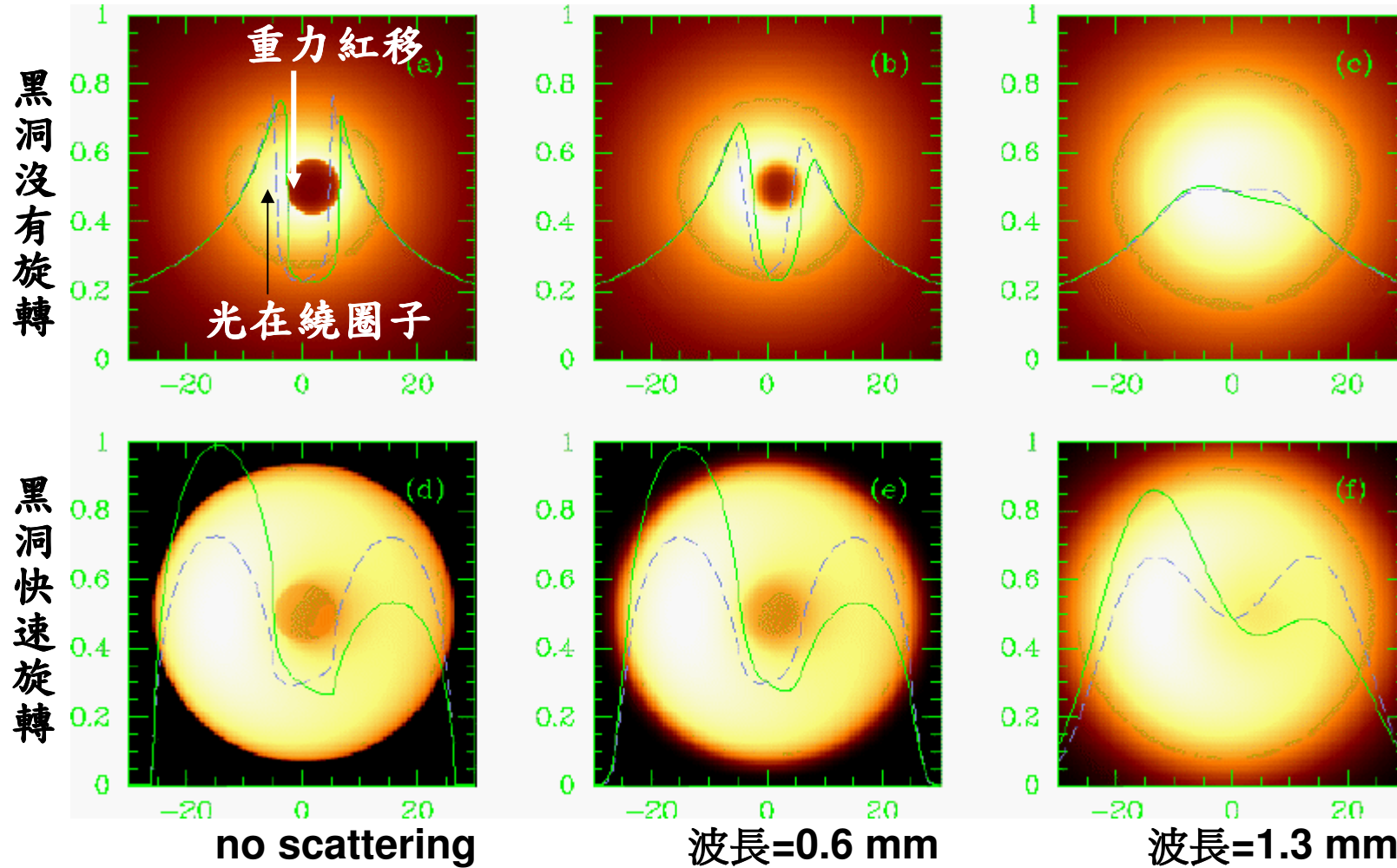
**Supermassive black hole!**  
(c.f. stellar-mass black  
hole resulting from a  
collapsed a massive star)



# 是否能真的看到黑洞：「黑洞的影子」！？

<http://www.mpifr-bonn.mpg.de/staff/hfalcke/bh/sld14.html>

黑洞在發光的吸積盤中，產生比事件穹界還大的「影子」！





scattering (散射): street lamp in the rain

同理，星際物質會散射黑洞  
旁邊吸積盤的光，使得黑洞  
的「影子」看不清楚。



The closest region to Sagittarius A\* we can see so far

# 廣設10座望遠鏡 不眠不休觀測10年

# 台中美科學家享黑洞實證

### 研究團隊繪製的黑洞圖像

■圖為根據望遠鏡看到影像所繪製的黑洞位置圖。

■圖為經電腦計算、調整後較接近實體的黑洞繪圖。

**240光年的範圍**

■台中美研究團隊利用特長基線干涉陣列望遠鏡，發現在人馬座A\*強烈無線電波發射的地方（強烈光源處），中間有一個超大質量黑洞。中研院提供

### 天文發現

「高瑋芬、張馨芳、台北報導」天文科學界在二、三十年前提出銀河系中心藏匿著大質量黑洞的推論，最近由台灣、中國、美國五名天文學家合作，透過對銀河系中心人馬座A\*（即人馬座A位置光源處）神秘電波源的高解析度觀測，終於找出支持這項觀點的有力證據。

這是天文學家首次看到距離銀河中心如此近的区域，並可做為檢驗「廣義相對論」的工具。這項重大發現刊登於本月三日出版的英國自然科學權威期刊《自然》(Nature)。

台中美研究團隊五名成員都曾是中研院天文所的教授或客座學人，包括來自中國科學院上海天文台研究員沈志強、美國國家電波天文台台長魯國鏞、美國加州理工學院的梁茂昌、中研院天文所特聘研

該小組利用國際先進的特長基線干涉陣列（簡稱VLA）天文望遠鏡，在二〇〇二年十一月首次獲得人馬座A\*在三點五毫米波長上的影像，由此推斷出的最小質量密度比目前任何已知可能的黑洞密度都要大一萬倍以上，強烈支持人馬座A\*的超大質量黑洞本質。這項發現經過兩年多的驗證，至今才在權威期刊《自然》公布成果。

質曾樸受訪時說，五名研究成員十年來在美國夏威夷、加州、華盛頓州、愛荷華州、新墨西哥州

質曾樸對此次發現銀河系中心存在超大質量黑洞的證據，相當高興。

廖瑞祥攝

### 國際研究學者團隊成員

學者	曾任中研院職務
質曾樸	現任主任
沈志強	天文所籌備處副教授
魯國鏞	天文所籌備處主任
梁茂昌	天文所籌備處研究助理
趙軍輝	天文所籌備處客座學人

資料來源：中研院

### 黑洞小檔案

**定義** 黑洞是擁有強大引力的物體，引力之大即使是宇宙中速度最高的光線也不能逃離黑洞

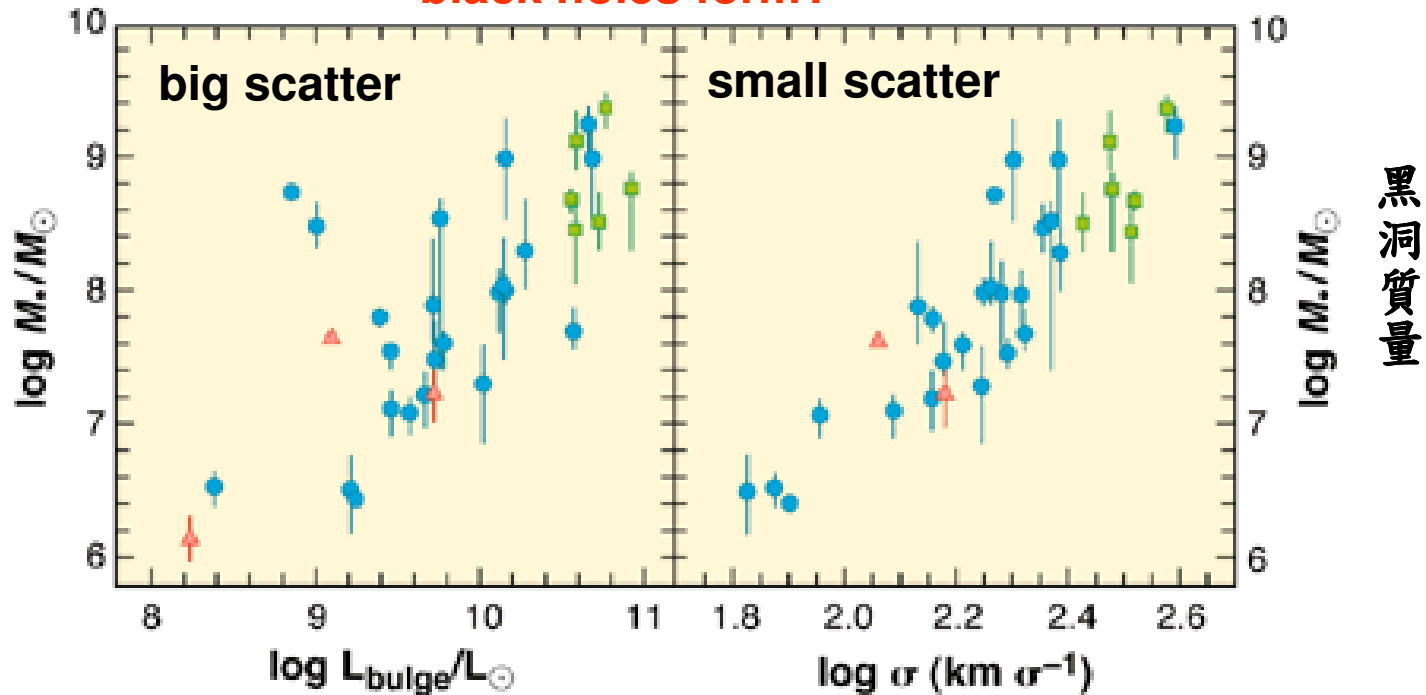
**起源** 1907~1915年愛因斯坦發展廣義相對論，預測該天體的存在；1960年代則由美國科學家約翰惠勒創立黑洞一詞

資料來源：中央大學天文所副教授孫維新

# Mass-Velocity Dispersion Relation for Super-massive Black Holes

Kormendy 2000

Tell us about how galaxies & super-massive black holes form?



黑洞質量

circle: stellar dynamics  
square: ionized gas dynamics  
triangle: maser disk dynamics

天體在星系球核  
(galactic bulge)內的環繞速度

# 有中等質量的黑洞(intermediate-mass )嗎？

Can the mass of a black hole be between stellar mass (3-20 solar masses) and super-mass ( $>10^6$  solar masses)?

**X-ray intensity  $\rightarrow$  mass**

Some x-rays sources seem to imply their mass lies in the intermediate mass range. For instance, an X-ray source in the starburst galaxy “M82 X-1”

[http://www.nasa.gov/centers/goddard/news/topstory/2005/new\\_blackhole.html](http://www.nasa.gov/centers/goddard/news/topstory/2005/new_blackhole.html)