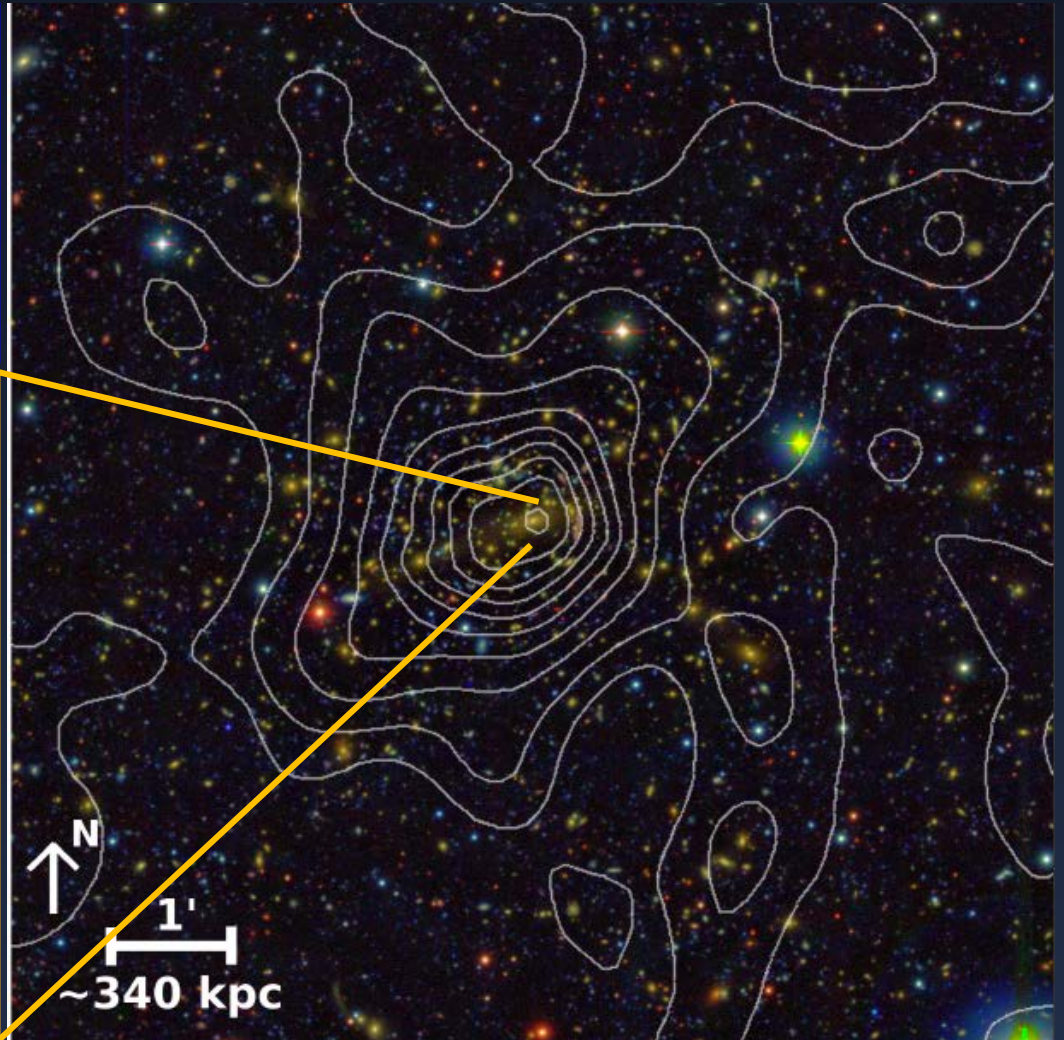


# Subaru Shear-and-Magnification Weak-Lensing Analysis of CLASH Galaxy Clusters

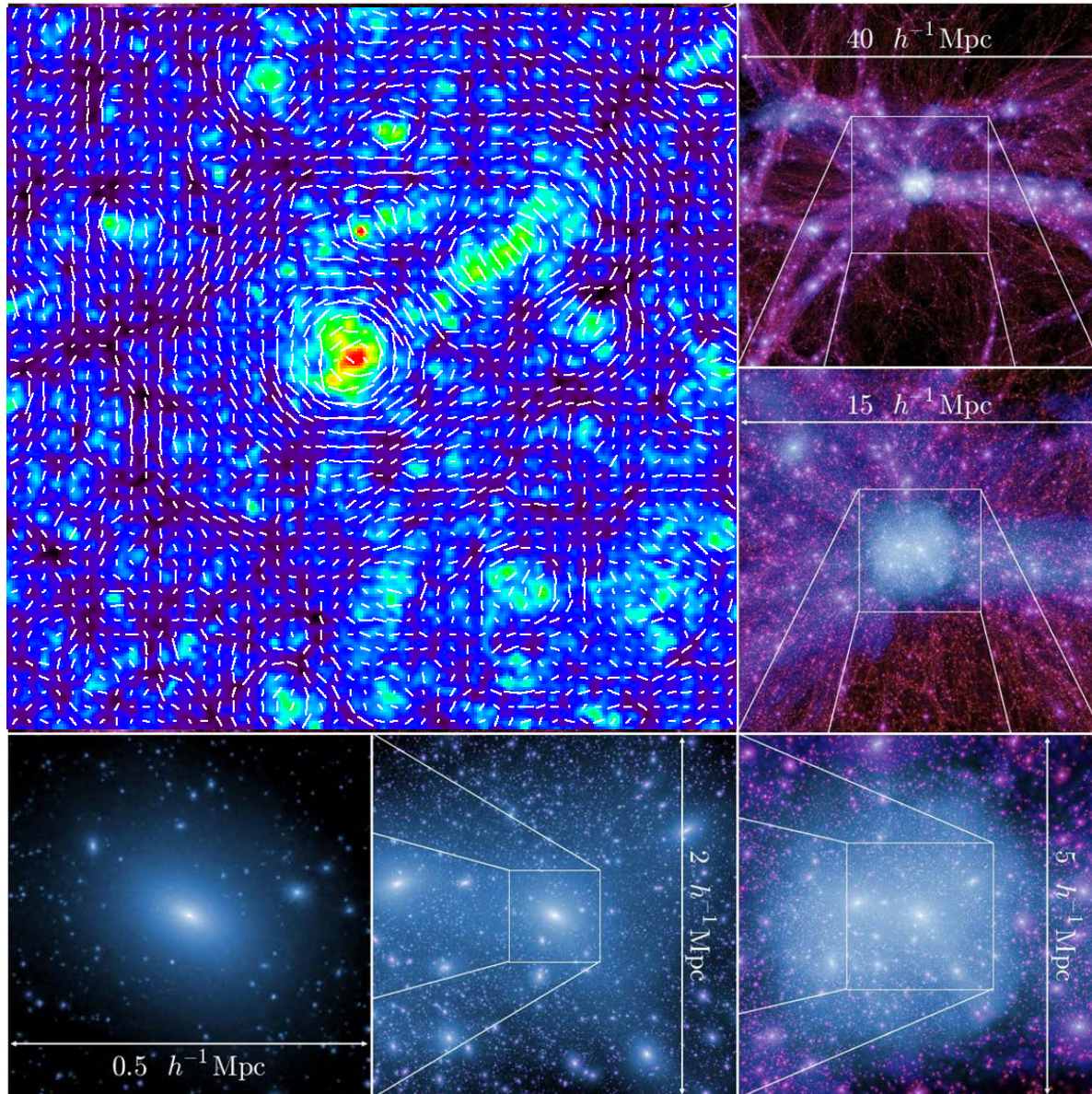
Cluster Lensing And Supernova survey with Hubble



Keiichi Umetsu (ASIAA, Taiwan) with the CLASH team



# Weak Lensing for Cluster Cosmology



## Key Ingredients

### Halo structure (1h)

- Mass,  $M_{200c}$
- Density profile,  $\rho(r)$
- Concentration,

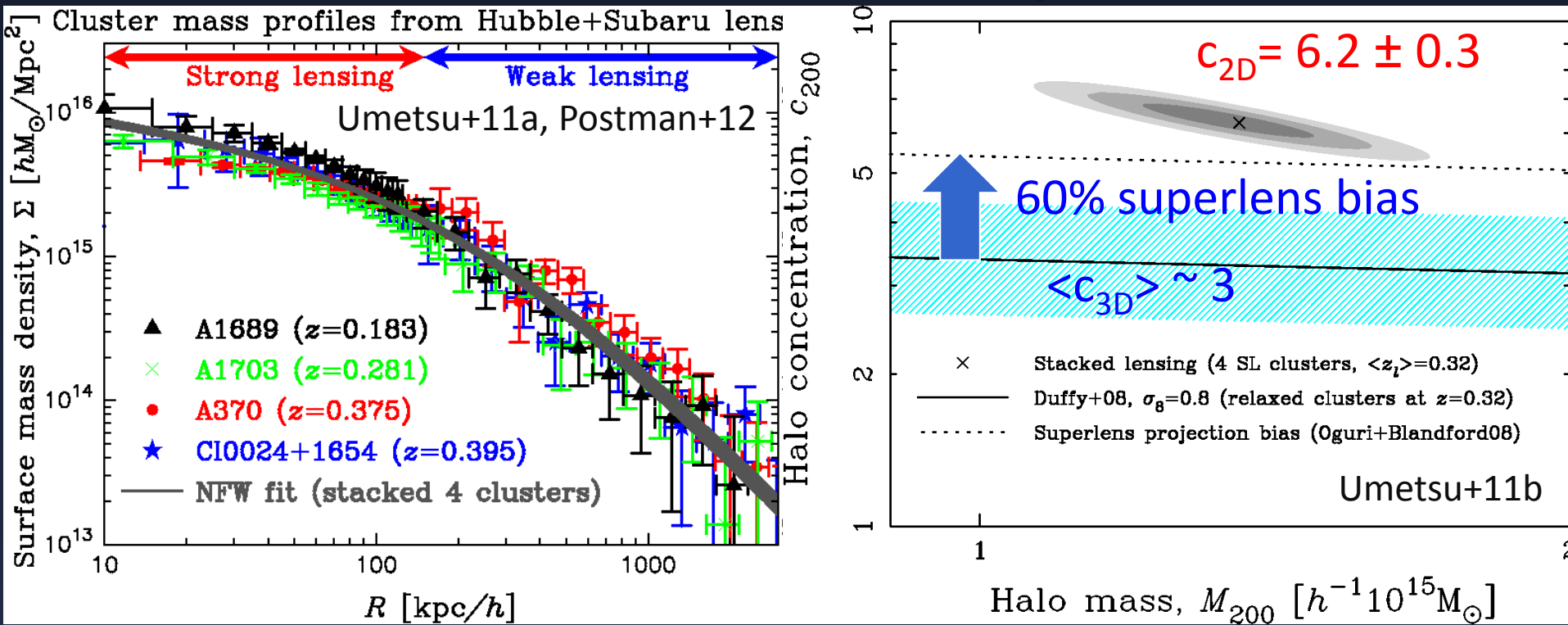
$$c_{200c} = r_{200c} / r_{-2}$$

### Surrounding LSS (2h)

- Halo bias  $b(M, z)$
- Primordial matter  $P(k)$

# CLASH Objectives & Motivation

Before CLASH (2010), deep-multicolor Strong (*HST*) + Weak (*Subaru*) lensing data only available for a handful of “super lens” clusters

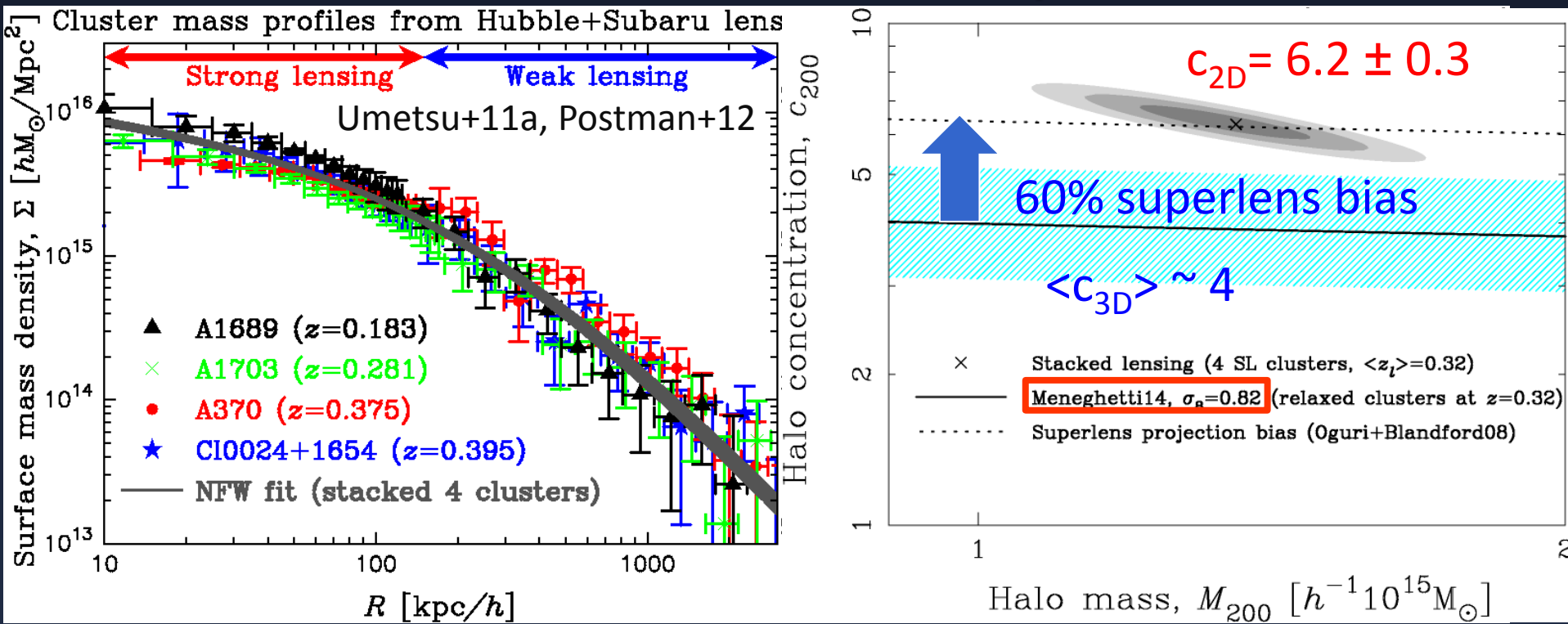


**Total mass profile shape:** consistent w self-similar NFW (cf. Newman+13; Okabe+13)

**Degree of concentration:** predicted superlens correction not enough if  $\langle c_{\text{LCDM}} \rangle \sim 3$ ?

# CLASH Objectives & Motivation

Before CLASH (2010), deep-multicolor Strong (*HST*) + Weak (*Subaru*) lensing data only available for a handful of “super lens” clusters



**Total mass profile shape:** consistent w self-similar NFW (cf. Newman+13; Okabe+13)

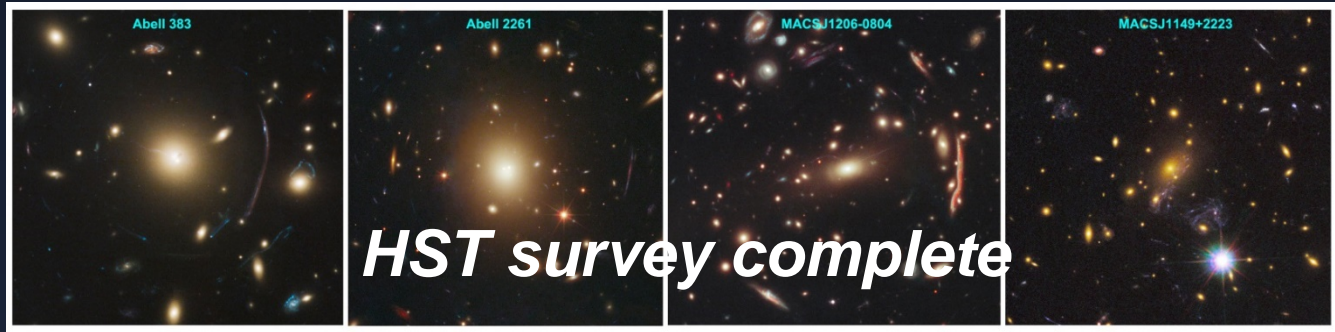
**Degree of concentration:** predicted superlens correction is just enough if  $\langle c_{\text{LCDM}} \rangle \sim 4$



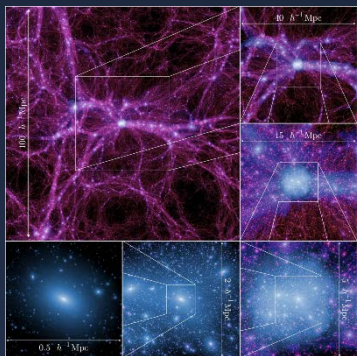


# CLASH: Observational + Theory Efforts

A 524-orbit *HST* Treasury Program to observe 25 clusters in 16 filters (0.23-1.6  $\mu\text{m}$ ) (Postman+CLASH 12)



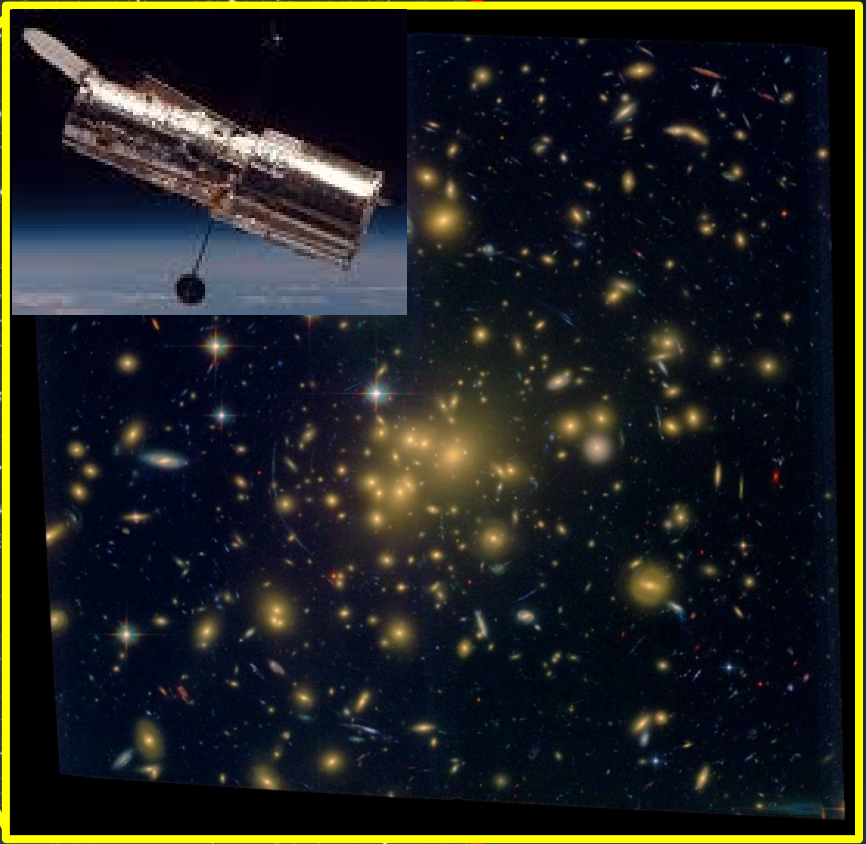
**Wide-field Subaru imaging** (0.4 - 0.9  $\mu\text{m}$ ) plays a unique role in complementing deep HST imaging of cluster cores (Umetsu et al. 2014, *ApJ*, 795, 163)



**MUSIC-2** (hydro + N-body re-simulation) provides an accurate characterization of CLASH sample with testable predictions (Meneghetti+14, *ApJ*, in press; arXiv:1404.1384)

***SUBARU* (S-Cam) multi-color  
imaging for wide-field weak**

**High-resolution space imaging  
with *HST* (ACS/WFC3) for  
strong lensing**



**34 arcmin**





# CLASH X-ray-selected Subsample ( $0.18 < z < 0.9$ )

- **X-ray morphology +  $T_x$  selection**

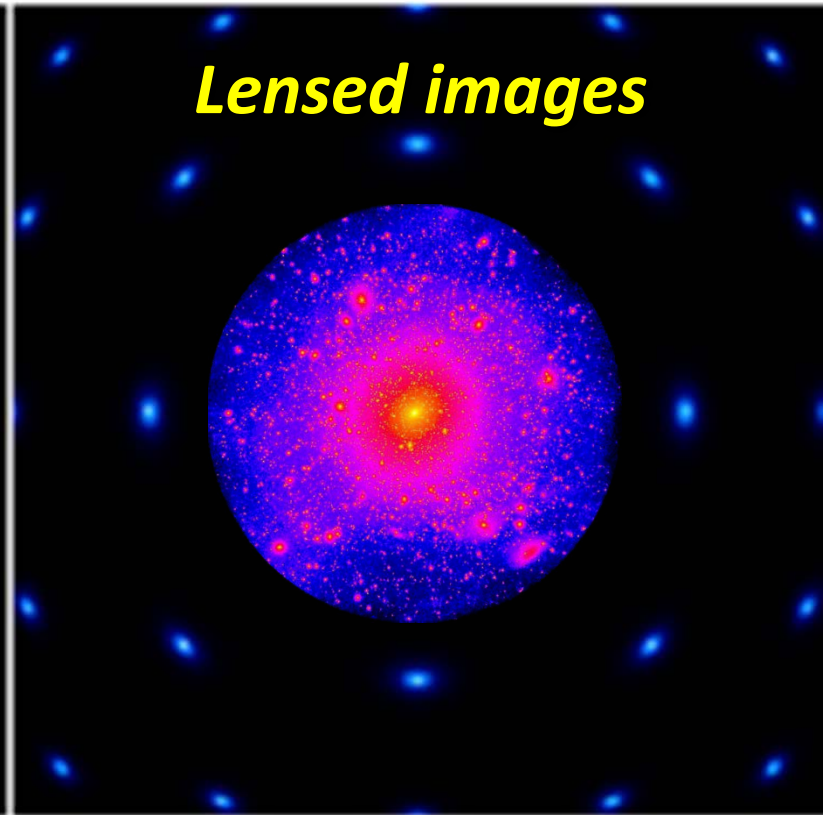
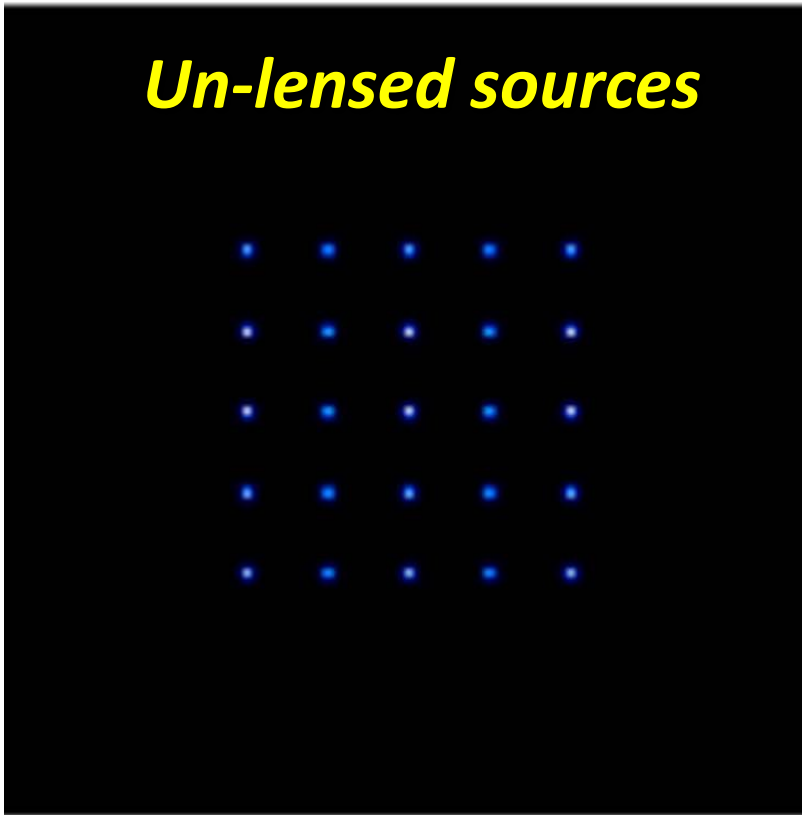
- $T_x > 5\text{keV}$  ( $M_{200c} > 5e14 M_{\text{sun}}/h$ )
- Small BCG to X-ray-peak offset,  $\sigma_{\text{off}} \sim 10\text{kpc}/h$
- Smooth regular X-ray morphology

→ **Optimized for radial-profile analysis ( $R > 2\sigma_{\text{off}} \sim 20\text{kpc}/h$ )**

- **CLASH theoretical predictions** (Meneghetti+CLASH 14)

- Composite relaxed (70%) and unrelaxed (30%) clusters
- Mean  $\langle c_{200c} \rangle = 3.9$ ,  $\sigma(c_{200c}) = 0.6$ ,  $c_{200c} = [3, 6]$
- Negligible orientation bias ( $\sim 2\%$  in  $\langle M_{3D} \rangle$ )
- $>90\%$  of CLASH clusters to have strong-lensing features

# Shear and Magnification Effects



- **Shear**

*Sensitive to “modulated” matter density*

✓ Geometric shape dist.:  $\delta e_+ \sim \gamma_+$

$\Sigma_{\text{crit}} \gamma_+ = \Delta \Sigma(R) \equiv \Sigma(< R) - \Sigma(R)$

- **Magnification**

*Sensitive to “total” matter density*

✓ Flux amplification:  $\mu F$

$\mu \approx 1 + 2\kappa; \quad \Sigma_{\text{crit}} \kappa = \Sigma(R)$

✓ Geometric area dist.:  $\mu \Delta \Omega$

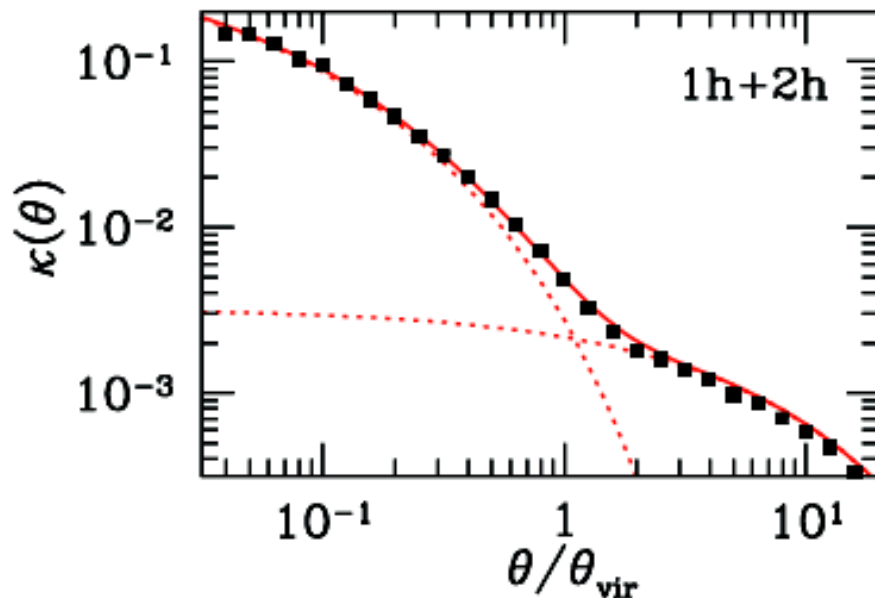


# Shear doesn't see mass sheet

Averaged lensing profiles in/around LCDM halos (Oguri+Hamana 11)

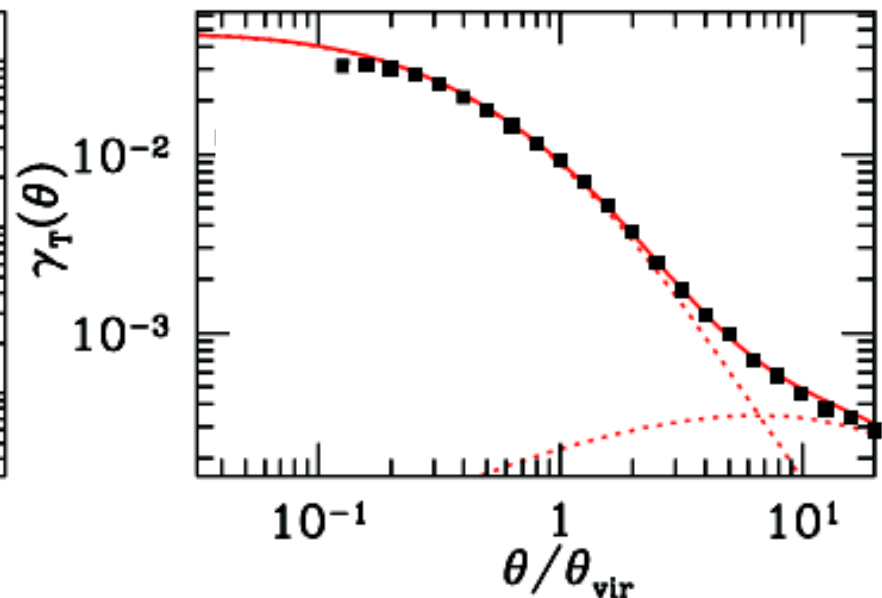
Total

$$\kappa = \Sigma(R) / \Sigma_{\text{crit}}$$



Modulated

$$\gamma_+ = \Delta\Sigma(R) / \Sigma_{\text{crit}}$$



- Tangential shear is a powerful probe of **1-halo term**, or **internal halo structure**.
- Shear alone cannot recover absolute mass, known as **mass-sheet degeneracy**:

$\gamma$  remains unchanged by  $\kappa \rightarrow \kappa + \text{const.}$



# CLASH Weak-Lensing Results (1)

Ensemble-averaged dark-matter halo structure:

- Cluster halo density profile,  $\langle \Delta \Sigma(R) \rangle$
- Degree of mass concentration,  $\langle C_{200c} \rangle$

from *stacked-shear-only WL* analysis

of 16 CLASH X-ray-selected clusters

Umetsu+CLASH 2014, *ApJ*, 795, 163 (arXiv:1404.1375)



# Averaged Halo (1h) Density Profile

Stacking of WL-shear signals by weighting individual clusters according to the sensitivity kernel matrix:

$$\langle\langle \widehat{\Delta\Sigma}_+ \rangle\rangle = \left( \sum_n \mathcal{W}_{+n} \right)^{-1} \left( \sum_n \mathcal{W}_{+n} \widehat{\Delta\Sigma}_{+n} \right),$$

*Summing over clusters (n=1, 2, ..)*

with individual sensitivity matrix

$$(\mathcal{W}_{+n})_{ij} \equiv \Sigma_{c,n}^{-2} (C_{+n}^{-1})_{ij}$$

defined with total covariance matrix

$$C_+ = C_+^{\text{stat}} + C_+^{\text{sys}} + C_+^{\text{lss}}.$$

**With “trace-approximation”, averaging (stacking) is interpreted as**

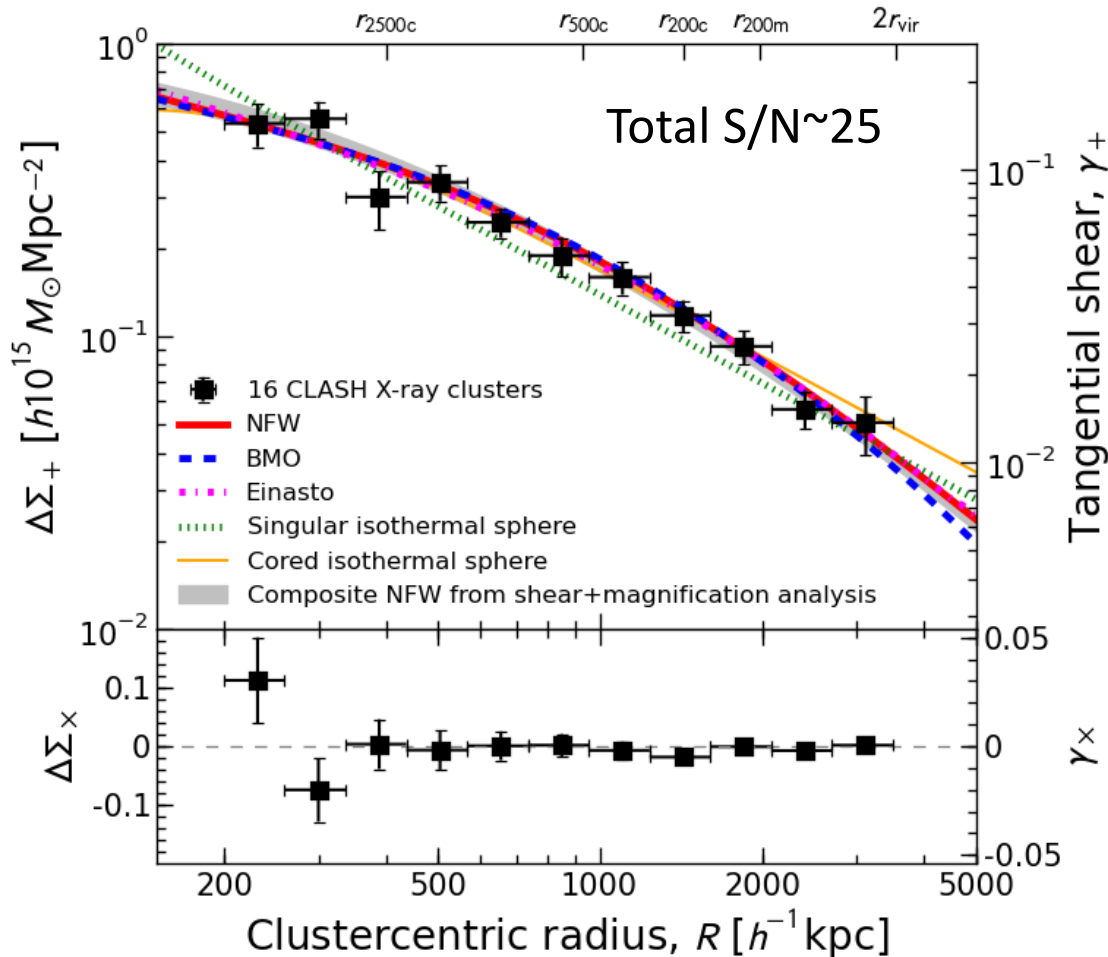
$$\langle\langle \Sigma_c^{-1} \rangle\rangle = \frac{\sum_n \text{tr}(\mathcal{W}_{+n}) \Sigma_{c,n}^{-1}}{\sum_n \text{tr}(\mathcal{W}_{+n})},$$

Umetsu et al. 2014,  
*ApJ*, 795, 163





# Stacked Halo Density Profile $\Delta\Sigma(R)$



Stacked-shear-only analysis provides a net 1-halo-only constraint ( $\gamma_{+,2h} < 10^{-3}$ ) at  $\langle z \rangle = 0.35$

**NFW** an excellent fit (PTE = 0.66)

- $M_{200c} = (1.3 \pm 0.1) 10^{15} M_{\text{sun}}$
- $c_{200c} = 4.01 (+0.35, -0.32)$

**Einasto** model (PTE=0.51)

- Einasto shape parameter  $\alpha = 0.19 \pm 0.07$ , consistent with NFW profile curvature ( $\alpha \sim 0.18$ )

Umetsu+CLASH 14, *ApJ*, 795, 163

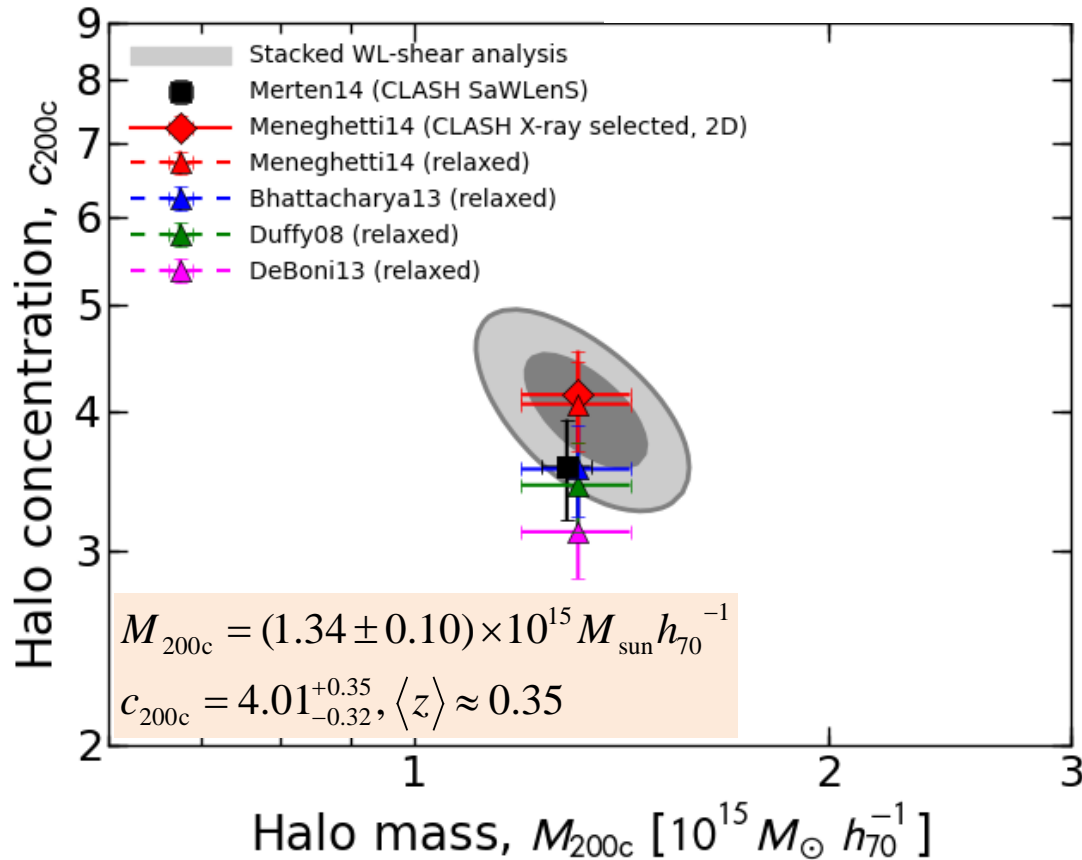
Consistent w a family of density profiles for collisionless DM halos (NFW, truncated variants of NFW, Einasto)



# Integrated Constraints on $c(M_{200c}, z)$

Theoretical predictions  
for stacked  $c(M, z)$

$$\langle c_{200c} \rangle = \frac{\int dM dz N(M, z) \hat{c}_{200c}(M, z)}{\int dM dz N(M, z)} \approx \frac{\sum_n \text{tr}(\mathcal{W}_n) \hat{c}_{200c}(M_n, z_n)}{\sum_n \text{tr}(\mathcal{W}_n)}$$



**Variance in theory due primarily to different cosmology ( $\sigma_8$ )**

Meneghetti14:  $\sigma_8=0.82$

Bhattacharya13:  $\sigma_8=0.8$

Duffy08:  $\sigma_8=0.796$

DeBoni13:  $\sigma_8=0.776$

- Excellent agreement with CLASH predictions (M14),  $c_{200c} \sim 4.0$
- Consistent with Bhatt13, Duffy08 predictions for “relaxed” halos at  $1\sigma$ ,  $c_{200c} \sim 3.6$



# CLASH Weak-Lensing Results (2)

Individual cluster mass properties:

- **Cluster mass profiles**  $\Sigma(R)$  from **joint *shear* + *magnification* WL analysis**
- **Cluster mass estimates** ( $M_{500c}$ ,  $M_{200c}$ ,  $M_{vir}$ ,  $M_{200m}$ ) assuming spherical NFW profiles

of 20 CLASH Clusters

Umetsu+CLASH 2014, *ApJ*, 795, 163 (arXiv:1404.1375)



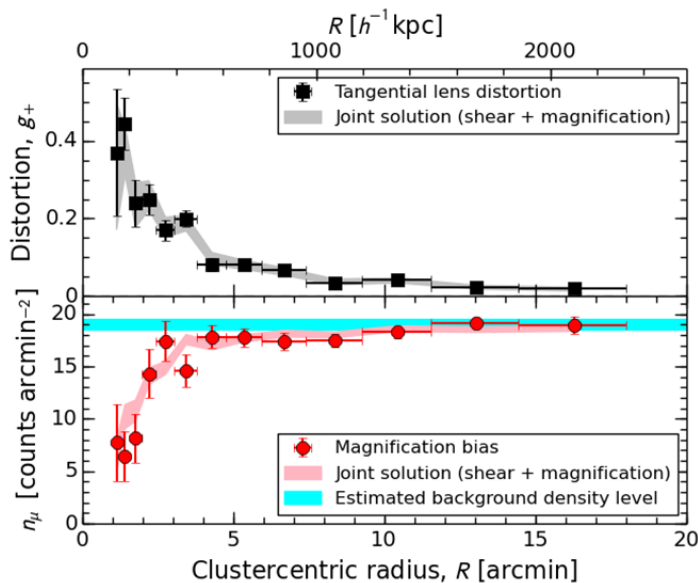
# Combining Shear and Magnification

**Bayesian joint likelihood approach** (Umetsu+11a; Umetsu 13)

Tangential (reduced) shear  
Inverse magnification

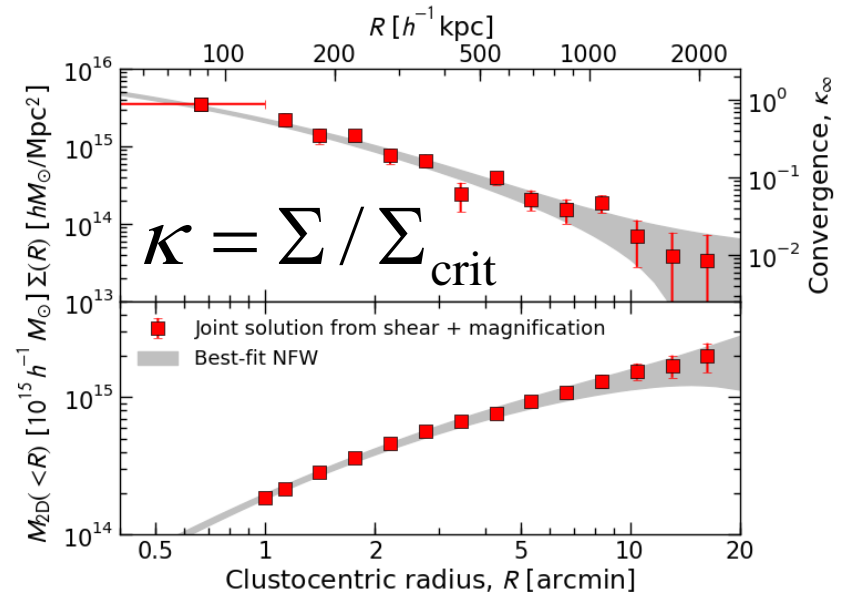
$$g_+(R) = \frac{\kappa(< R) - \kappa(R)}{1 - \kappa(R)},$$

$$\mu^{-1}(R) = [1 - \kappa(R)]^2 - [\kappa(< R) - \kappa(R)]^2$$



$g_+$

$\mu$



- Mass-sheet degeneracy broken
- Total statistical precision improved by  $\sim 20\text{-}30\%$
- Calibration uncertainties marginalized over:  $c = \{\langle W \rangle_s, f_{W,s}, \langle W \rangle_\mu, \bar{n}_\mu, s_{\text{eff}}\}$ .



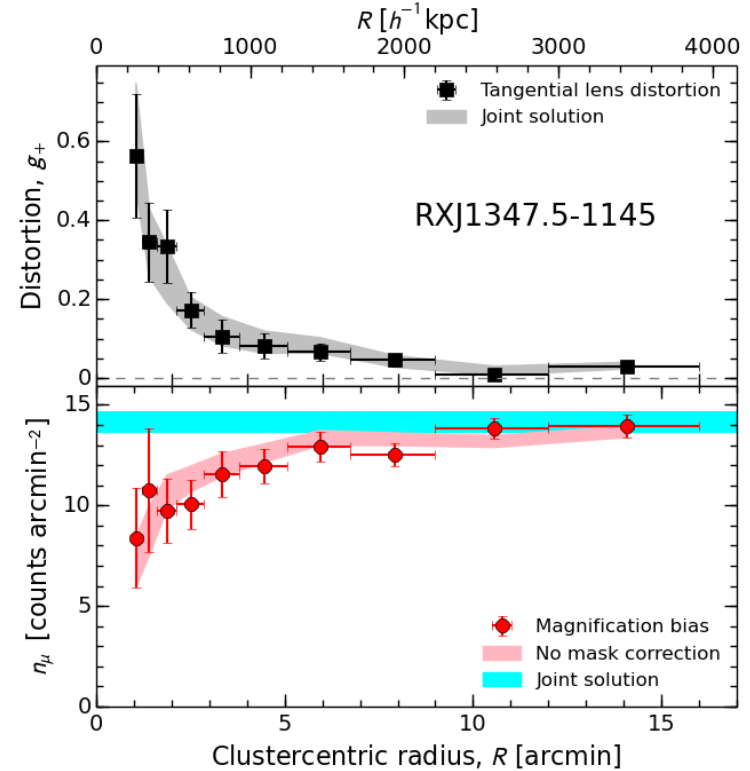
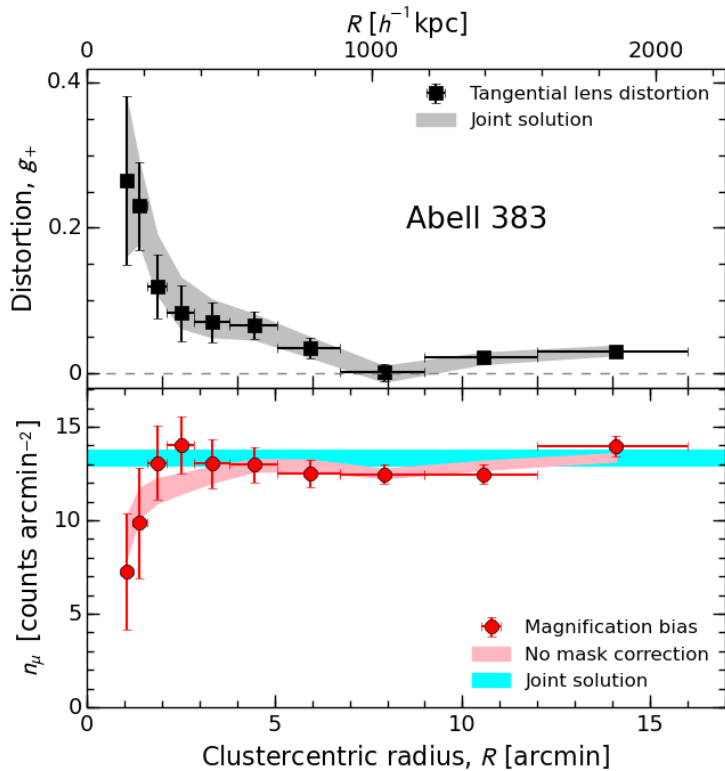
# Joint Shear + Magnification WL Analysis

CLASH low mass

$M_{200c} = 6e14 M_{\text{sun}}/h$  ( $z=0.19$ )

CLASH high mass

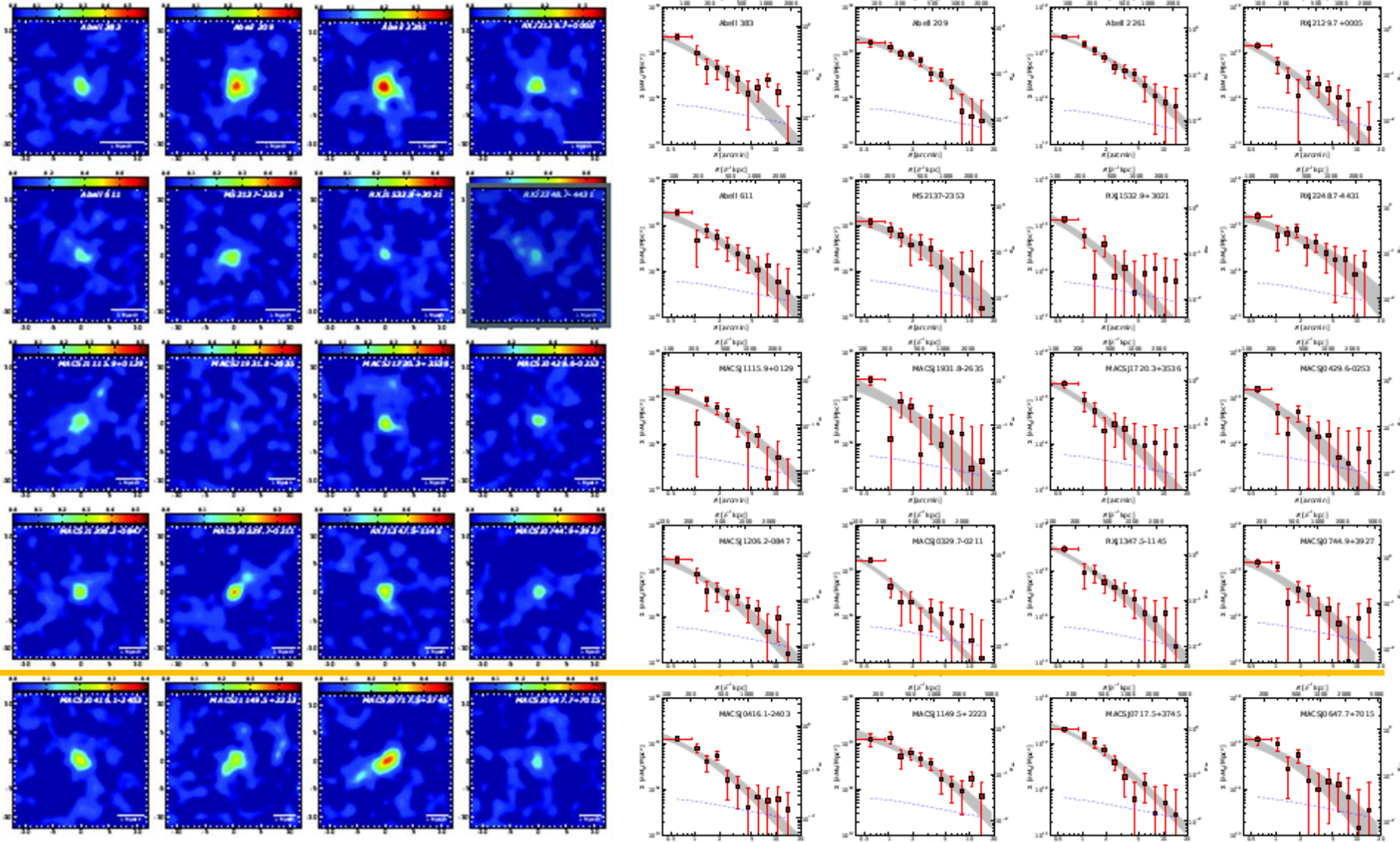
$M_{200c} = 20e14 M_{\text{sun}}/h$  ( $z=0.45$ )



Shear-magnification consistency:  $\langle \chi^2/\text{dof} \rangle = 0.92$  for 20 CLASH clusters  
Systematic mass calibration uncertainty  $\sigma_{M,3D} < 8\%$



# CLASH Mass Density Profile Dataset



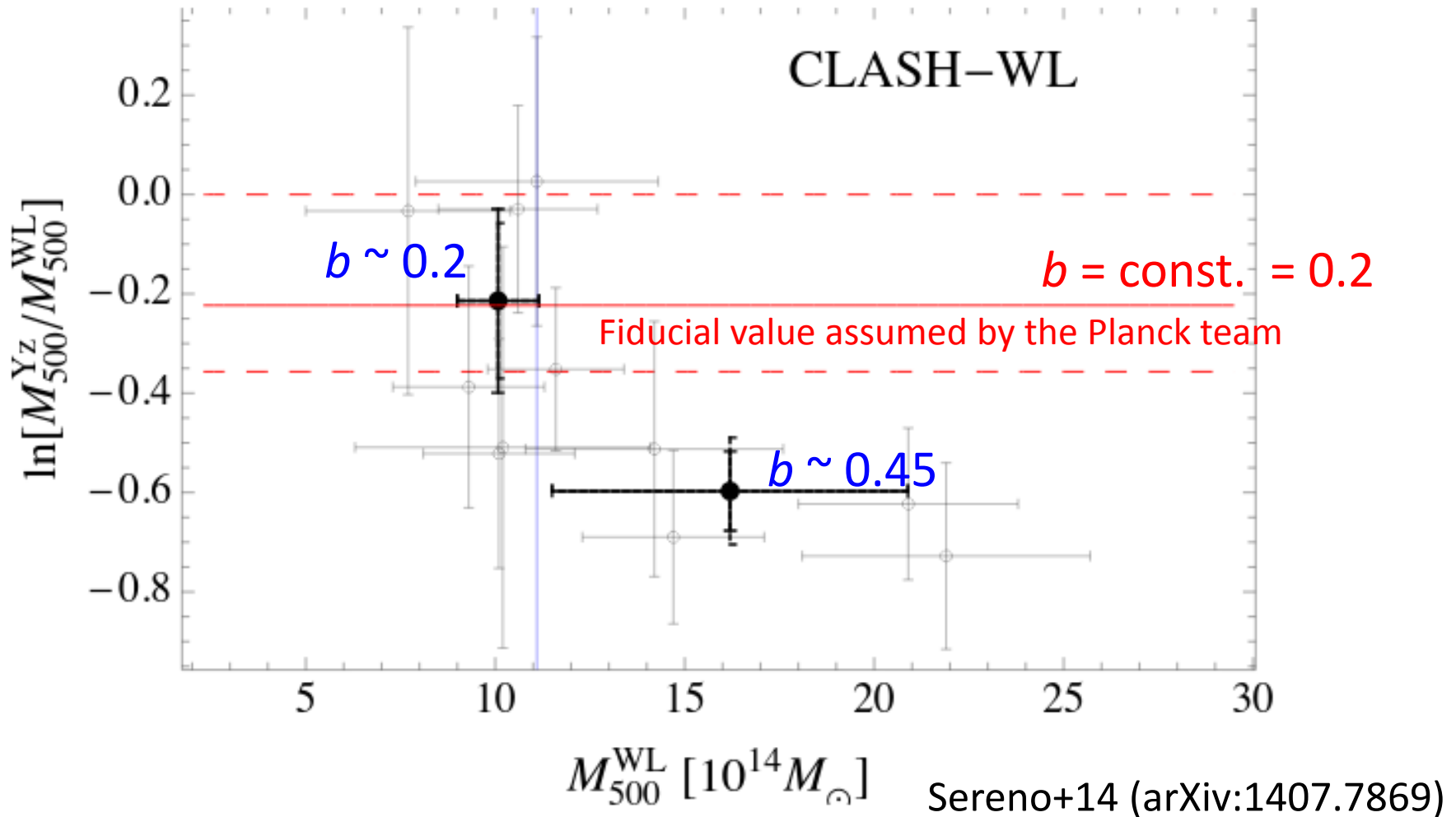
Umetsu+CLASH 2014, *ApJ*, 795, 163 (arXiv:1404.1375)





# Comparison with *Planck* Masses

Mass-dependent bias (20-45%) observed for *Planck* mass estimates





# CLASH: Strong-lensing, Weak-lensing Shear and Magnification

- Mass profile reconstruction from **full likelihood analysis of Strong-Lensing, Weak-Lensing shear and magnification** constraints (Umetsu13 multi-probe method)

$$L(\boldsymbol{\kappa}) = L_g(\boldsymbol{\kappa} | g_+) L_\mu(\boldsymbol{\kappa} | \mu^{\alpha-1}) L_{\text{SL}}(\boldsymbol{\kappa} | M_{2\text{D}})$$

1. Stacked mass profile analysis  $\langle \Sigma(R) \rangle$  at  $R = [0.01, 2] r_{\text{vir}}$

**1h term**

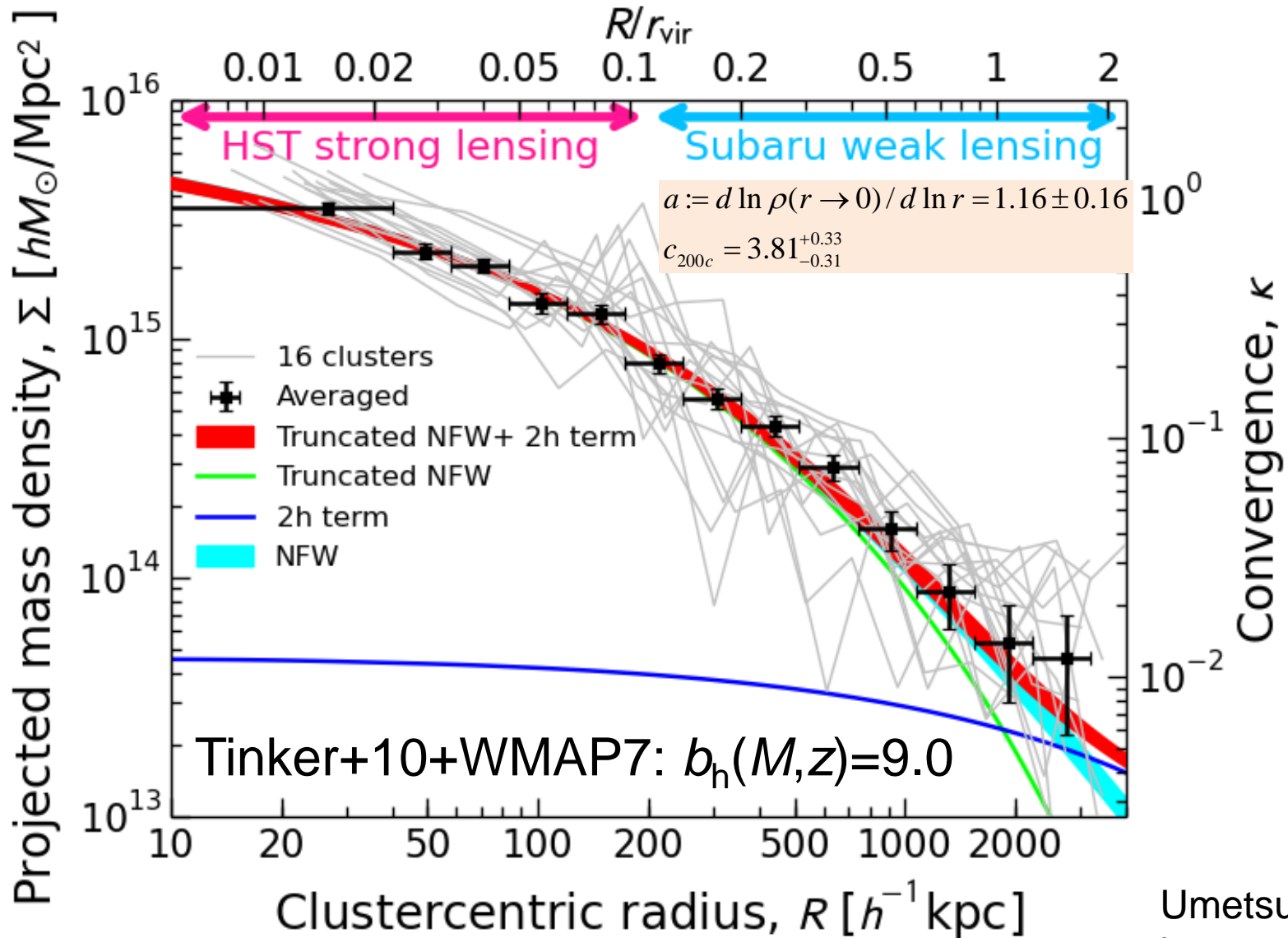
**2h term**

$$\Sigma_{\text{tot}}(R | M) = \Sigma_{1\text{h}}(R | M) + b_{\text{h}}(M) \Sigma_{\text{m}}(R)$$

2. Concentration-mass-redshift relation  $c_{200\text{c}}(M_{200\text{c}}, z)$

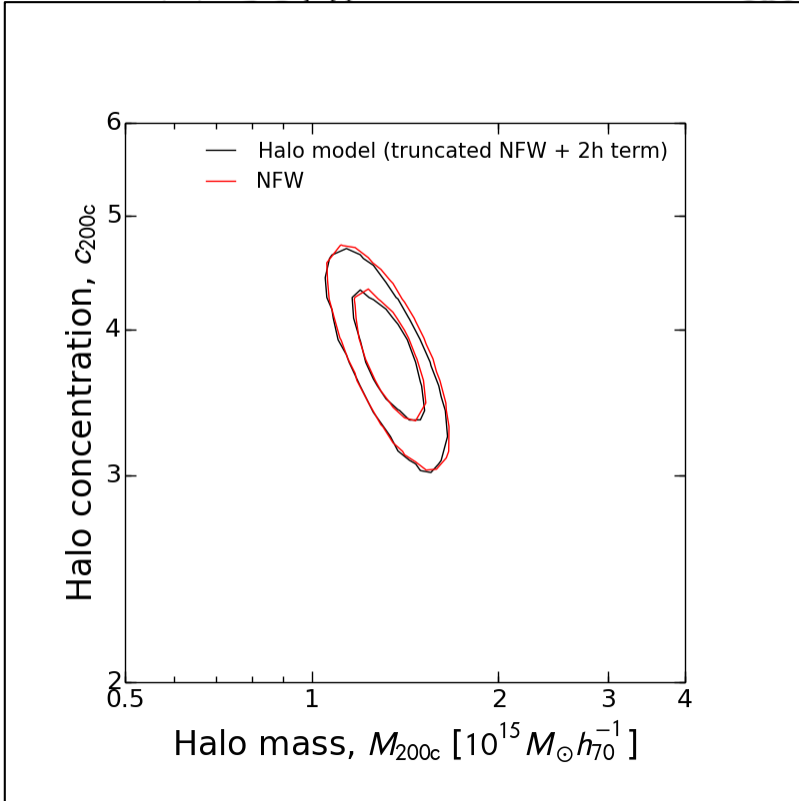
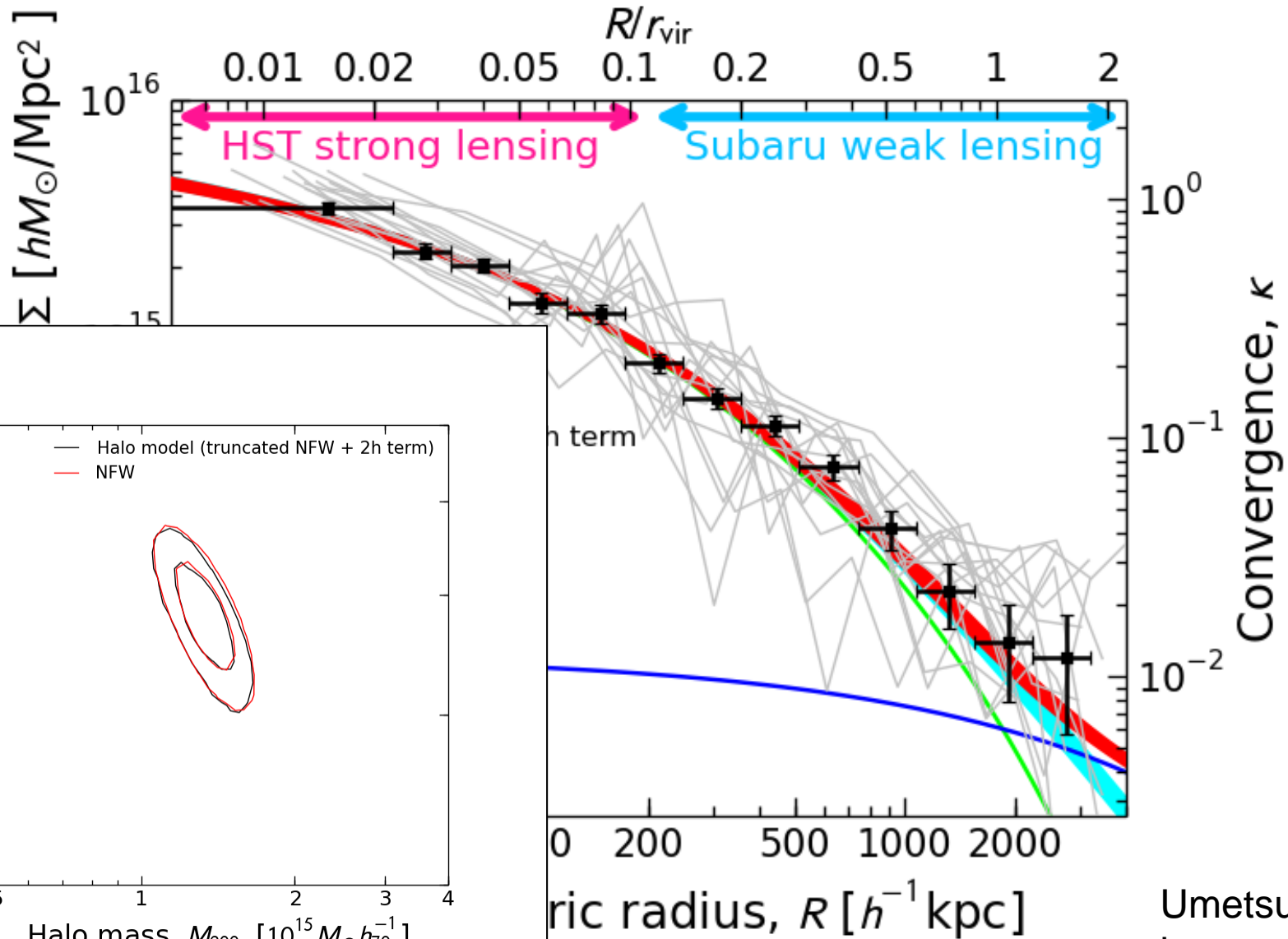


# Averaged Total Mass Profile





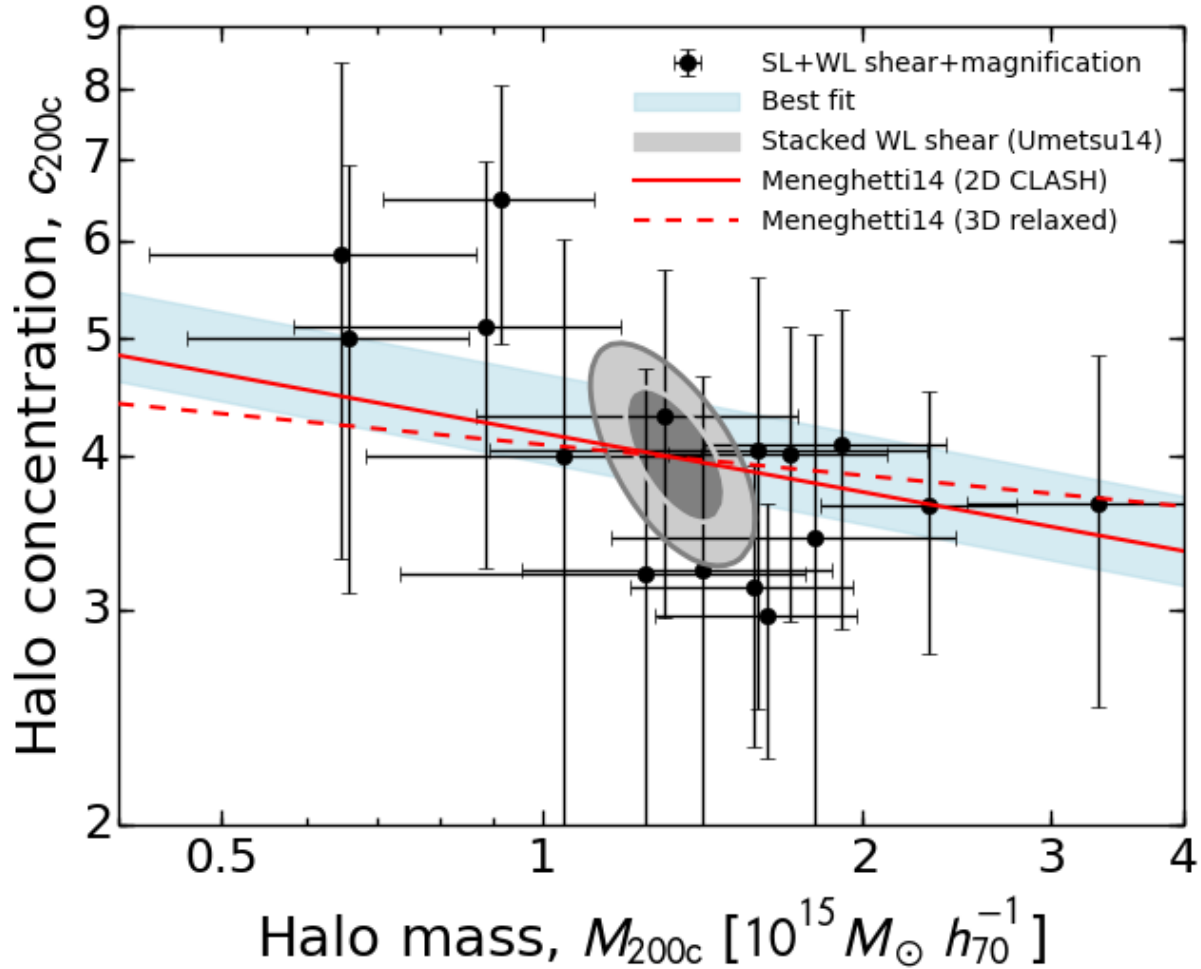
# Averaged Total Mass Profile



Umetsu+2015,  
in prep



# C-M relation



$$\partial \ln c / \partial \ln M = -0.16 \pm 0.08$$

$$c(9 \times 10^{14} M_{\text{sun}}, z = 0.35) = 4.10 \pm 0.35$$

$$\sigma_{\text{inc}} < 0.1$$

Umetsu+2015,  
in prep



# Summary

- Observed c-M relation is consistent with
  - theoretical expectation ( $\sigma_8=0.82$ ),  $\langle c_{200c} \rangle \sim 3.9$ , which accounts for CLASH selection function and projection effects
- Consistent shear-magnification measurements allow for accurate cluster mass profile measurements for 20 CLASH clusters with **+/-8% systematic mass-calibration uncertainty**.
- Averaged total matter distribution  $\langle \Sigma \rangle$  at  $R=[0.01,2]r_{\text{vir}}$  from full-lensing analysis (SL + shear + magnification) is consistent with LCDM halo-model with  $c_{200c}=4.0\pm 0.3$ ,  $M_{200c}=(1.3\pm 0.1)10^{15}M_{\text{sun}}$ ,  $b_h \sim 9$

# CLASH Products released

<http://archive.stsci.edu/prepds/clash/>

- Calibrated and co-added images [HST, Subaru]
- Object catalogs [HST, Subaru]

Subaru (S-Cam) product release will be completed by September 2014



# CLASH-WL Summary

- Ensemble-averaged halo structure  $\Delta\Sigma$  (1h) of X-ray-regular CLASH clusters is consistent with a family of standard (collisionless) DM predictions:
  - $M_{200c} = (1.3 \pm 0.1) 10^{15} M_{\text{sun}}, \langle z \rangle = 0.35$
  - NFW (PTE=0.66):  $c_{200c} = 4.01 (+0.35, -0.32)$
  - Einasto (PTE=0.51): degree of curvature,  $\alpha_E = 0.19 \pm 0.07$
- The stacked-mean concentration agrees with:
  - theoretical expectation,  $\langle c_{200c} \rangle \sim 3.9$ , which takes into account CLASH selection function and projection effects (Meneghetti+14)
  - measured effective Einstein radius,  $\langle \theta_{\text{Ein}} \rangle = 20''$  ( $z_s = 2$ ), from independent HST-SL analysis (Zitrin+CLASH 14, in prep)





# CLASH-WL Summary (contd.)

- Consistent geometric shear vs. magnification measurements allow for accurate cluster mass profile measurements for 20 CLASH clusters with  $\pm 8\%$  systematic mass-calibration uncertainty.
- Total matter distribution  $\Sigma$  (1h+2h) recovered from full-lensing analysis (SL + shear + magnification) is consistent with shear-based halo model predictions ( $b_h = 9 \pm 2$  at  $M_{200} = 1.3e15 M_{\text{sun}}$ ,  $z = 0.35$ ), establishing further consistency in the context of LCDM.

# Supplemental Slides

# Latest simulation vs. CLASH

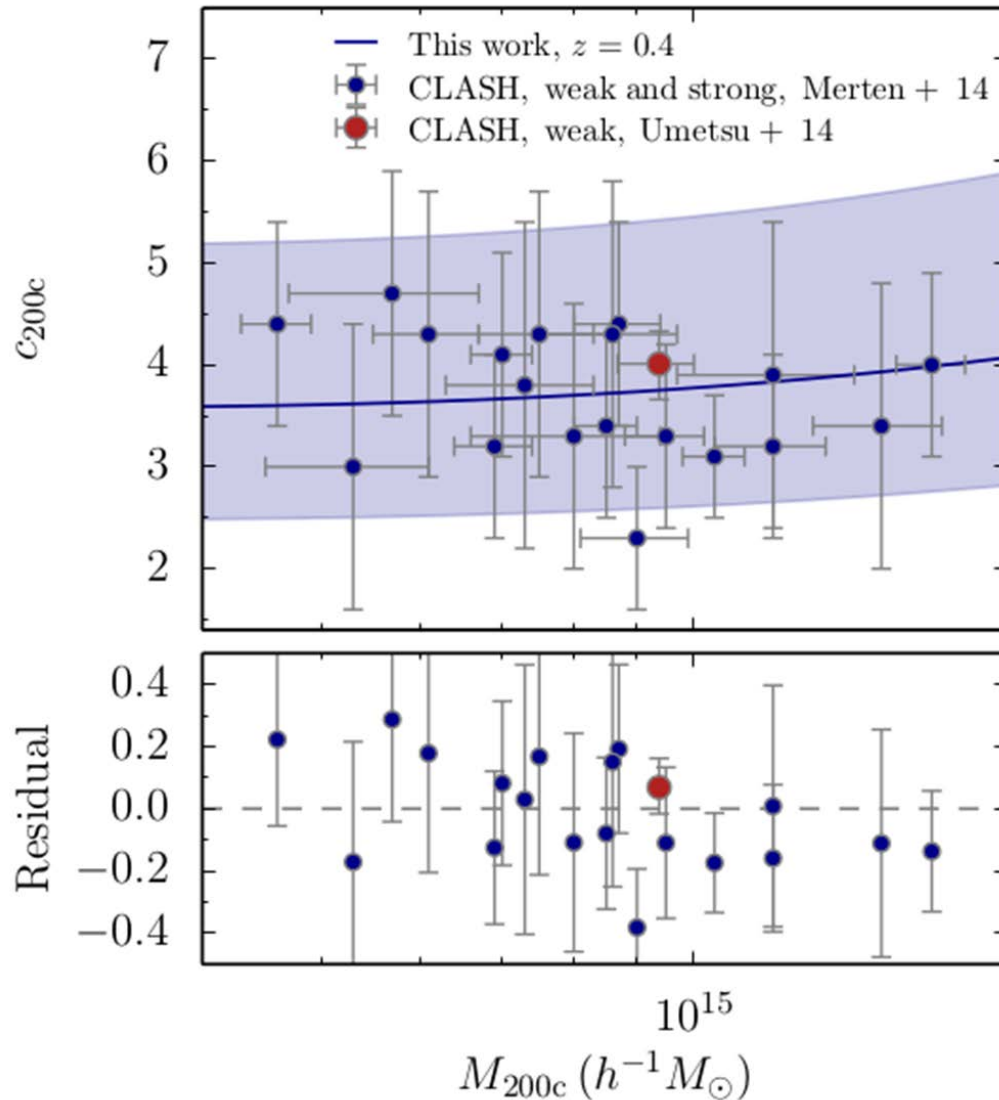
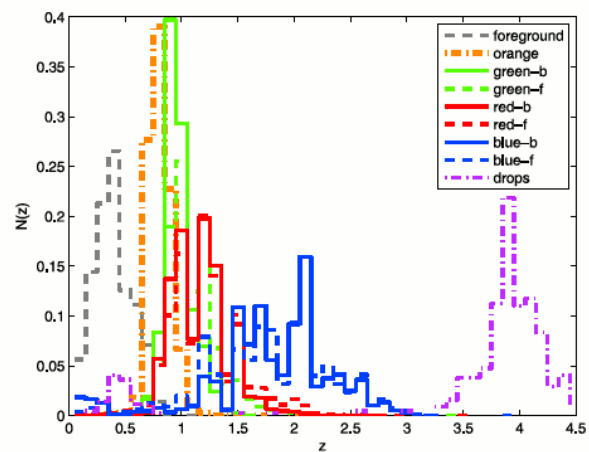
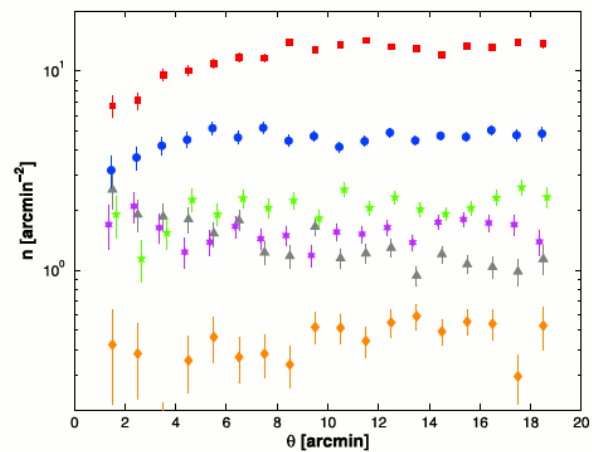
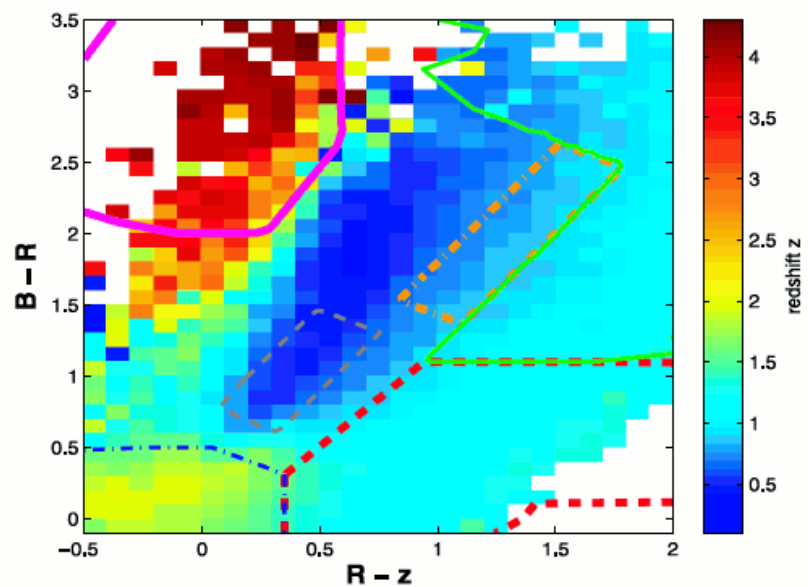
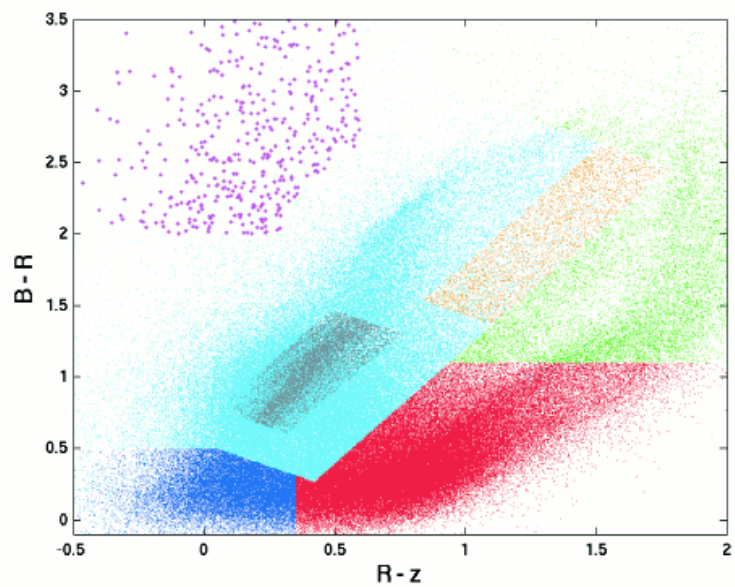
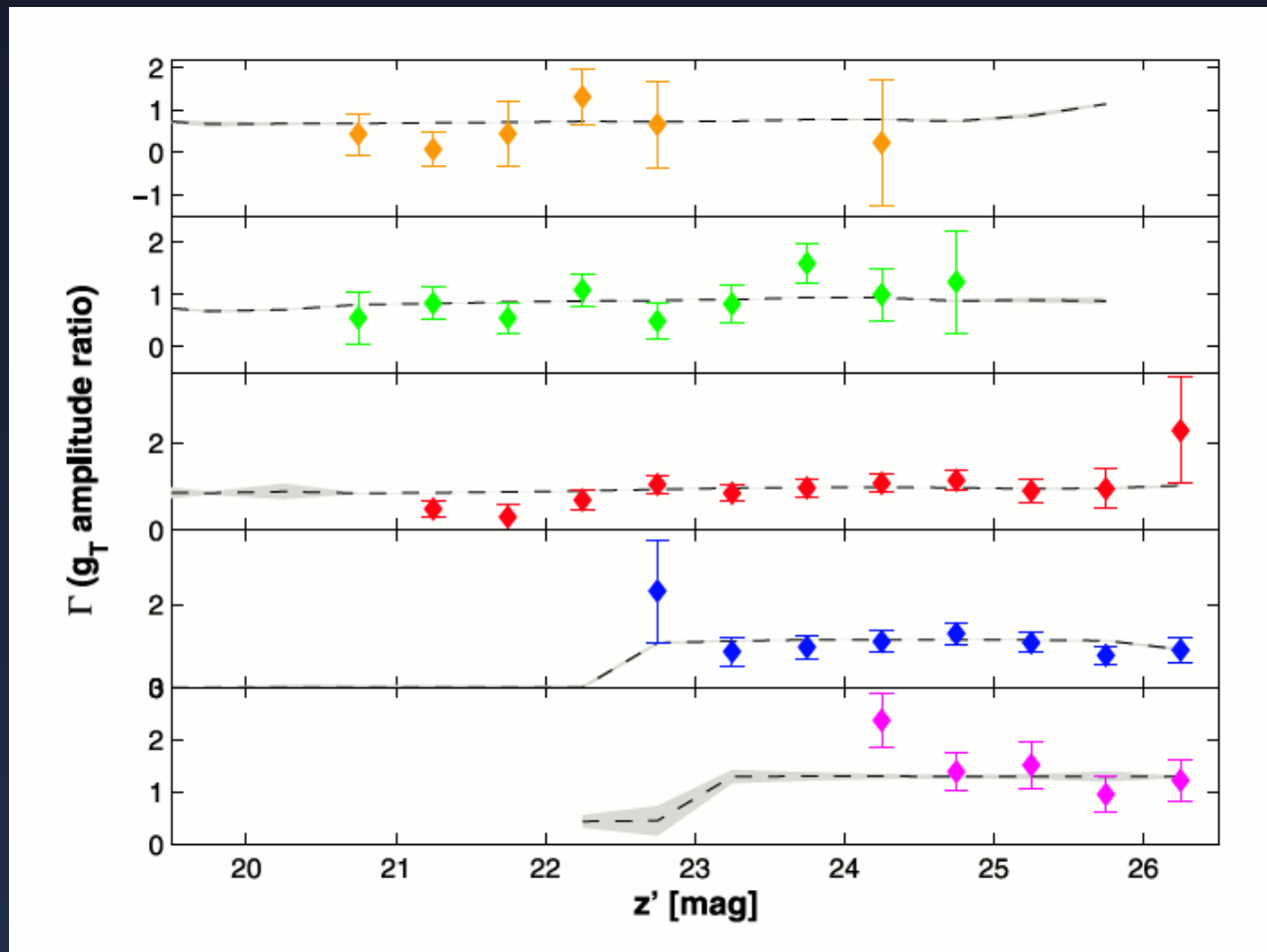


Figure from Diemer & Kravtsov 2014b



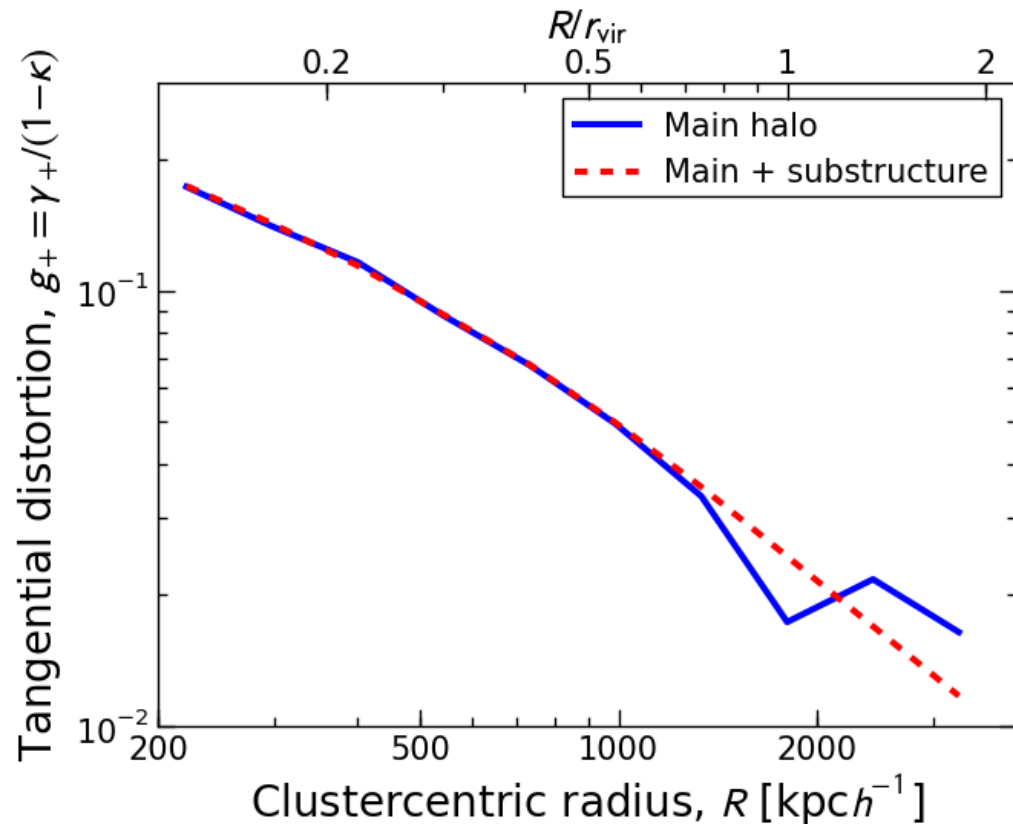
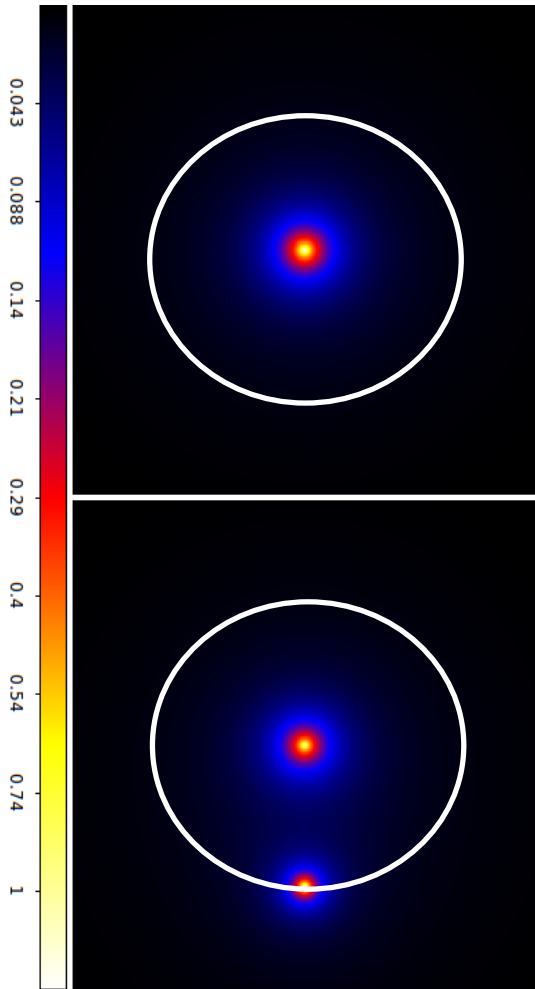


# SUBARU shear strength as a function of magnitude



# Non-local substructure effect

A substructure at  $R \sim r_{\text{vir}}$  of the main halo, modulating  $\Delta\Sigma(R) = \Sigma(< R) - \Sigma(R)$



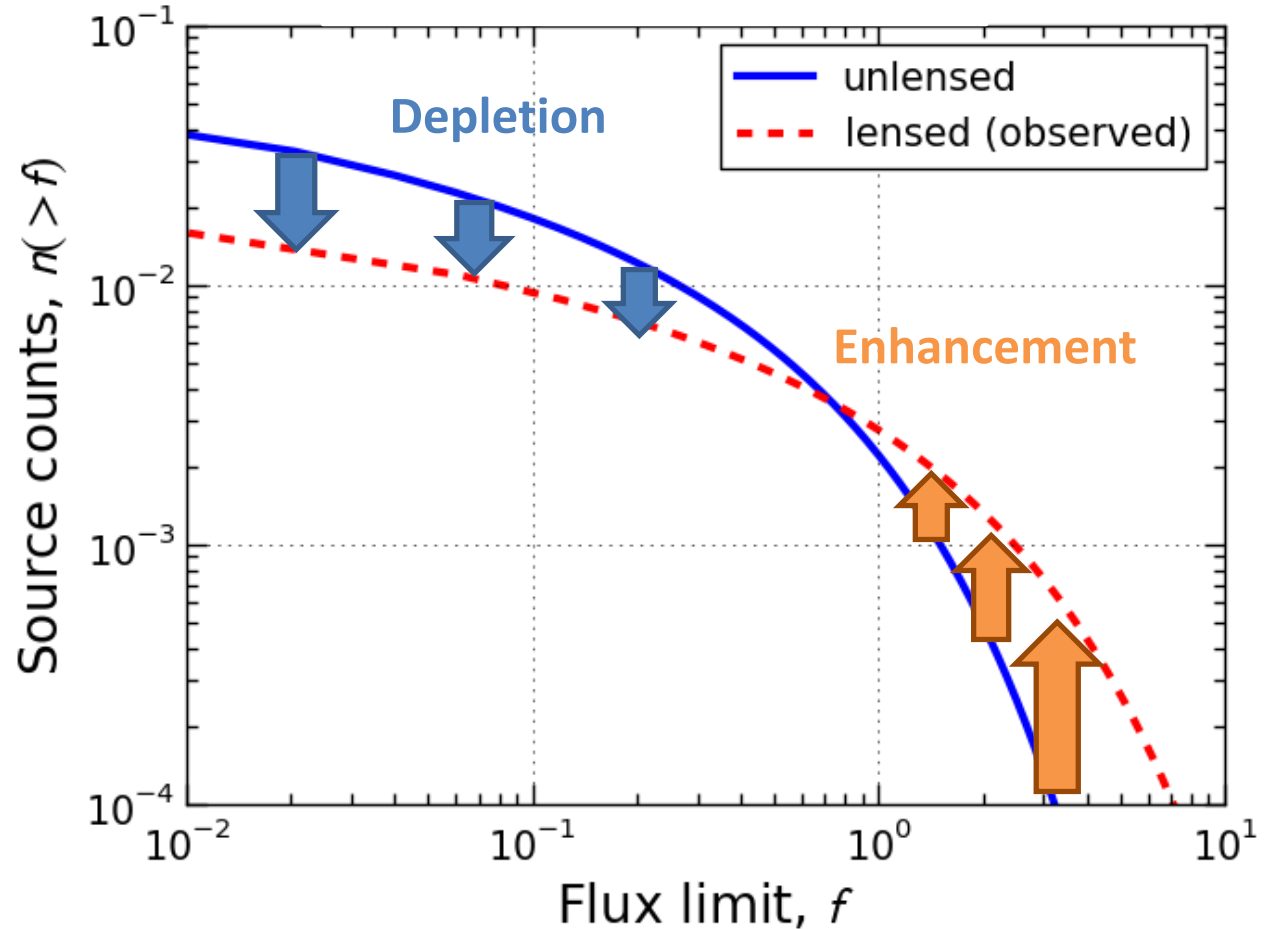
Known  $\sim 10\%$  negative bias in mass estimates from tangential-shear fitting, inherent to clusters sitting in substructured field (Rasia+12)

# Magnification bias effects

Flux-limited  
source counts:

$$n_{\text{obs}}(> f) = \mu^{-1} n(> \mu^{-1} f)$$

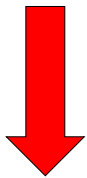
Broadhurst, Taylor &  
Peacock 95



Flux amplification

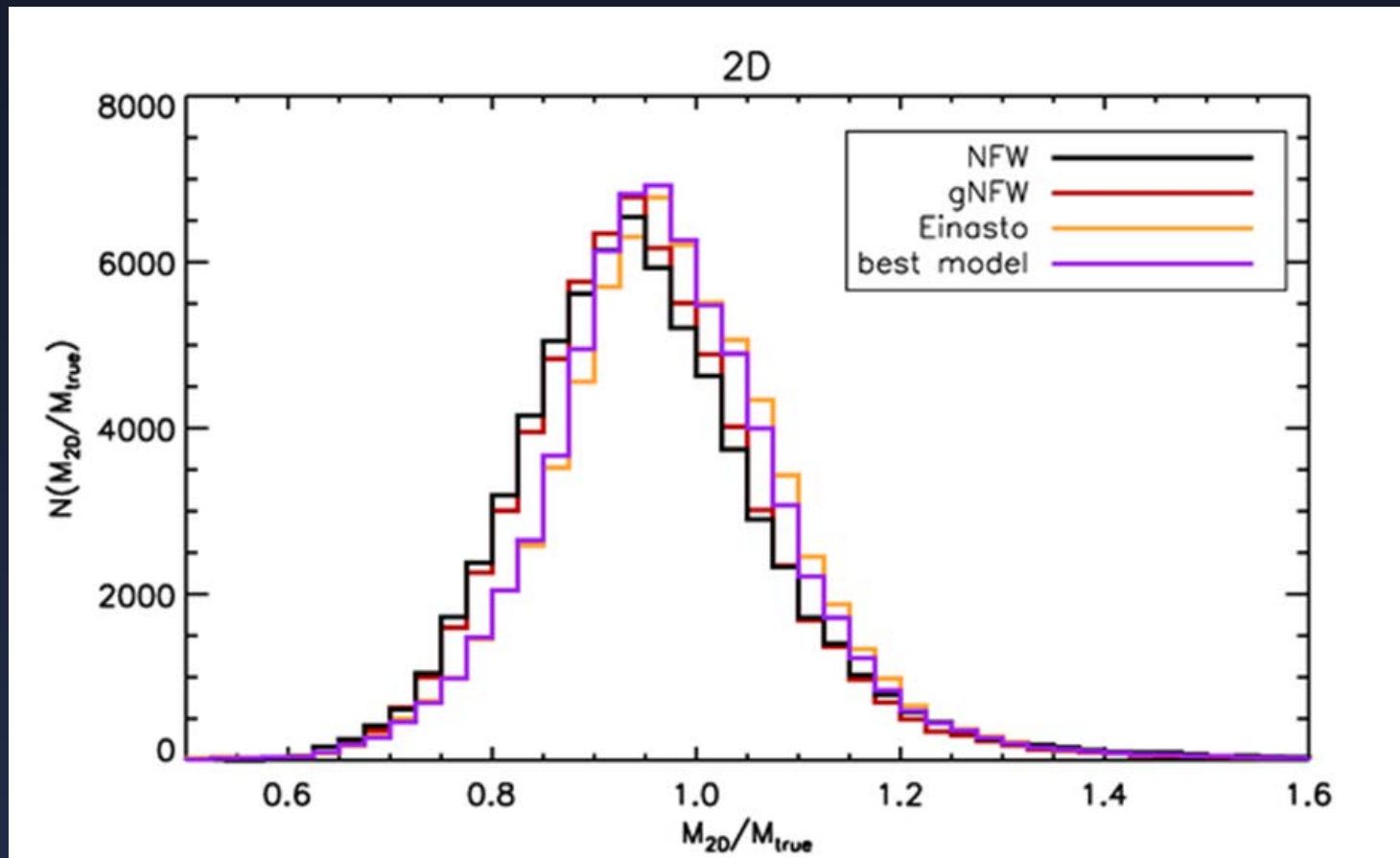


Geometric area  
distortion



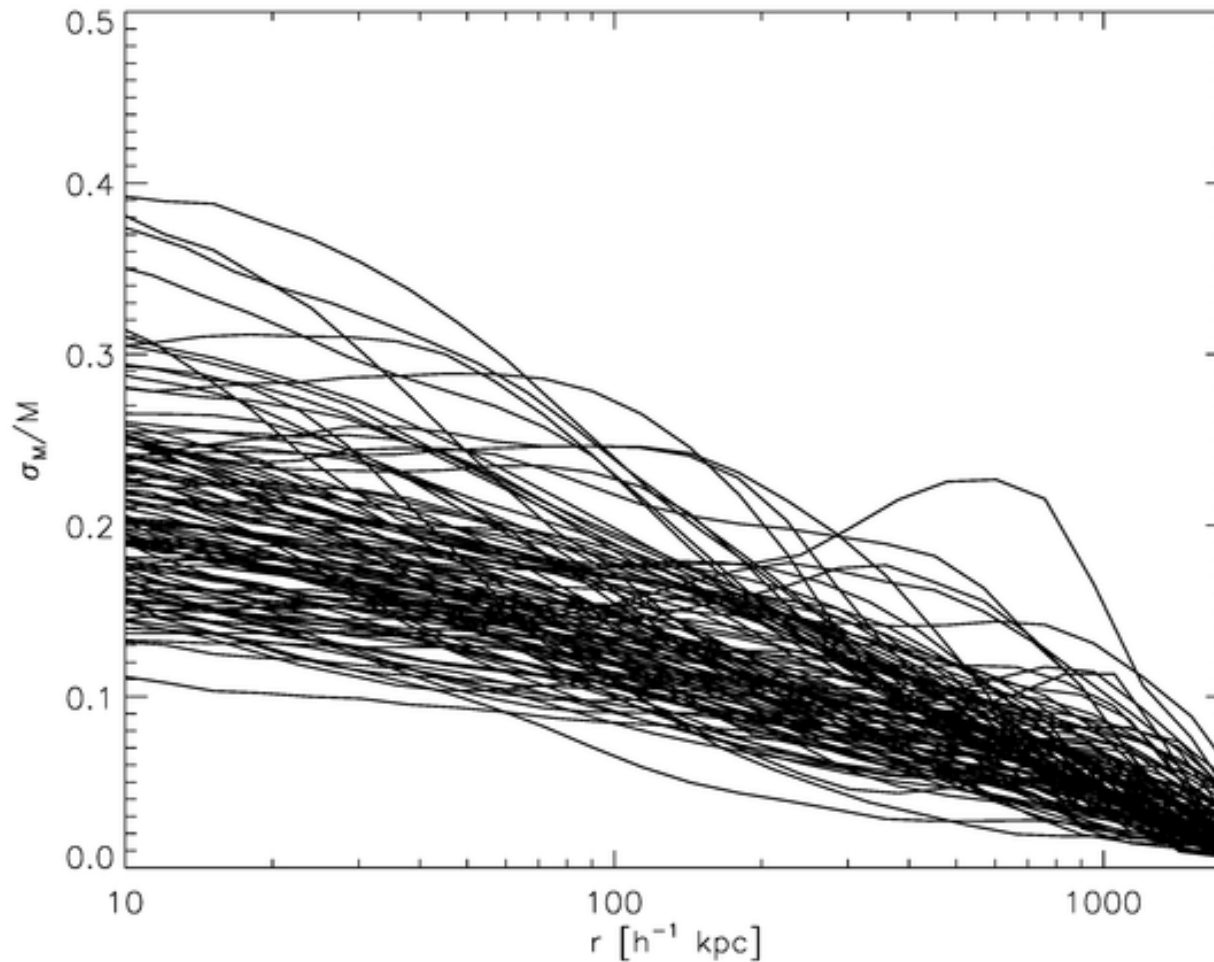
$n/\mu$

# Cluster masses recovered from lensing analysis





# Scatter in $M_{2D}(R)$ by halo triaxiality

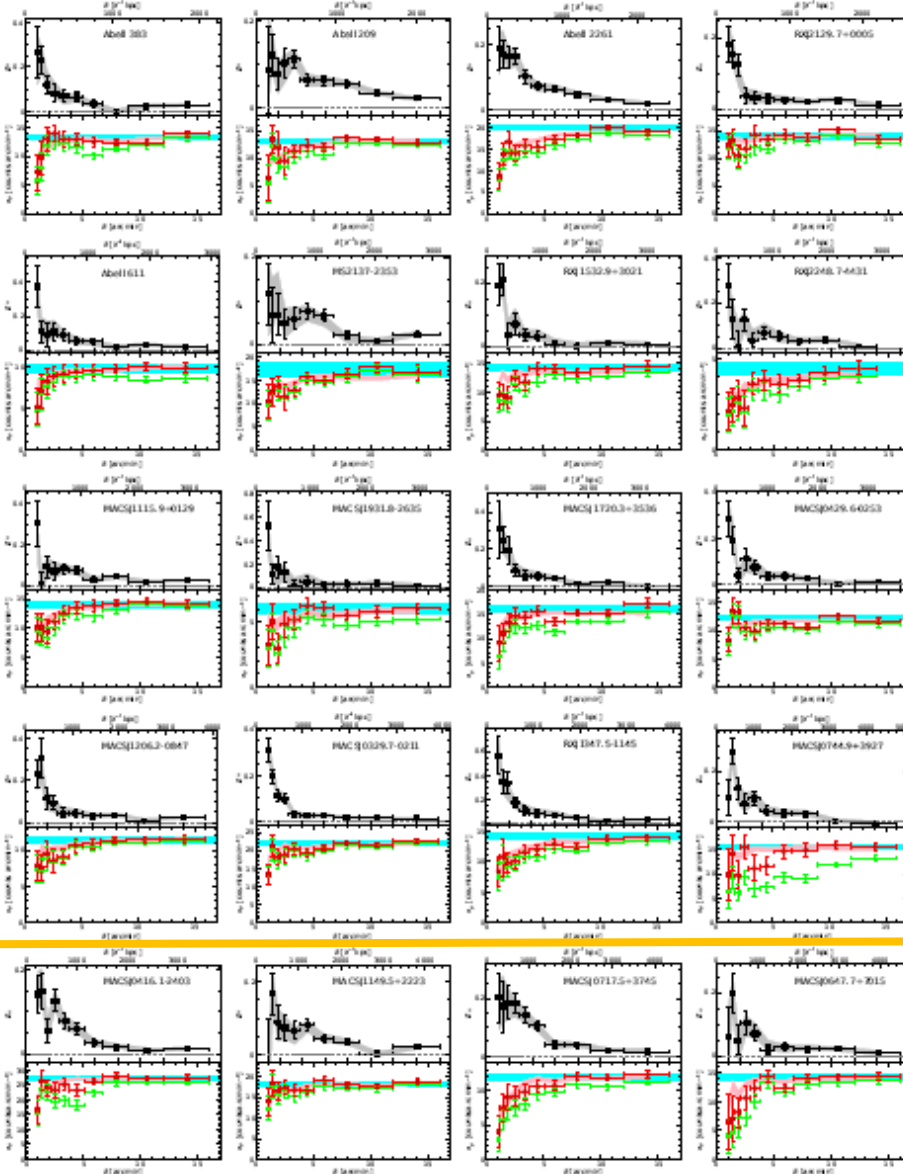


MUSIC-2 simulation by Massimo





# 20 CLASH clusters in Umetsu+14



## 16 X-ray-selected clusters

- 15 clusters from 8.3m Subaru Telescope
- 1 southernmost cluster (RXJ2248) from 2.2m ESO/MPG
- $0.18 < z < 0.69$

**$\langle \chi^2/\text{dof} \rangle = 0.92$  for 20 CLASH clusters**

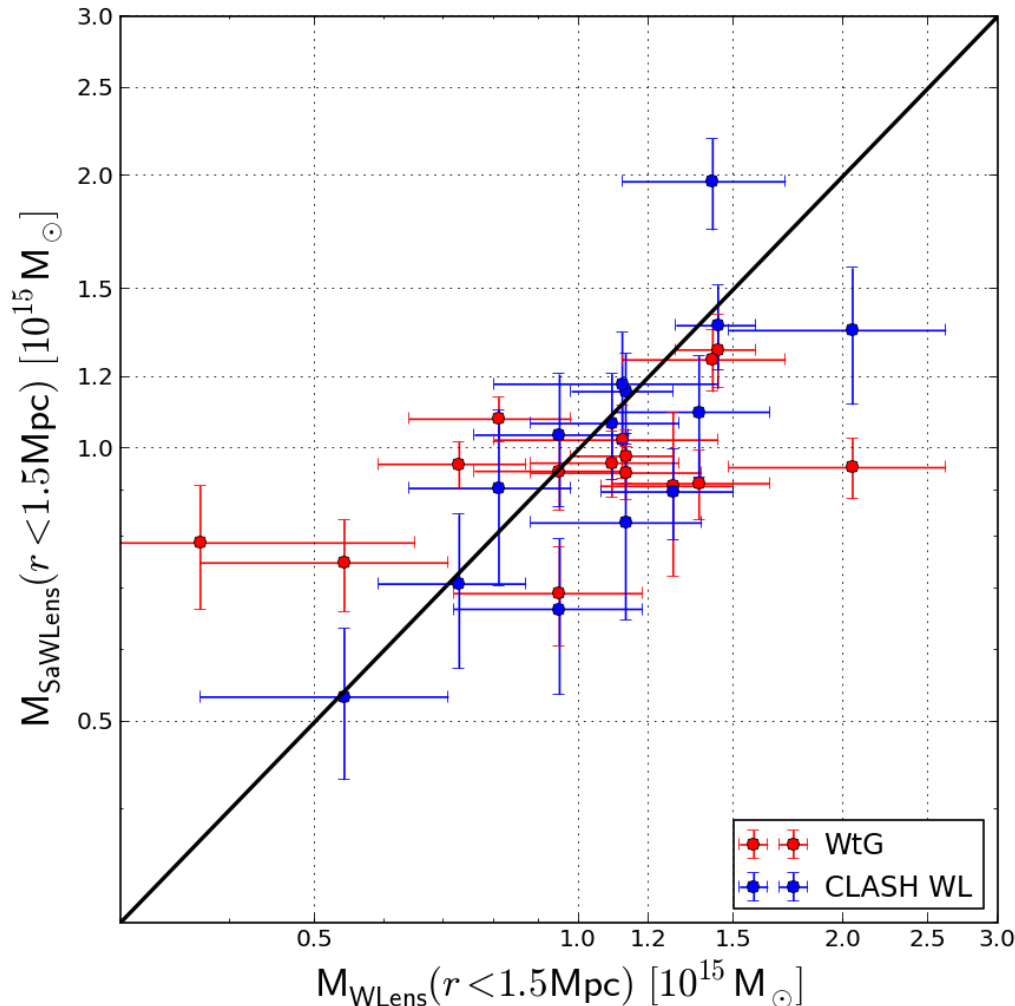
## 4 high-magnification clusters

- All 4 clusters from 8.3m Subaru Telescope



# Mass Comparisons @ R=1.5Mpc

Merten+CLASH 14



**Un-weighted geometric mean mass ratios ( $\langle Y/X \rangle = 1/\langle X/Y \rangle$ )**

- $\langle \text{SaWLens} / \text{WL} \rangle = 0.96$
- $\langle \text{WL} / \text{WtG} \rangle = 0.91$
- $\langle \text{SaWLens} / \text{WtG} \rangle = 0.88$

**WL (Umetsu+14)**

→ shear+mag (Subaru)

**SaWLens (Merten+14)**

→ SL + shear (HST+Subaru)

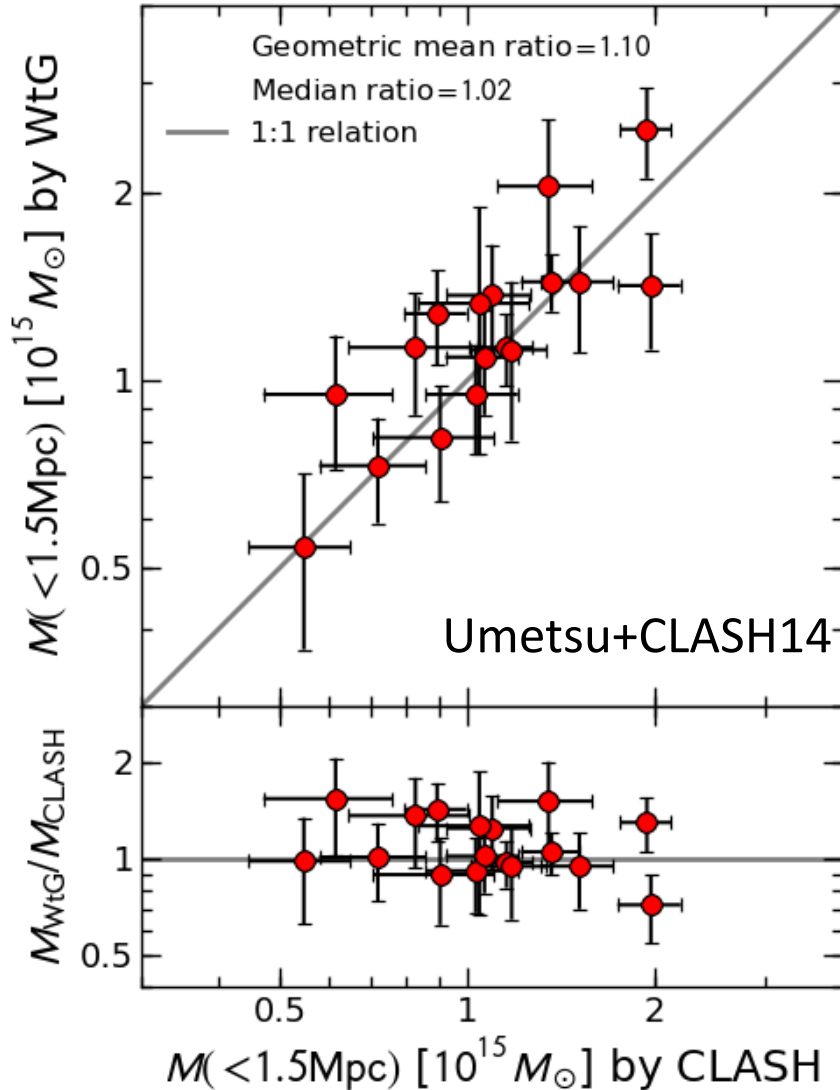
**WtG (Applegate+14)**

→ shear (Subaru)

Note: WL mass calibration uncertainty of 8 percent



# Comparison with WtG @R=1.5Mpc



17 clusters in common (Subaru):

- **WtG**: shear-only (Applegate+14), NFW  $c_{200c}=4$  prior
- **CLASH**: shear + magnification, NFW log-uniform:  $0.1 < c_{200c} < 10$

**Un-weighted geometric mean mass ratio ( $\langle Y/X \rangle = 1/\langle X/Y \rangle$ )**

- $\langle M_{\text{WtG}}/M_{\text{CLASH}} \rangle = 1.10$
- Median ratio = 1.02

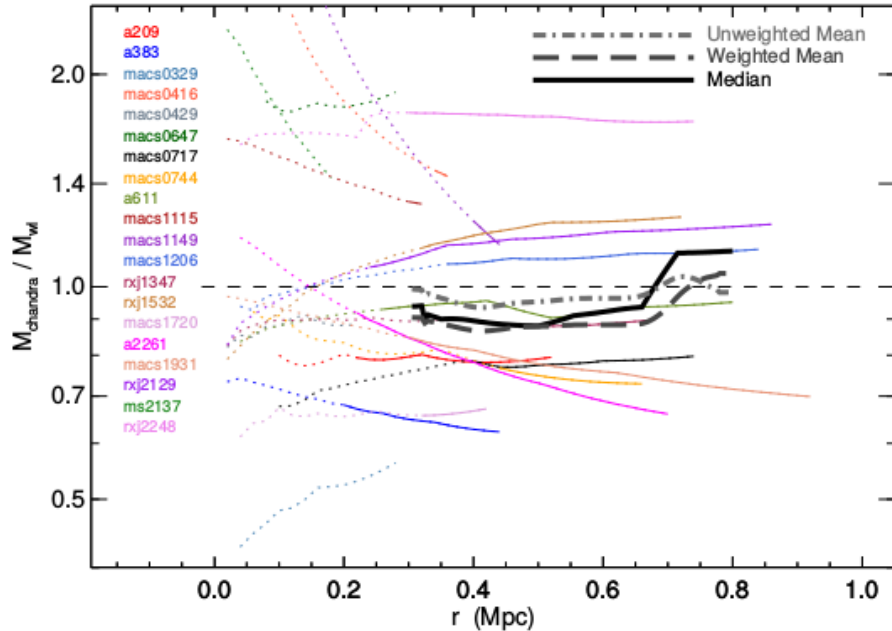
Systematic uncertainty in the overall mass calibration of 8% from shear-magnification consistency (Umetsu+14)

No mass dependent bias

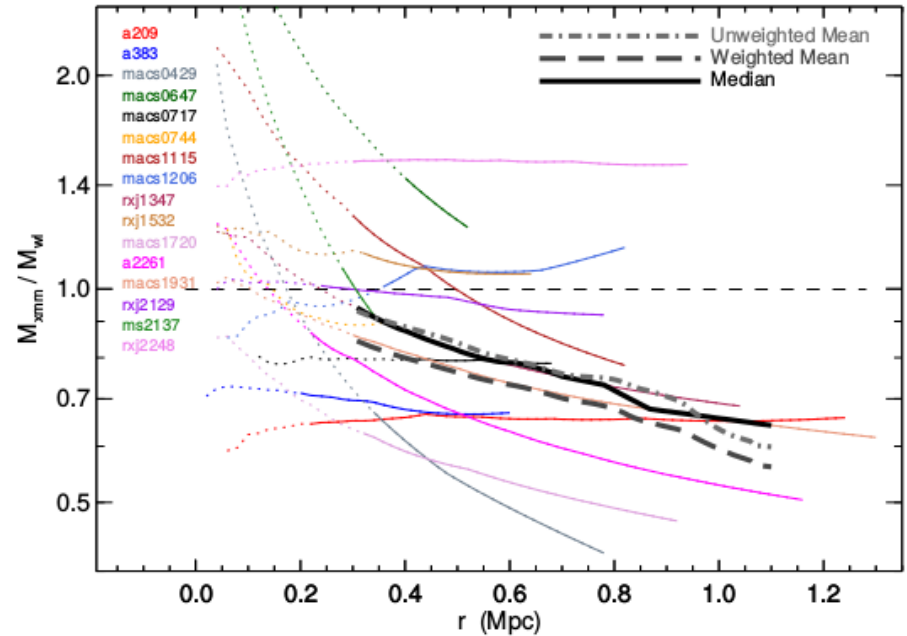


# CLASH Comparisons with X-ray masses

## Chandra HSE / Subaru-WL



## XMM HSE / Subaru-WL



### X-ray to WL comparison at R=0.5Mpc

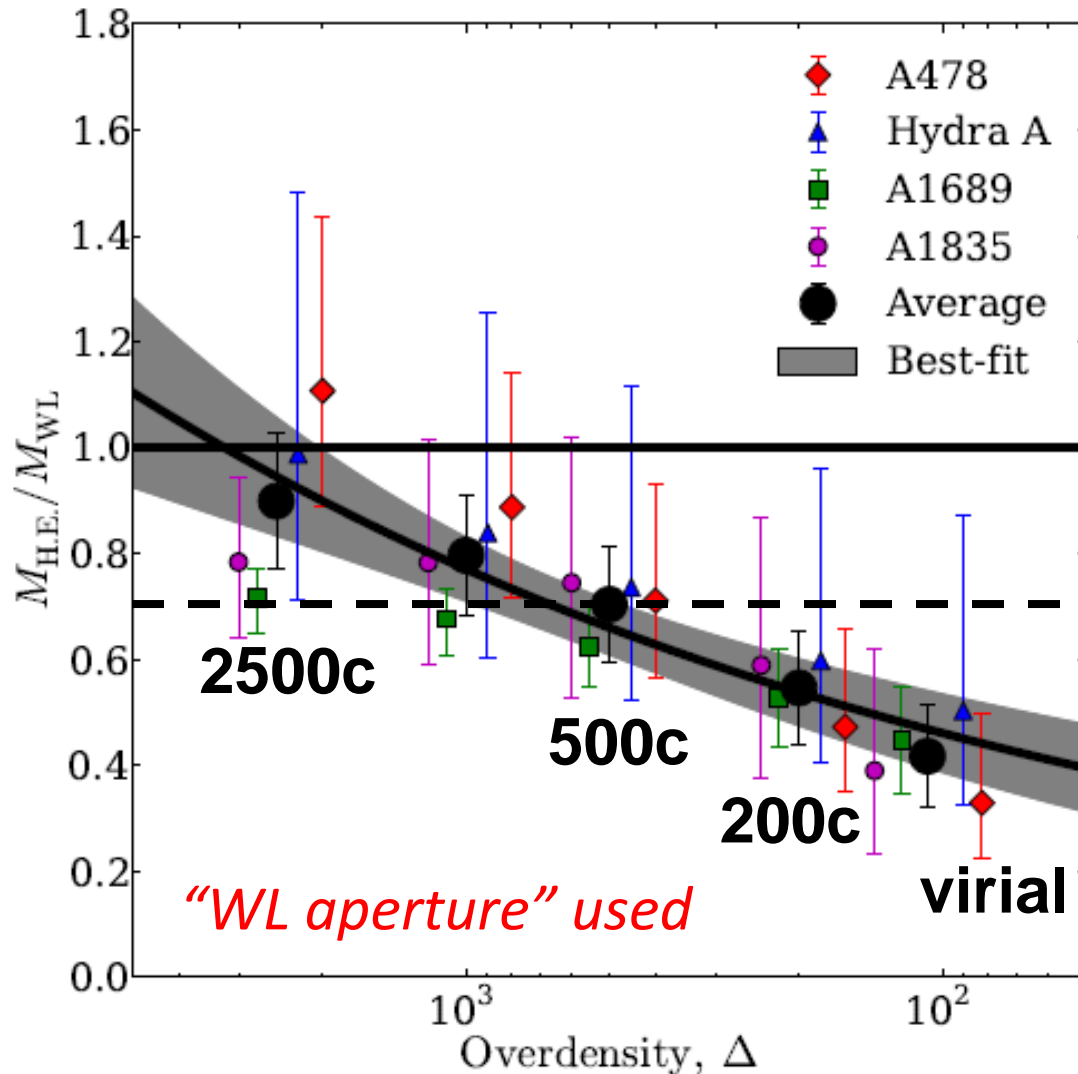
- $b = 1 - \langle M_{\text{Chandra}} / M_{\text{WL}} \rangle = 0.05 \pm 0.07$  (11 clusters)
- $b = 1 - \langle M_{\text{XMM}} / M_{\text{WL}} \rangle = 0.16 \pm 0.06$  (14 clusters)

### X-ray to WL comparison at $r_{500}$ [no aperture correction]

- $b = 1 - \langle M_{\text{Chandra}} / M_{\text{WL}} \rangle = 0.09 \pm 0.12$  (20 clusters)
- $b = 1 - \langle M_{\text{XMM}} / M_{\text{WL}} \rangle = 0.41 \pm 0.07$  (16 clusters)

Donahue+CLASH  
14, ApJ, accepted  
(arXiv:1405.7876)  
See also Sereno+14

# Suzaku-X HSE vs. Subaru WL



Independent *Suzaku*-HSE vs. Subaru-WL results, consistent with XMM-HSE vs. Subaru-WL of CLASH collaboration

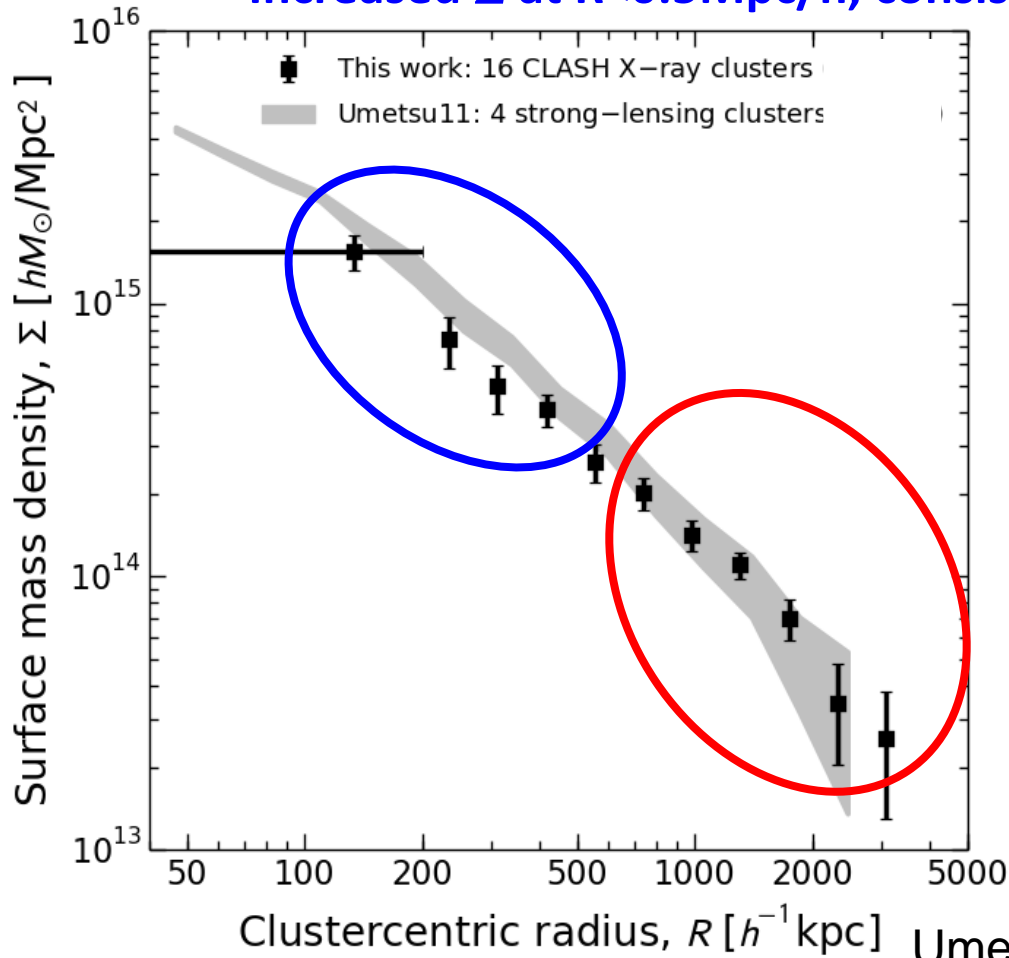
Okabe, Umetsu et al.14, PASJ, in press (arXiv:1406.3451)





# Comparison with pre-CLASH results

- $C_{200}$  vs  $\theta_E$  relation, consistent with triaxial CDM halos (Oguri+12)
- **Similar  $v$  (MAH), similar  $\Sigma$  in outskirts (Diemer & Kravtsov 14)**
- **Increased  $\Sigma$  at  $R < 0.5 \text{ Mpc}/h$ , consistent w orientation bias (Gao+12)**



## CLASH X-ray-selected sample

- $M_{200} = 1.3e15 M_{\text{sun}}$
- $\underline{C_{200} = 4.0}$
- $\underline{\theta_E \sim 15'' (z_s=2)}$
- $\underline{v=3.8 (b_h \sim 9)}$

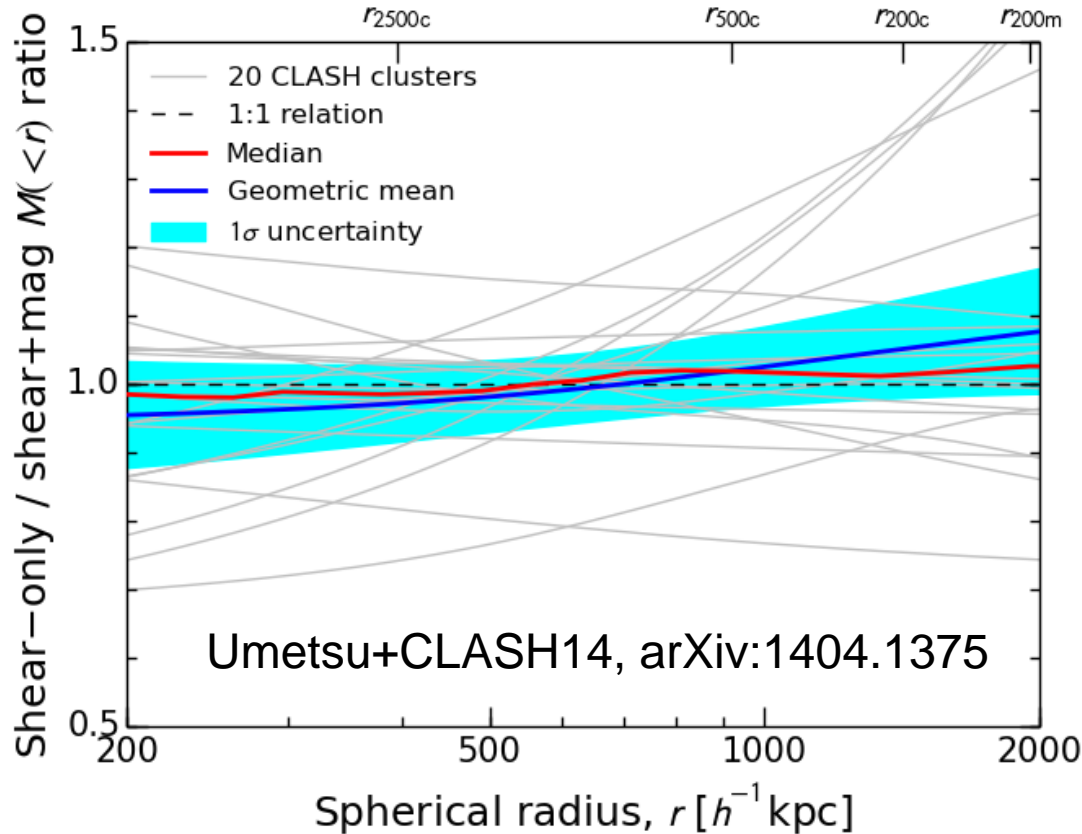
## Umetsu11b sample

- $M_{200} = 1.7e15 M_{\text{sun}}$
- $\underline{C_{200} = 6.1}$
- $\underline{\theta_E \sim 36'' (z_s=2)}$
- $\underline{v=4.1 (b_h \sim 11)}$



# Shear-Magnification Consistency

$M(<r)$  de-projected assuming spherical NFW (20 CLASH clusters)



Umetsu et al. 14,  
ApJ, accepted  
(arXiv:1404.1375)

Internal systematic uncertainty in the overall mass calibration,  
empirically derived to be about +/- 8%

# Ensemble-averaged DM halo profile

Stacking of weak-lensing signals by weighting individual clusters according to the sensitivity kernel matrix:

$$\langle\langle \widehat{\Delta\Sigma}_+ \rangle\rangle = \left( \sum_n \mathcal{W}_{+n} \right)^{-1} \left( \sum_n \mathcal{W}_{+n} \widehat{\Delta\Sigma}_{+n} \right),$$

with the individual sensitivity matrix

$$(\mathcal{W}_{+n})_{ij} \equiv \Sigma_{c,n}^{-2} (C_{+n}^{-1})_{ij}$$

defined with the total covariance matrix

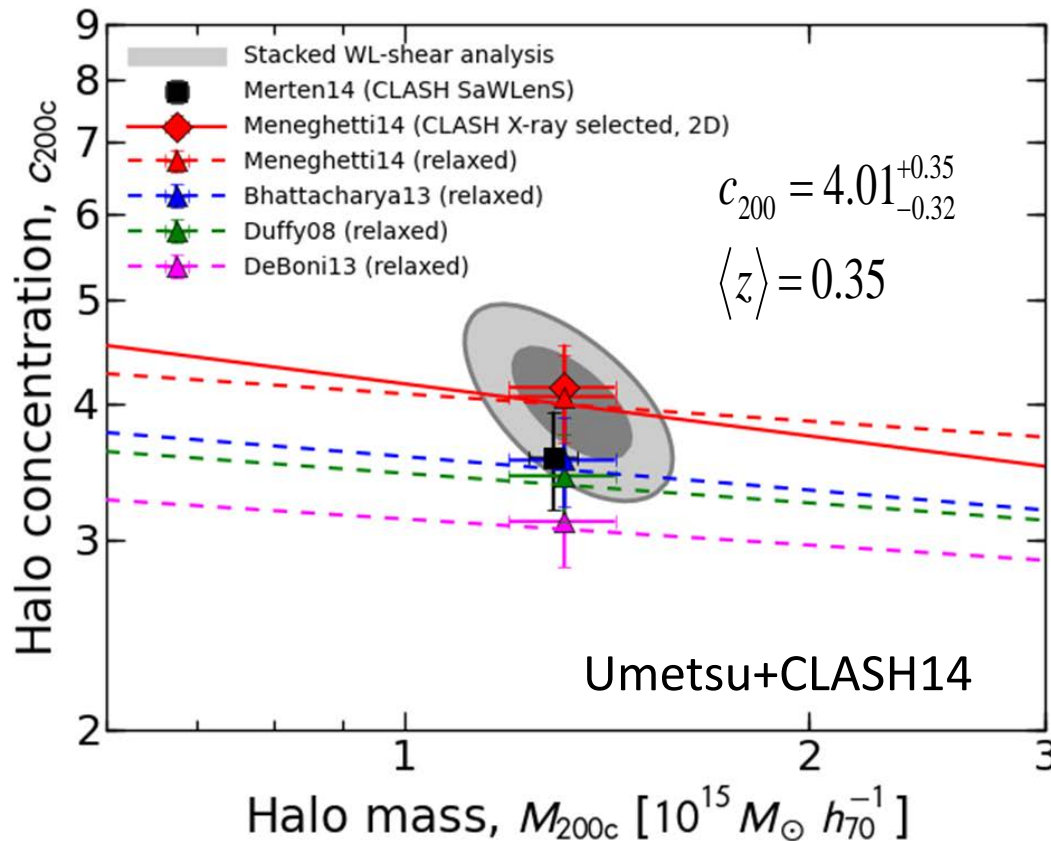
$$C_+ = C_+^{\text{stat}} + C_+^{\text{sys}} + C_+^{\text{lss}}.$$

**With “trace-approximation”, averaging is interpreted as**

$$\langle\langle \Sigma_c^{-1} \rangle\rangle = \frac{\sum_n \text{tr}(\mathcal{W}_{+n}) \Sigma_{c,n}^{-1}}{\sum_n \text{tr}(\mathcal{W}_{+n})},$$



# CLASH-WL vs. c-M relations



M14 (MUSIC-2):  $\sigma_8=0.82$

Bhat13:  $\sigma_8=0.8$

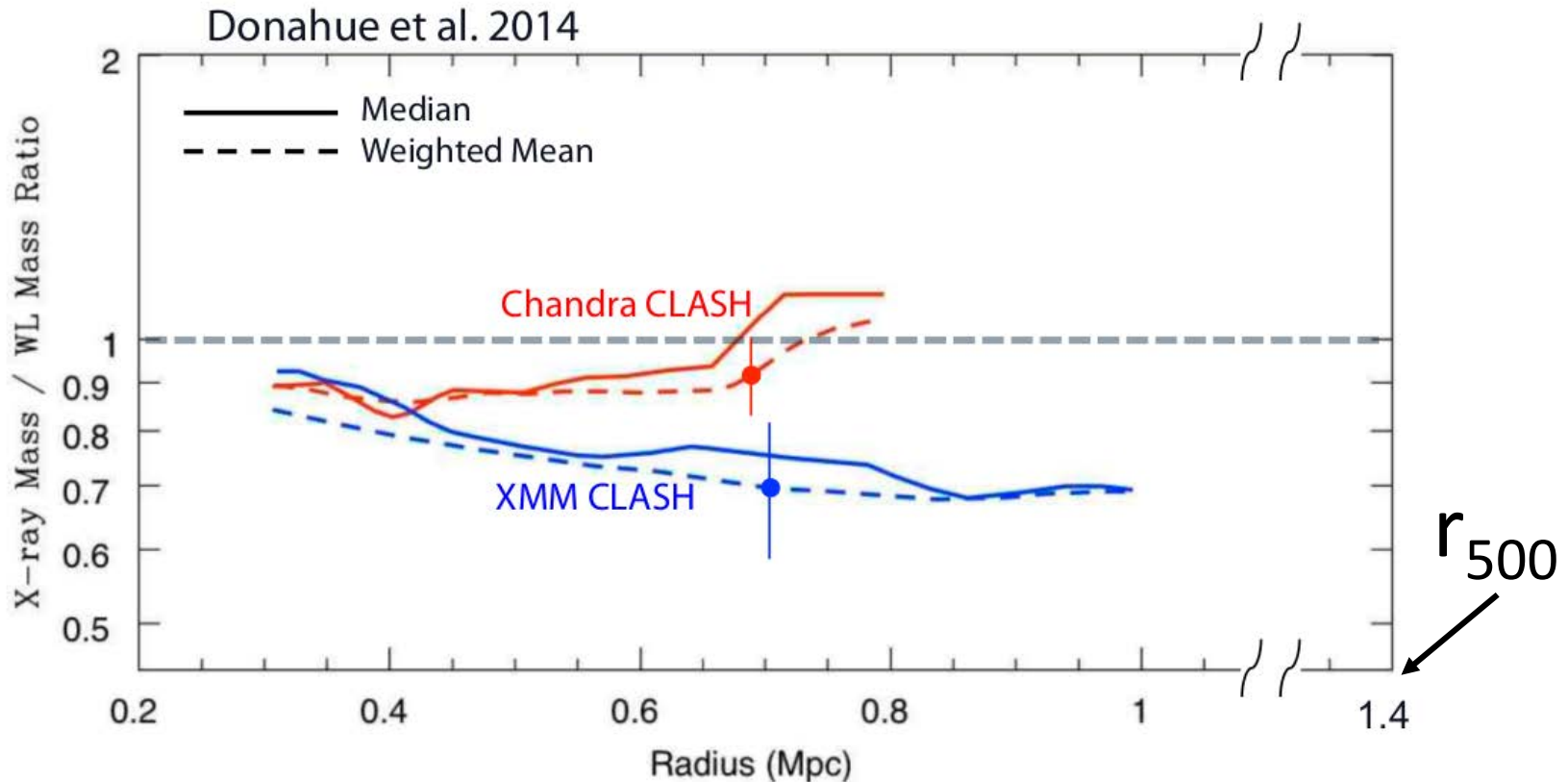
Duffy08:  $\sigma_8=0.8$

DeBoni13:  $\sigma_8=0.78$

At low  $M_{200c}$ , X-ray selection picks up clusters with higher concentrations (Meneghetti+14)



# CLASH: WL vs. X-ray Mass Comparison



## X-ray to WL mass comparison at $r_{500}$

- $b = 1 - \langle M_{\text{Chandra}} / M_{\text{WL}} \rangle = 0.22 \pm 0.10$
- $b = 1 - \langle M_{\text{XMM}} / M_{\text{WL}} \rangle = 0.44 \pm 0.06$

Donahue+CLASH  
2014, *ApJ*, 794, 136