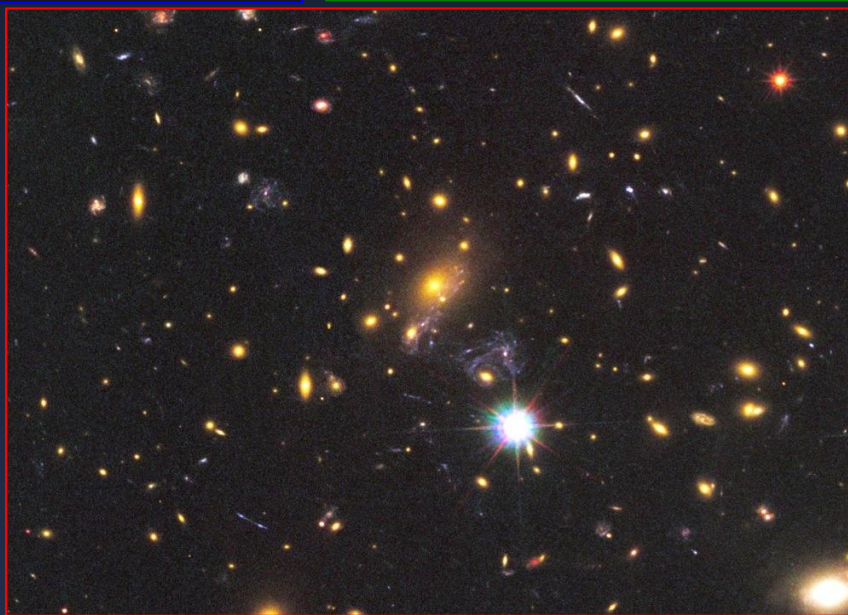
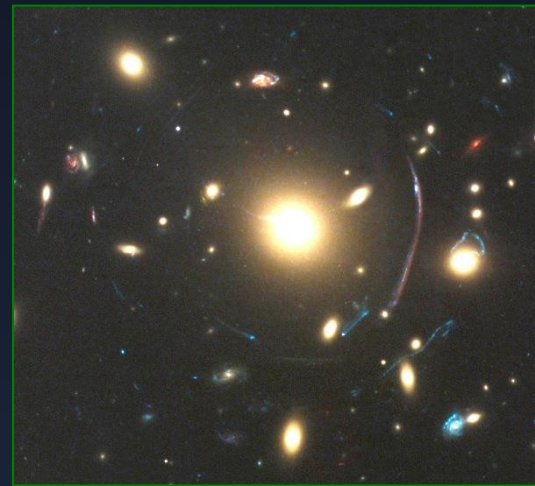
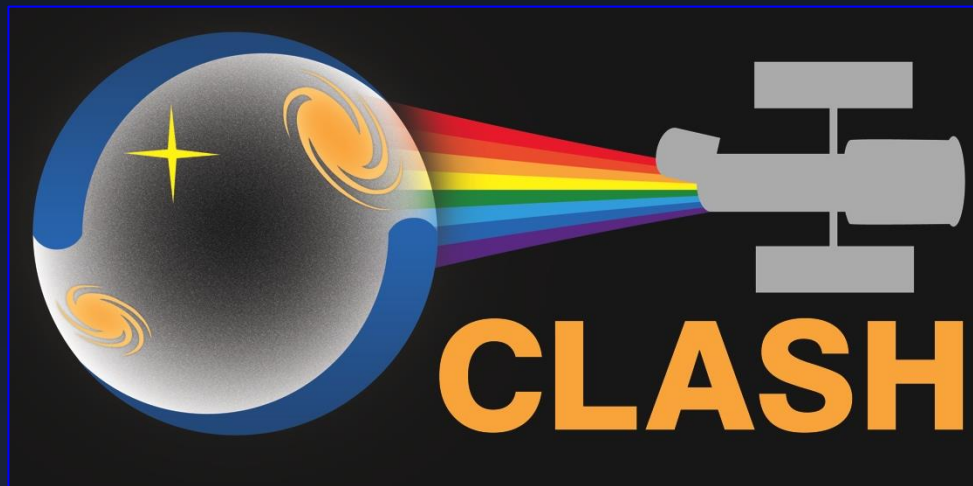


Mass Distribution in and around Galaxy Clusters from Gravitational Lensing:

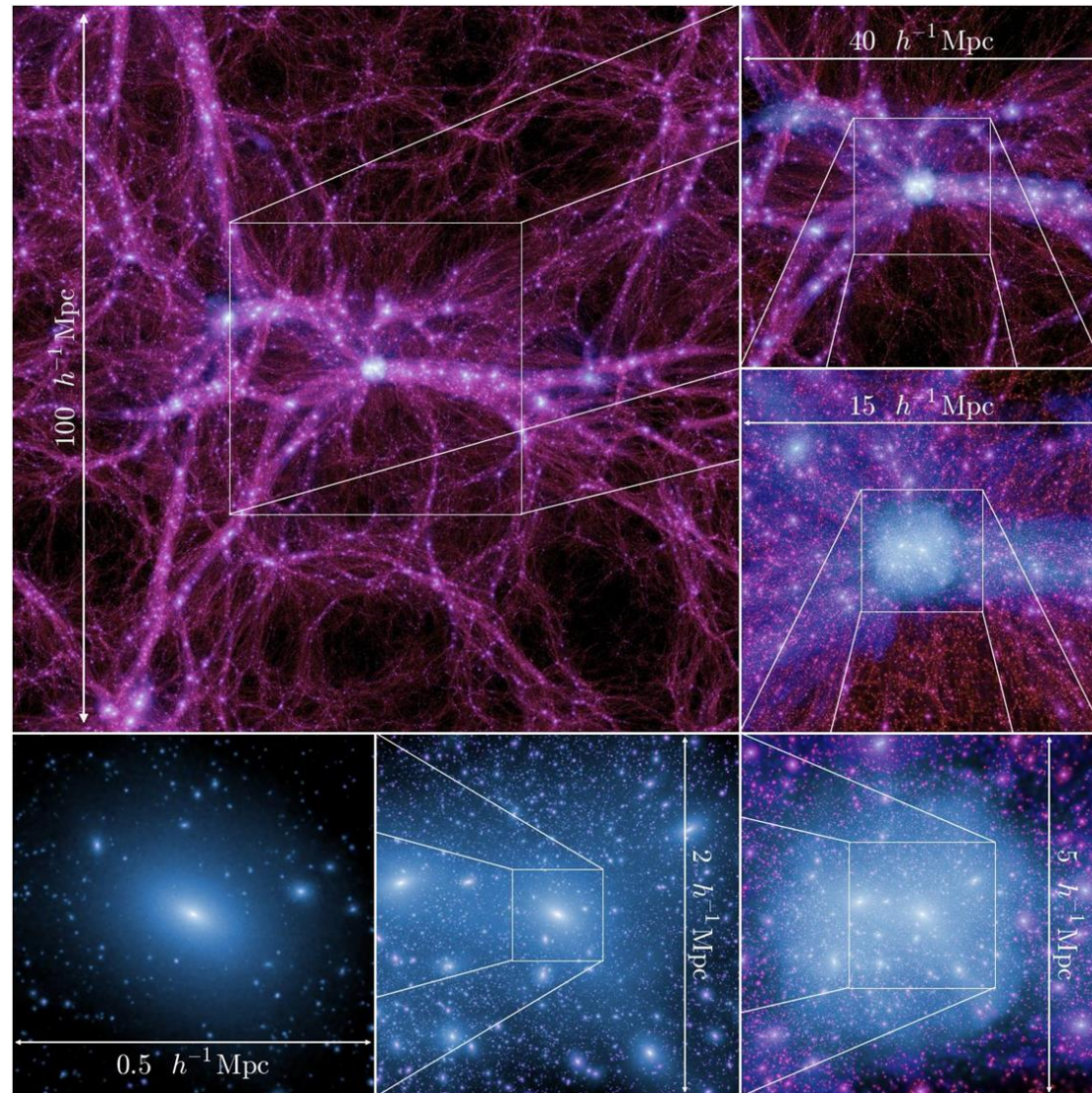
Cluster Lensing And Supernova survey with Hubble



Keiichi Umetsu (ASIAA, Taiwan) with the CLASH team

Galaxy Clusters as Cosmological Probes

Boylan-Kolchin+09



Surrounding LSS (2h)

- ✓ Halo bias $b(M,z)$
- ✓ Primordial matter $P(k)$

Halo structure (1h)

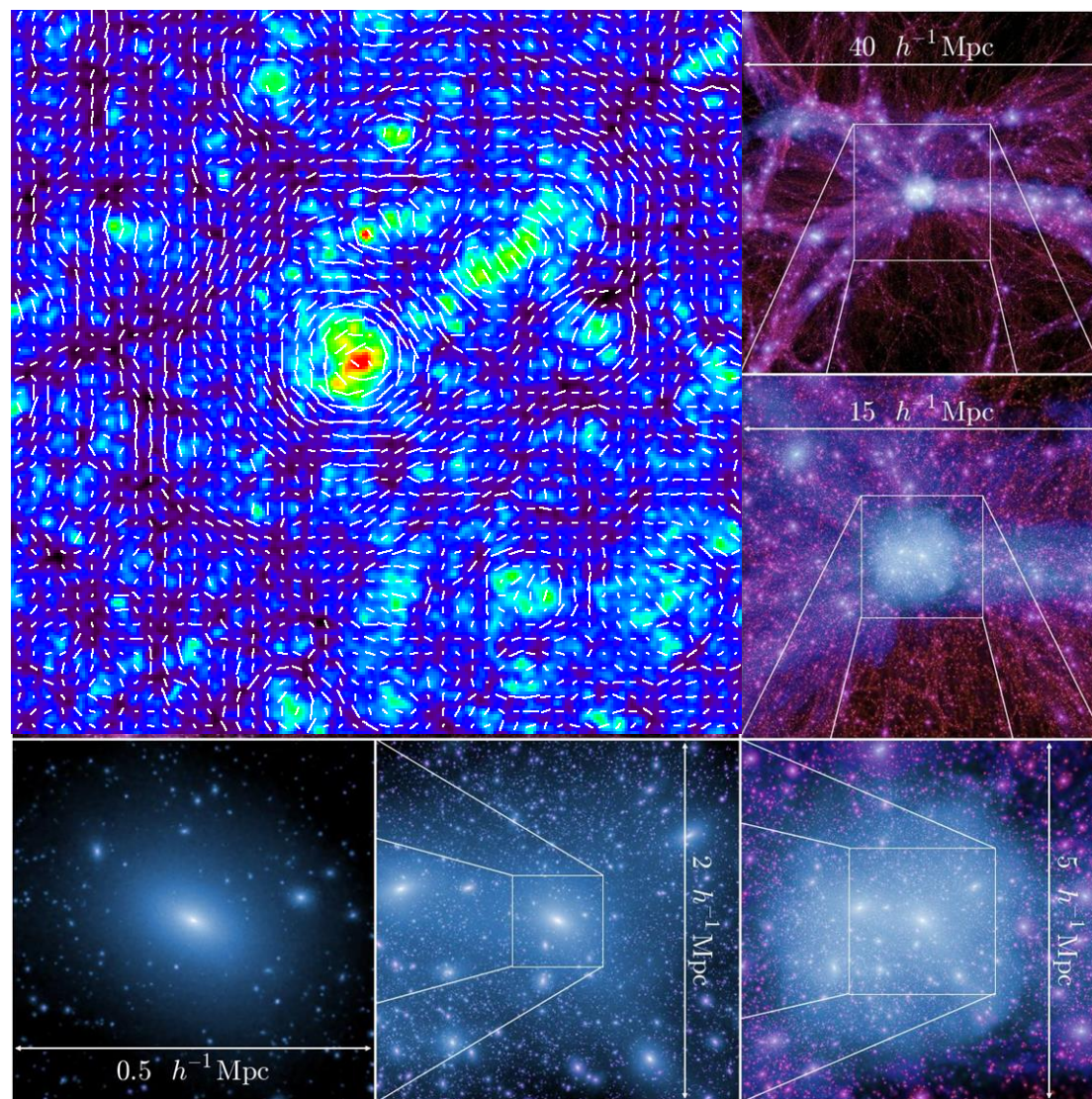
- ✓ Mass, $M(r)$:
Cluster cosmology
- ✓ Concentration, $c(M,z)$:
Halo mass assembly
- ✓ Central cusp:
DM nature

Substructure

- ✓ Mass accretion history
- ✓ Subhalo mass function

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Tangential Shear

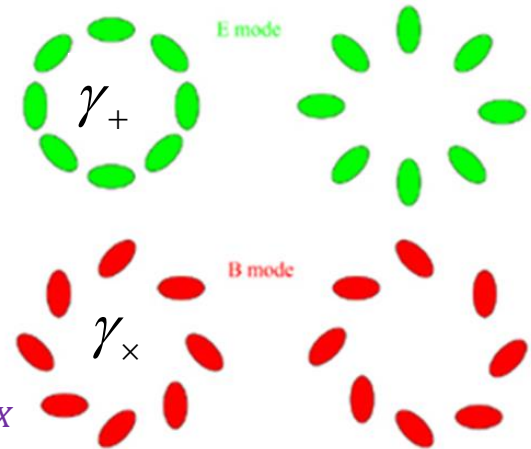
Measure of azimuthally-averaged tangential coherence of elliptical distortions around a given point (Kaiser 95):

$$\gamma_+(R) = \Delta\Sigma(R) / \Sigma_{\text{crit}}$$

$$(\Gamma_+)_{ij} = \left(\delta_i \delta_j - \frac{1}{2} \Delta^{(2)} \delta_{ij} \right) \psi_+$$

$$\gamma_\times(R) = 0$$

$$(\Gamma_\times)_{ij} = (\epsilon_{kj} \partial_i \partial_k - \epsilon_{ki} \partial_j \partial_k) \psi_\times$$



$\Delta\Sigma(R)$ is the *radially-modulated surface mass density*:

$$\Delta\Sigma(R) = \underline{\Sigma(< R)} - \Sigma(R)$$

Sensitive to interior mass

$$\Sigma = \int dl \delta\rho$$

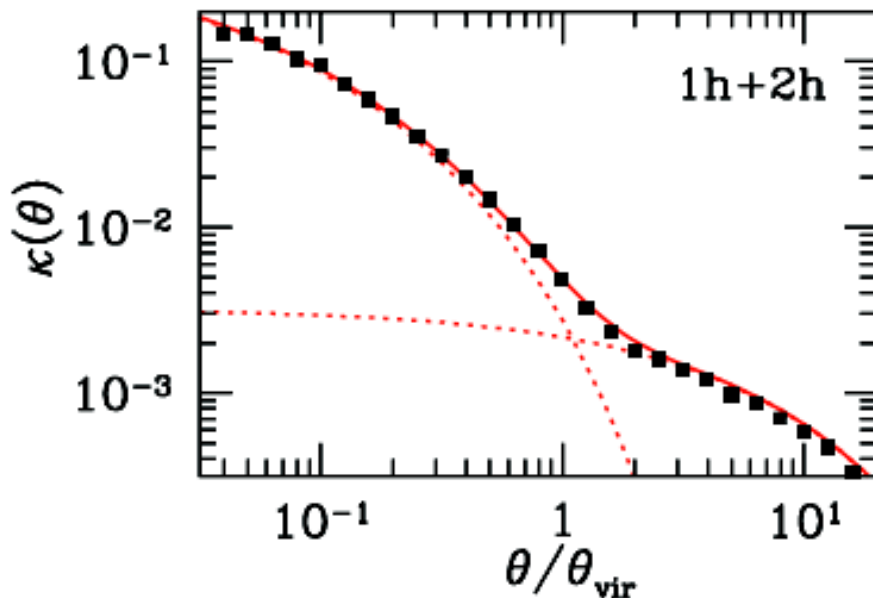
$\Sigma_{\text{crit}}(z_l, z_s)$ is the *critical surface mass density of lensing*

Shear doesn't see mass sheet

Averaged lensing profiles in/around LCDM halos (Oguri+Hamana 11)

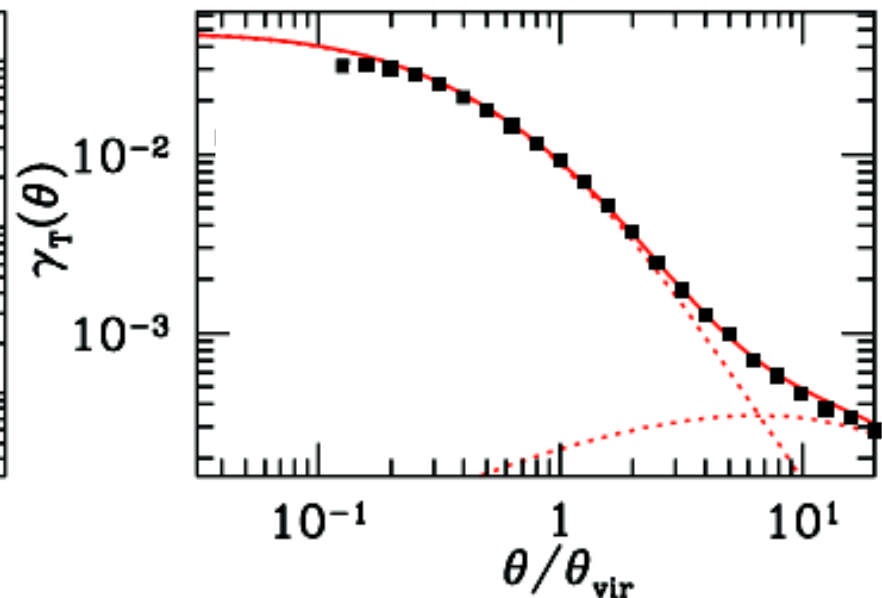
Total

$$\kappa = \Sigma(R) / \Sigma_{\text{crit}}$$



Modulated

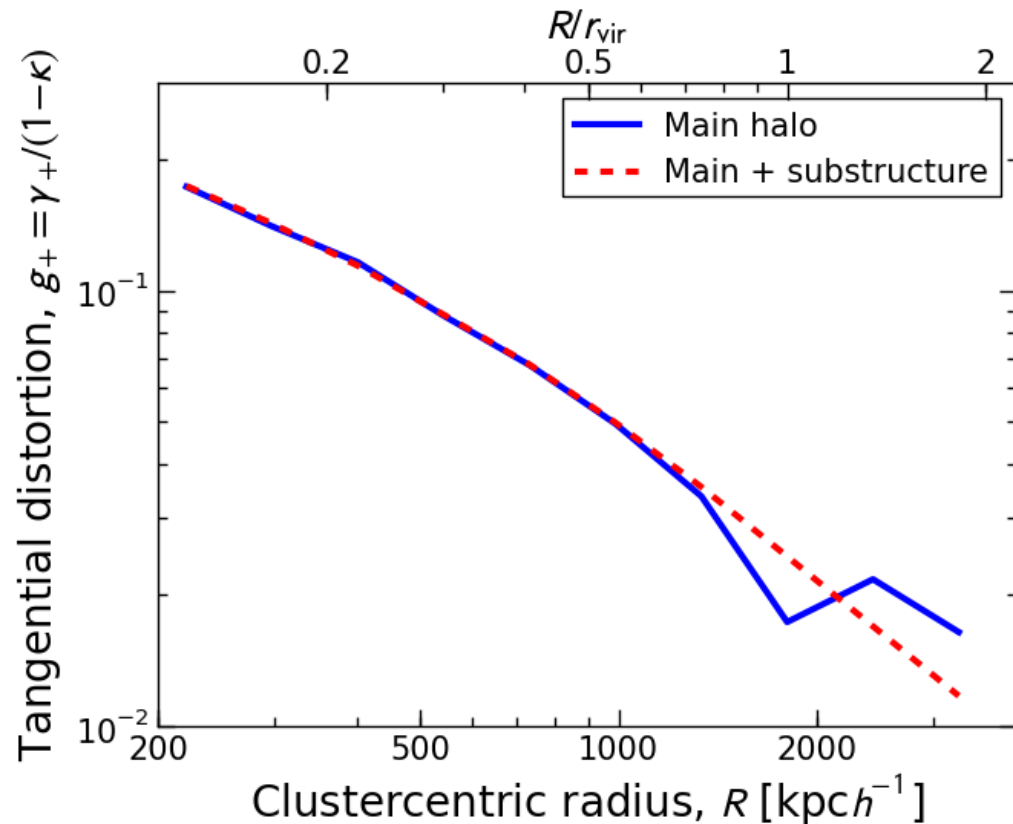
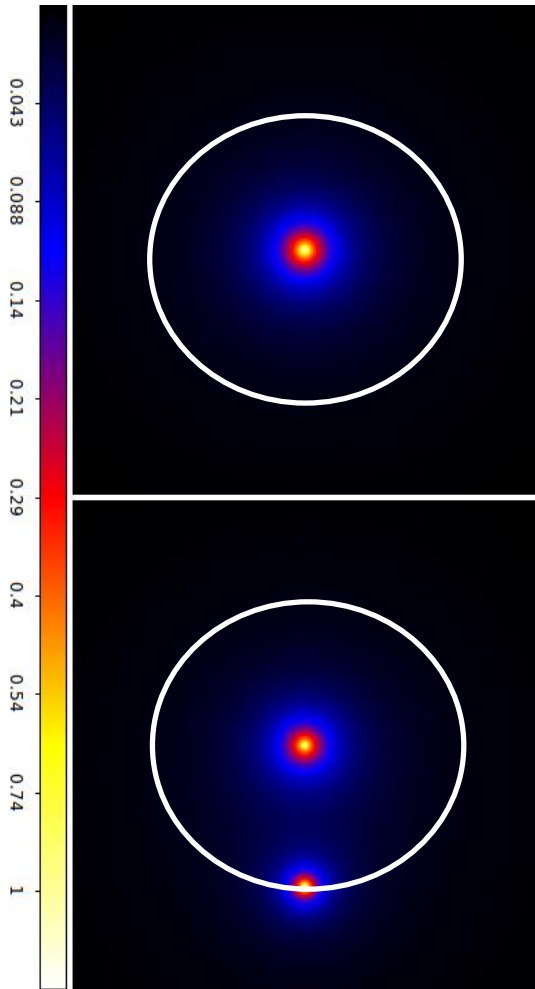
$$\gamma_+ = \Delta\Sigma(R) / \Sigma_{\text{crit}}$$



- Tangential shear is a powerful probe of **1-halo term**, or **internal halo structure**.
- Shear alone cannot recover absolute mass, known as **mass-sheet degeneracy**

Non-local substructure effect

A substructure at $R \sim r_{\text{vir}}$ of the main halo, modulating $\Delta\Sigma(R) = \Sigma(< R) - \Sigma(R)$



Known $\sim 10\%$ negative bias in mass estimates from tangential-shear fitting, inherent to clusters sitting in substructured field (Rasia+12)

Cluster Lensing Magnification



MACSJ1149 ($z=0.54$)

Zheng+CLASH. 2012, *Nature*, 489, 406

Magnification Effects

Source plane

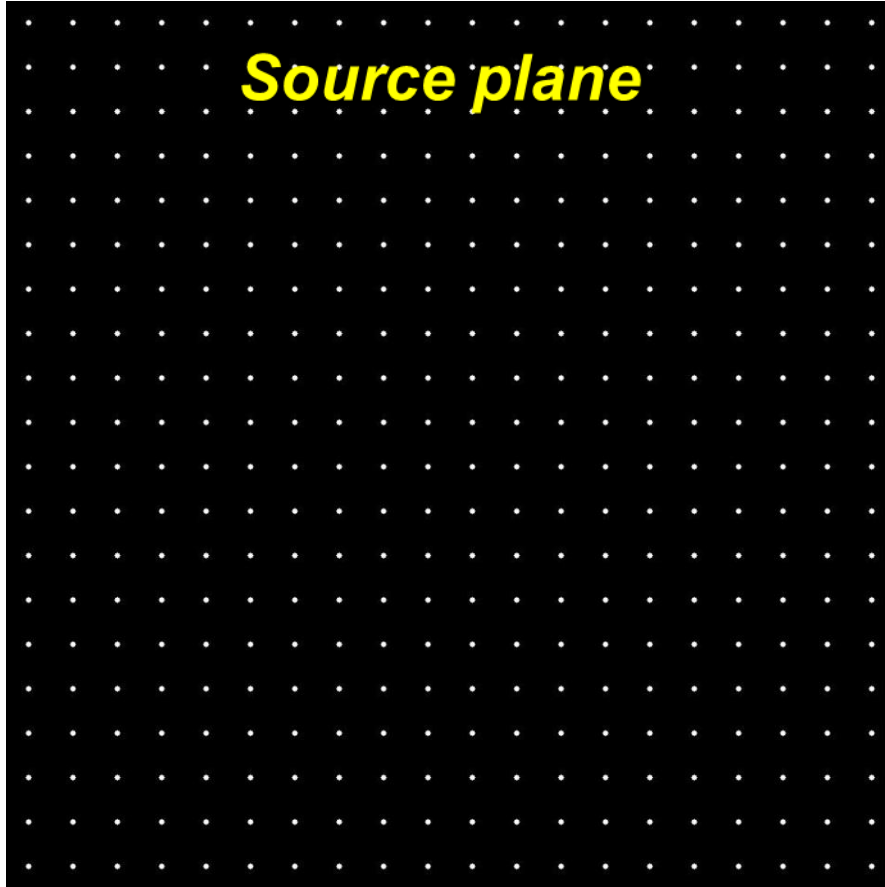
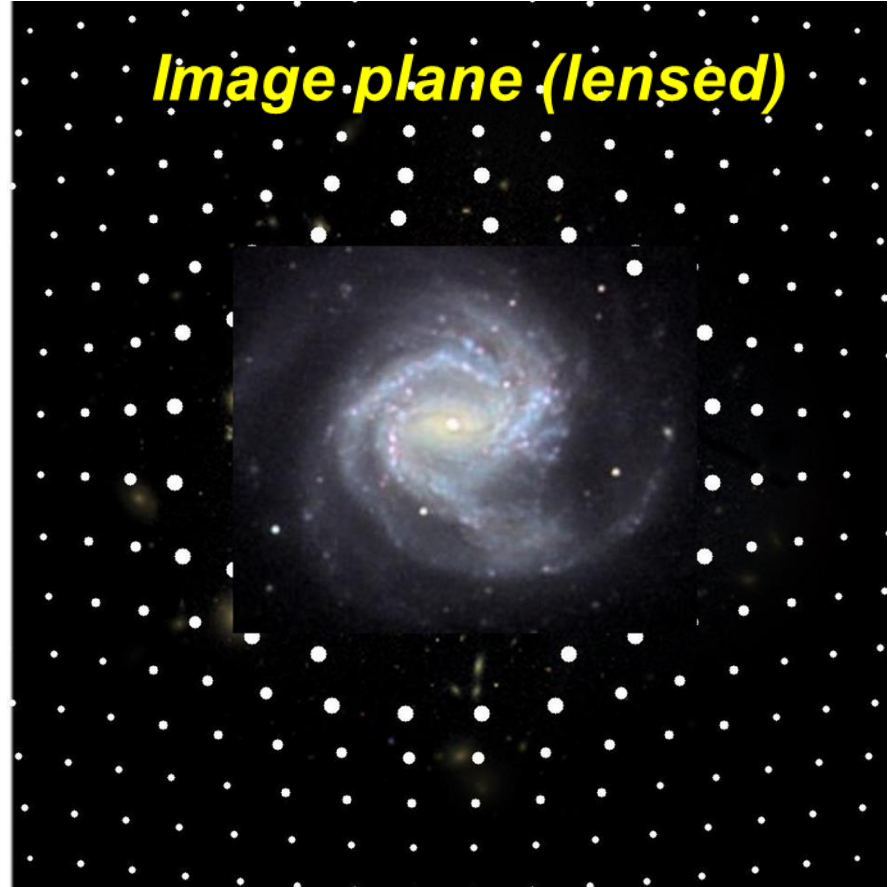


Image plane (lensed)



- Image flux, F : $\mu \sim 1+2\kappa$
- Image size, r : $\mu^{1/2} \sim 1+\kappa$
- Sky area, $\Delta\Omega$: $\mu \sim 1+2\kappa$

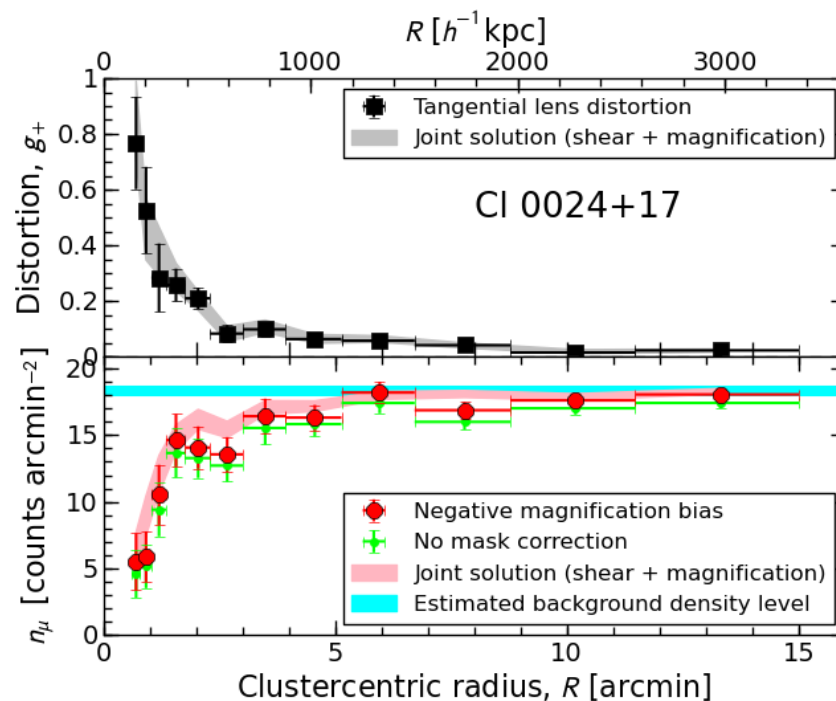
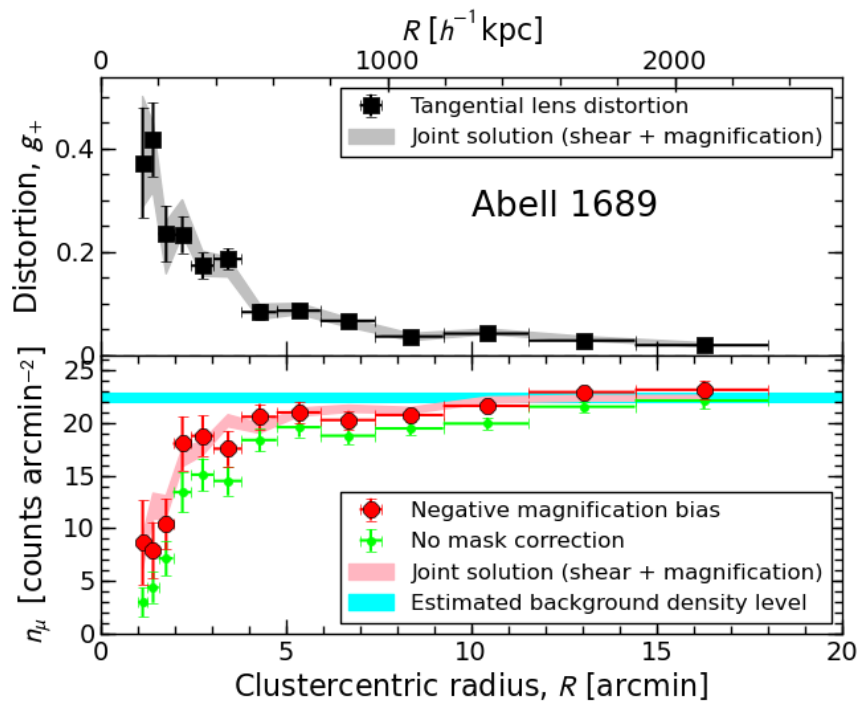
Sensitive to “local” matter density

$$\kappa = \Sigma / \Sigma_{\text{crit}}$$

Negative Magnification Bias: Count Depletion

Geometric shear-magnification consistency

Number counts of red galaxies at $\langle z \rangle \sim 1$ highly depleted



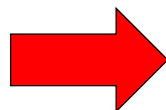
Umetsu+11a, ApJ, 729, 127

Subaru telescope data

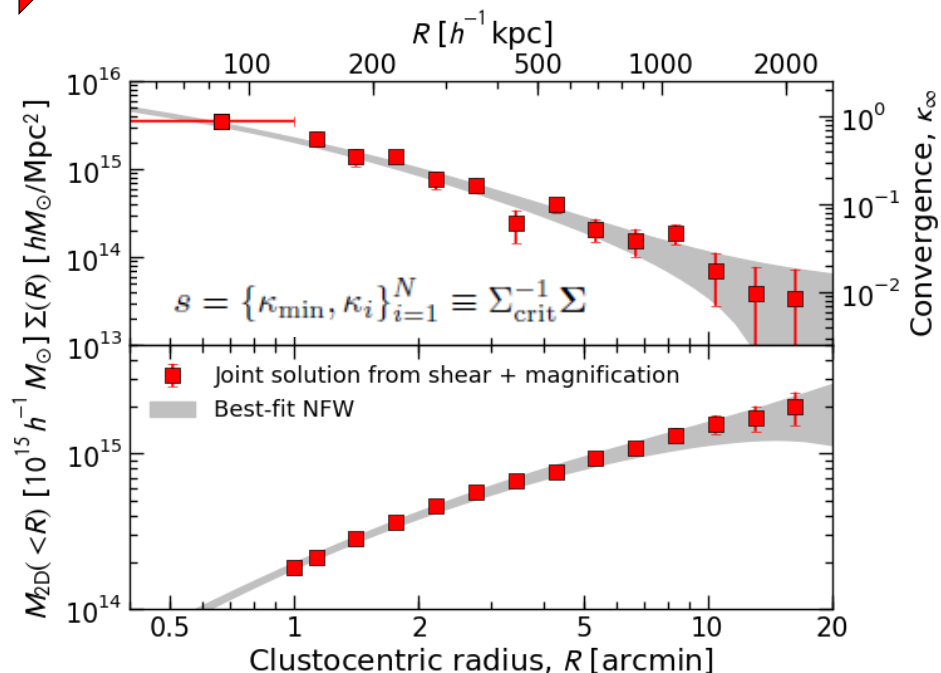
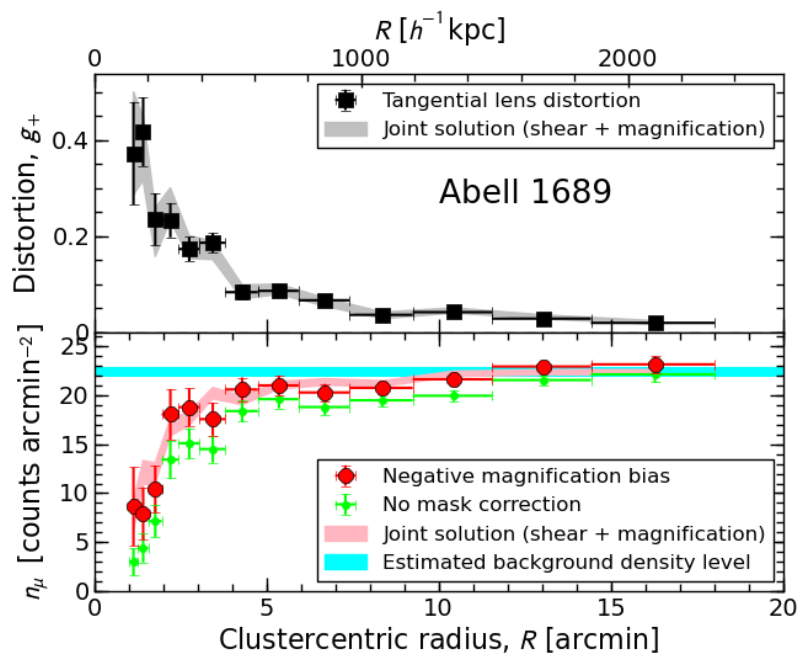
Combining Shear and Magnification

Bayesian joint-likelihood analysis (Umetsu+11a; Umetsu 13)

Shear + magnification



Non-parametric $\Sigma(R)$ solution

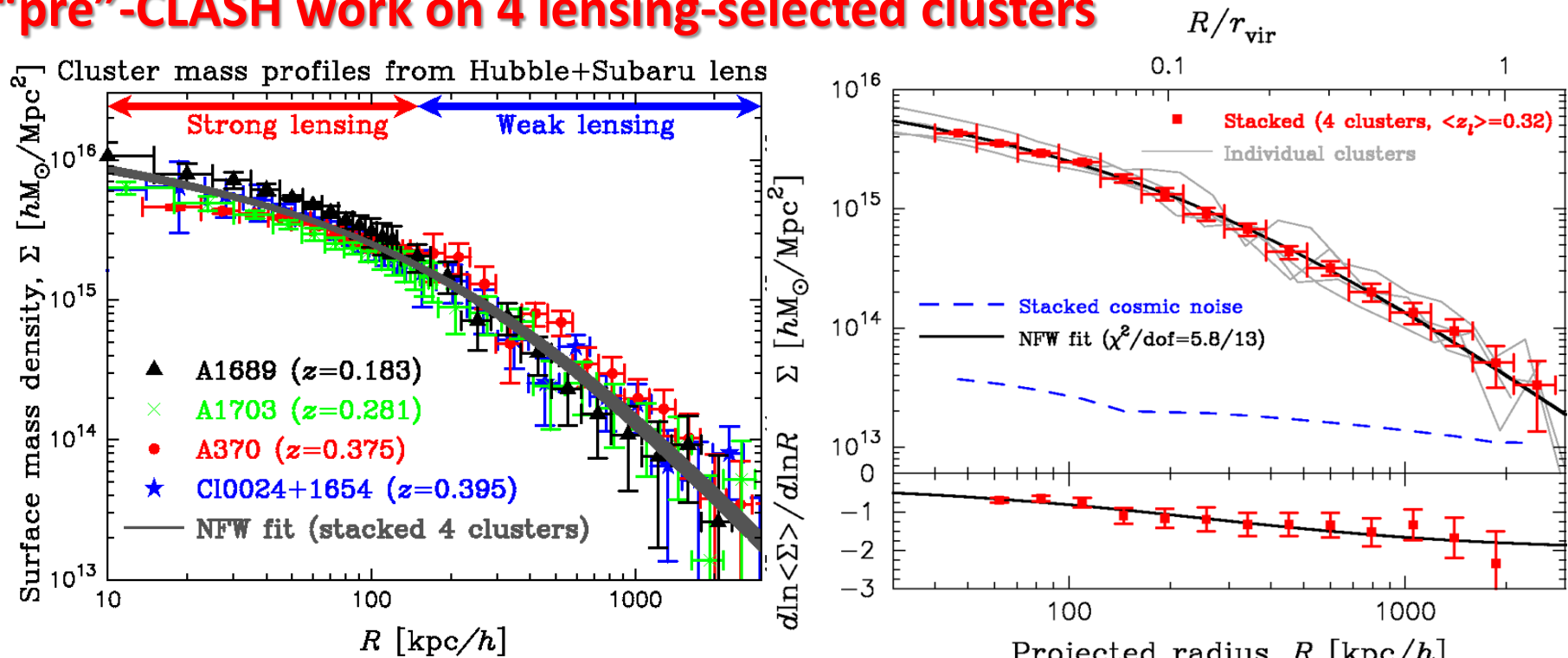


- Mass-sheet degeneracy broken
- Total statistical precision improved by $\sim 20\text{-}30\%$
- Calibration uncertainties marginalized over: $c = \{\langle W \rangle_s, f_{W,s}, \langle W \rangle_\mu, \bar{n}_\mu, s_{\text{eff}}\}$.

Mass profiles from full-lensing analysis

Multi-scale, multi-probe lensing approach (**strong-lensing** + **shear** + **magnification**) with *HST*+*Subaru*, probing > 2 decades in cluster-centric radius, $R = [5 \times 10^{-3}, 1.5] R_{\text{vir}}$

“pre”-CLASH work on 4 lensing-selected clusters





CLASH:

Cluster Lensing And Supernova survey with Hubble

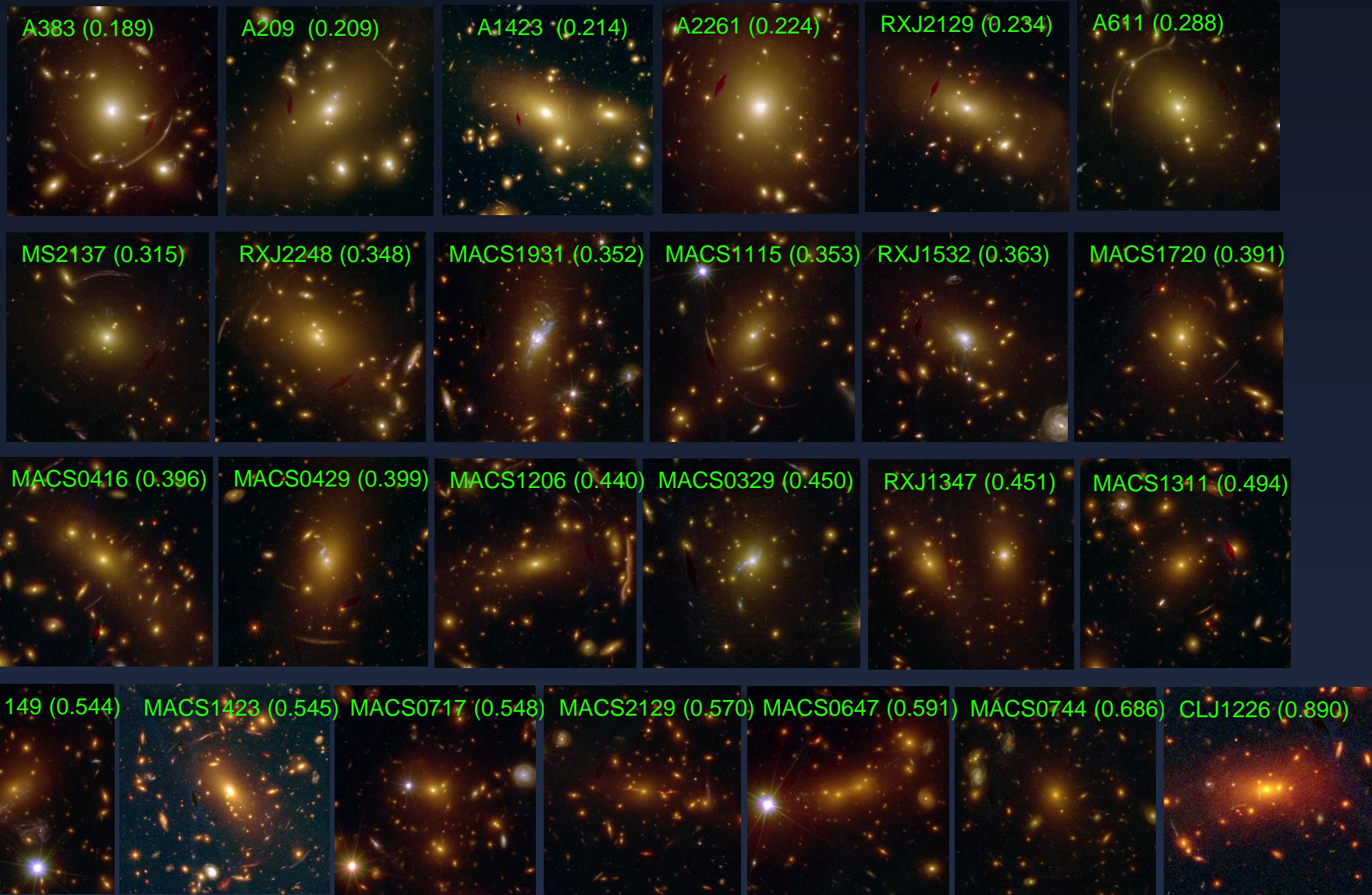
An HST Multi-Cycle Treasury Program designed to place new constraints on the fundamental components of the cosmos: dark matter, dark energy, and baryons.



Wide-field Subaru imaging ($0.4 - 0.9 \mu\text{m}$) plays a unique role in complementing deep HST imaging of cluster cores.

My talk will focus on CLASH-WL results based primarily on Subaru data

The CLASH Gallery (HST)



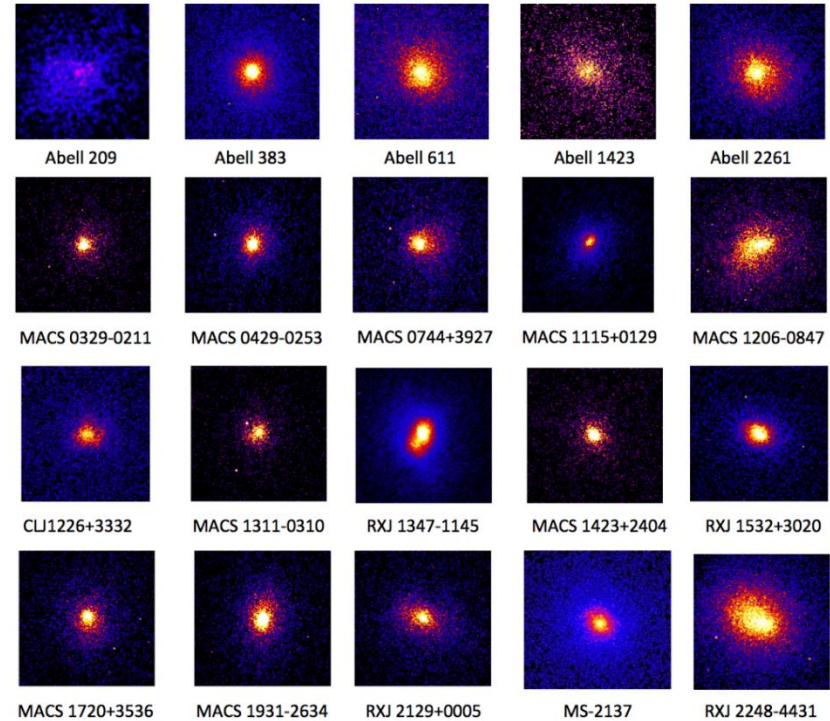
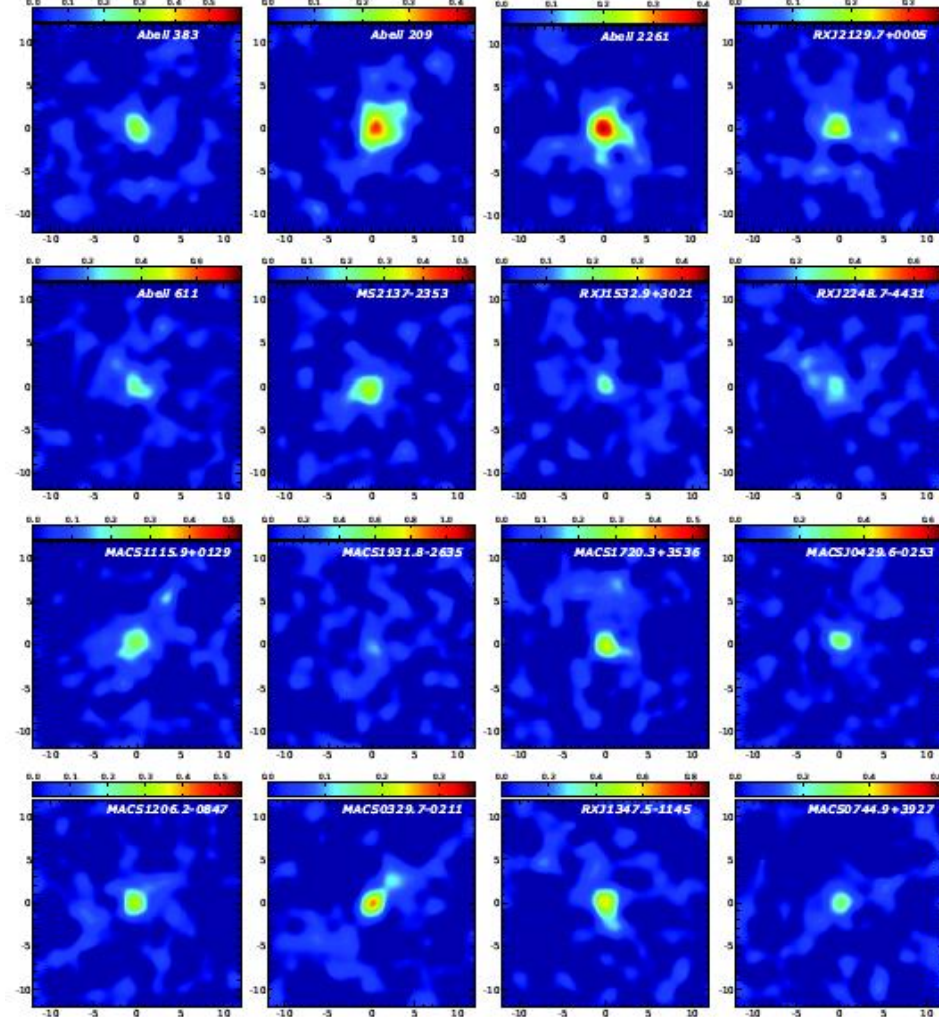
The final HST observation for CLASH was on 9-July-2013 ... 963 days, 15 hrs, 31 min after first obs.



CLASH X-ray-selected subsample

WL mass maps: 16 clusters completed

X-ray maps: 20 CLASH clusters are purely X-ray selected to be massive and relaxed



Umetsu+CLASH 14, in prep (Subaru, 24'x24')

Postman+CLASH 12, ApJS

Ensemble-averaged DM halo profile

Stacking of weak-lensing signals by weighting individual clusters according to the sensitivity kernel matrix:

$$\langle\langle \widehat{\Delta\Sigma}_+ \rangle\rangle = \left(\sum_n \mathcal{W}_{+n} \right)^{-1} \left(\sum_n \mathcal{W}_{+n} \widehat{\Delta\Sigma}_{+n} \right),$$

with the individual sensitivity matrix

$$(\mathcal{W}_{+n})_{ij} \equiv \Sigma_{c,n}^{-2} (C_{+n}^{-1})_{ij}$$

defined with the total covariance matrix

$$C_+ = C_+^{\text{stat}} + C_+^{\text{sys}} + C_+^{\text{lss}}.$$

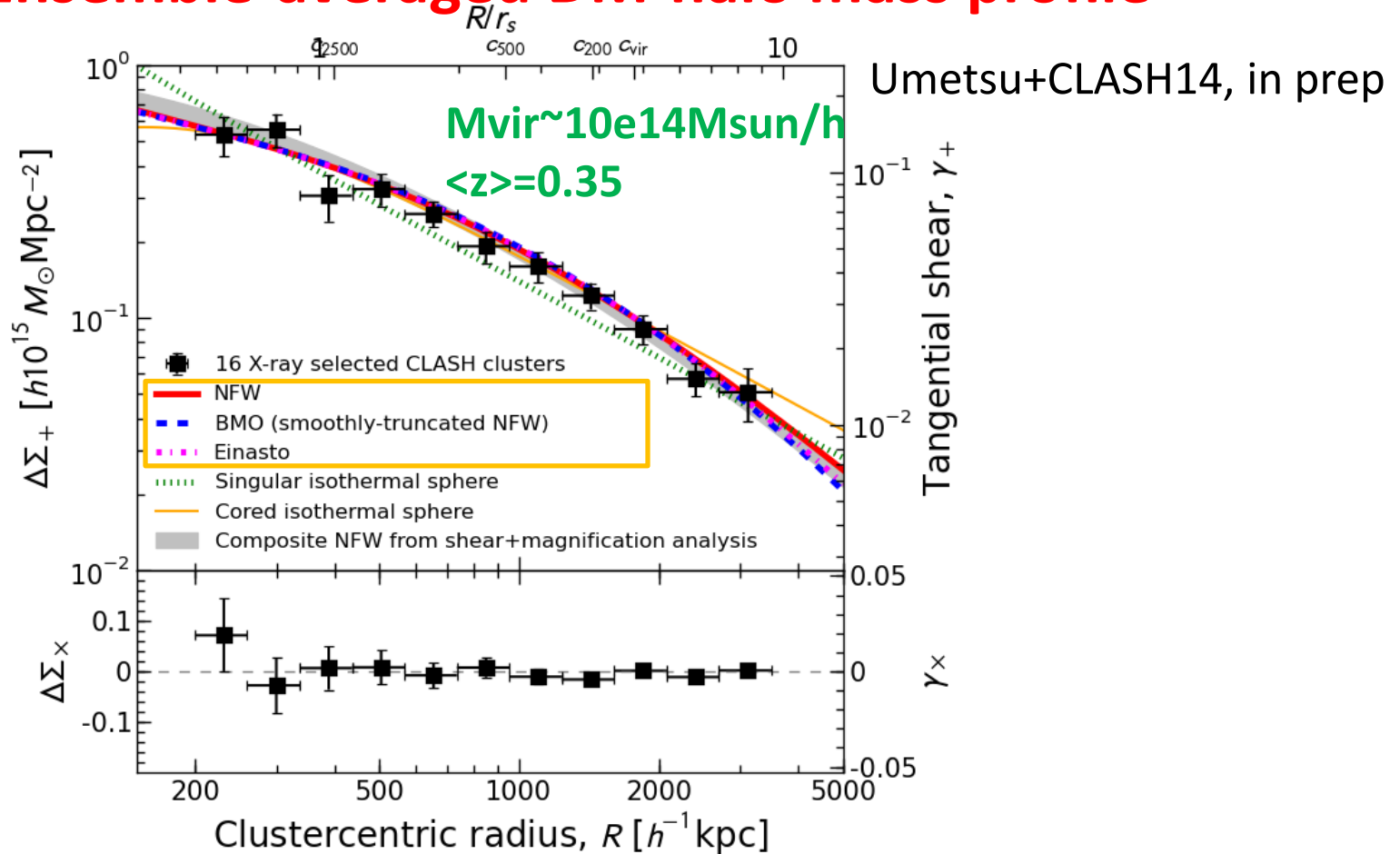
With “trace-approximation”, averaging is interpreted as

$$\langle\langle \Sigma_c^{-1} \rangle\rangle = \frac{\sum_n \text{tr}(\mathcal{W}_{+n}) \Sigma_{c,n}^{-1}}{\sum_n \text{tr}(\mathcal{W}_{+n})},$$



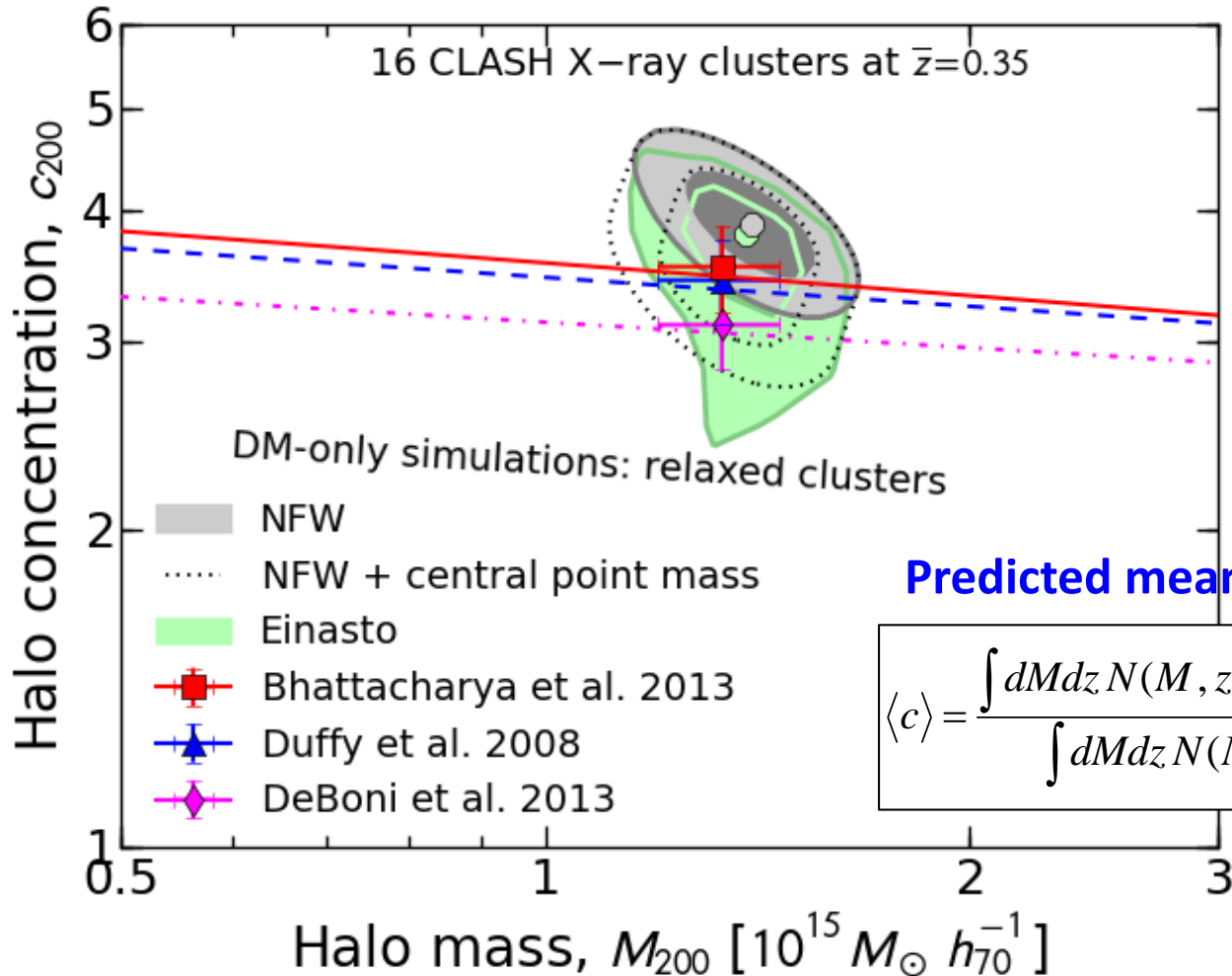
CLASH-WL: Stacked Shear-only Analysis

Ensemble-averaged DM-halo mass profile



Consistent with a family of density profiles for collisionless-DM halos in gravitational equilibrium (NFW, BMO, Einasto)

CLASH-WL: Mass-concentration relation



Predicted mean concentration

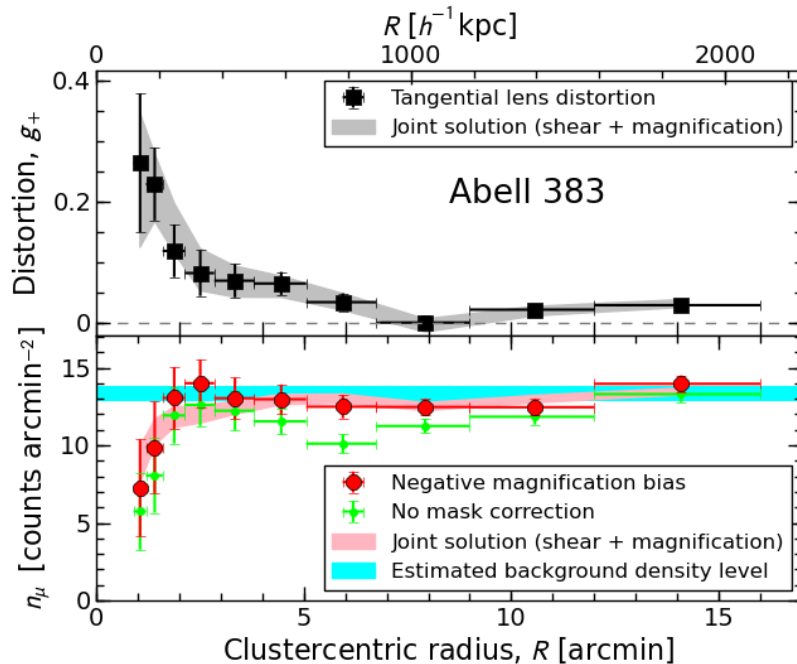
$$\langle c \rangle = \frac{\int dM dz N(M, z) \hat{c}(M, z)}{\int dM dz N(M, z)} \approx \frac{\sum_n \text{tr}(W_n) \hat{c}(M_n, z_n)}{\sum_n \text{tr}(W_n)}$$



CLASH-WL: Shear+Magnification measurements of 16 X-ray clusters

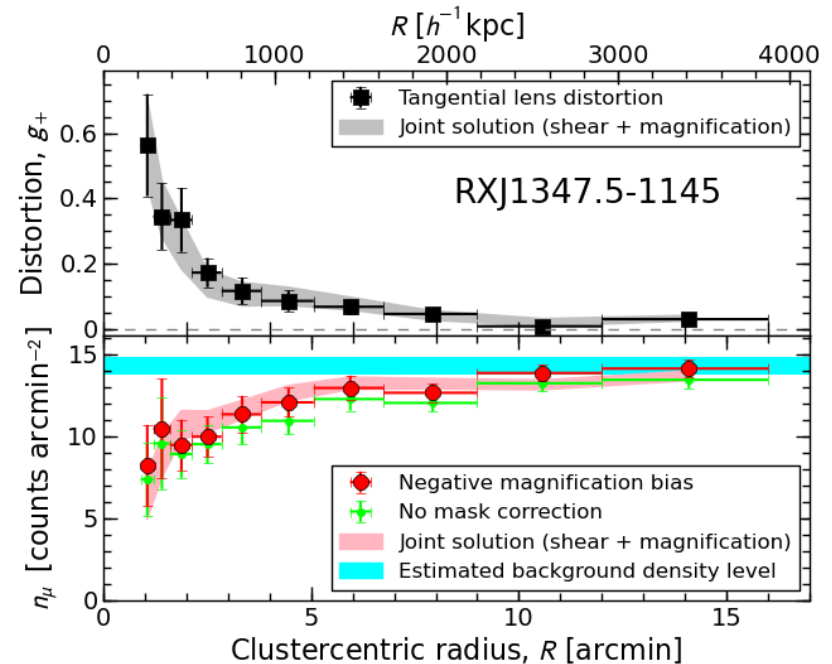
CLASH low mass

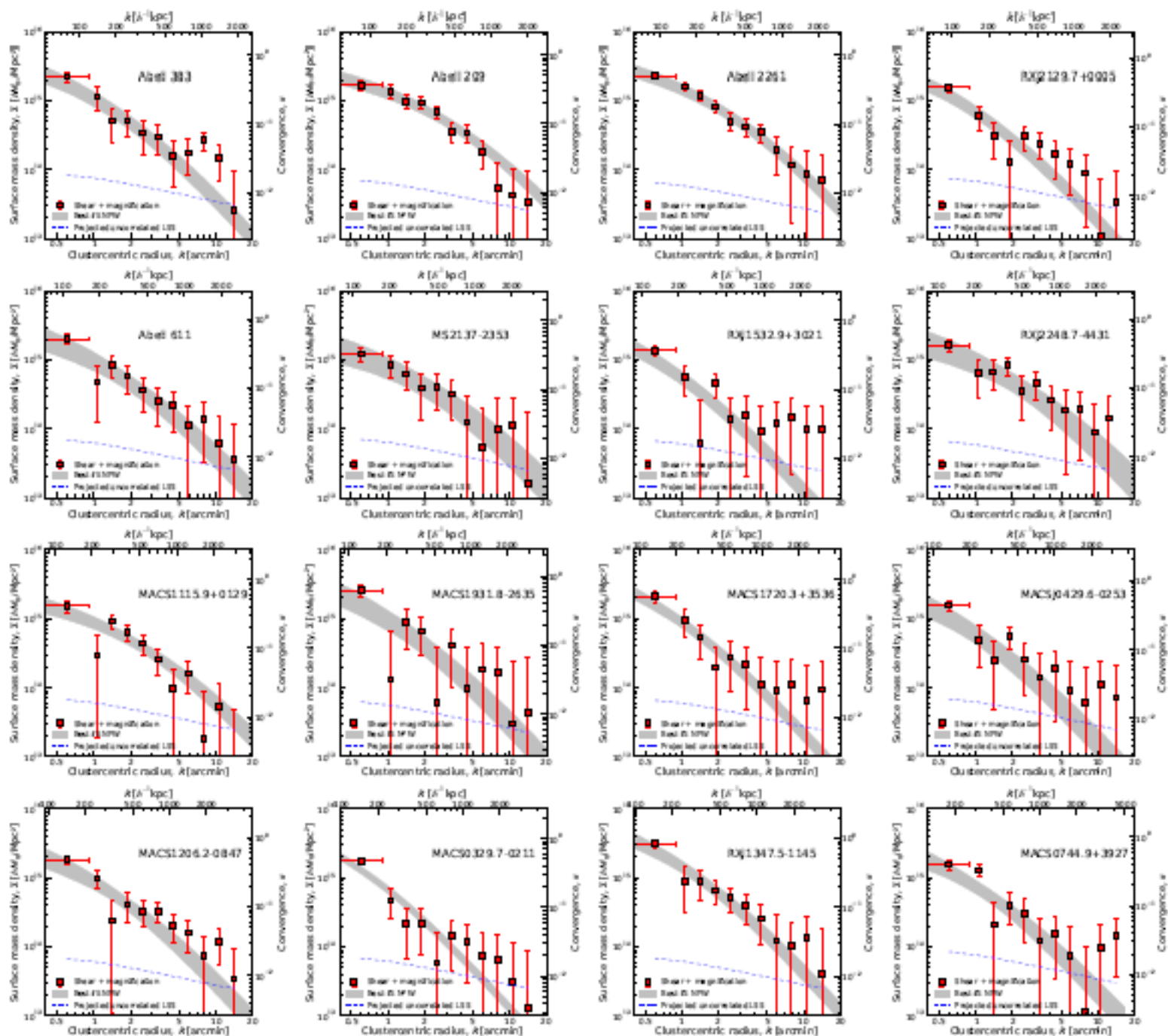
$M_{\text{vir}}=6e14M_{\text{sun}}/h$ ($z=0.19$)



CLASH high mass

$M_{\text{vir}}=23e14M_{\text{sun}}/h$ ($z=0.45$)

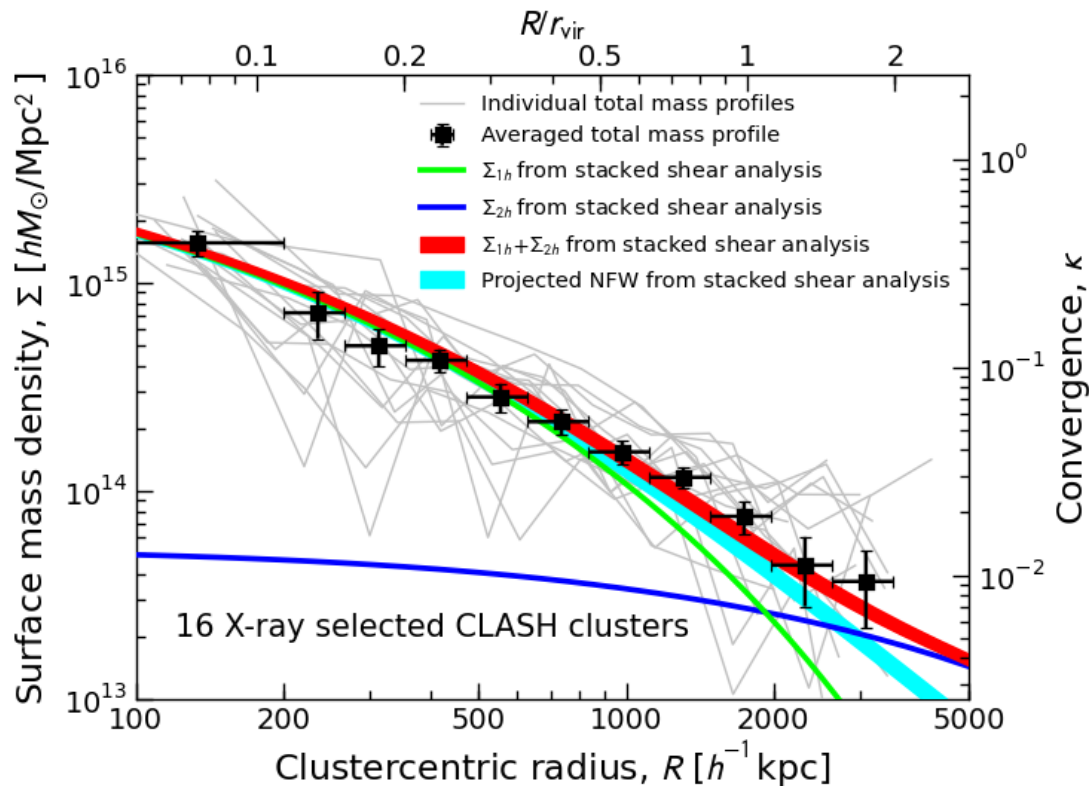




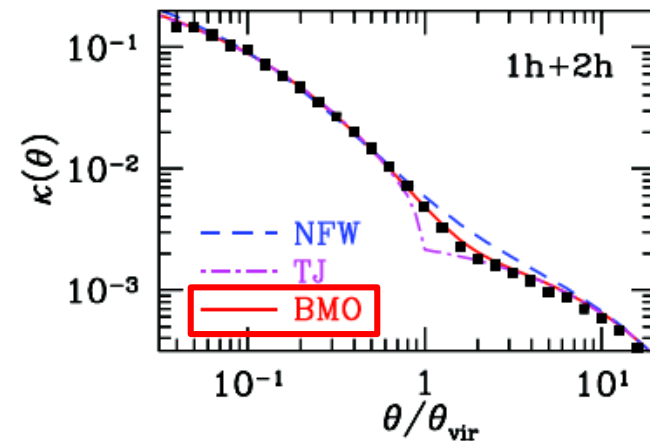


CLASH-WL: Stacked total mass profile from combined shear + magnification

- Measuring 1h+2h term out to $R=2r_{\text{vir}}$ around 16 X-ray clusters with $\langle M_{\text{vir}} \rangle = 10e14 M_{\text{sun}}/h$ at $\langle z \rangle = 0.35 \rightarrow$ halo bias $b_{\text{h}}^{\text{L}} = 9$ (Tinker+10)
- Testing shear vs. magnification consistency in the context of LCDM

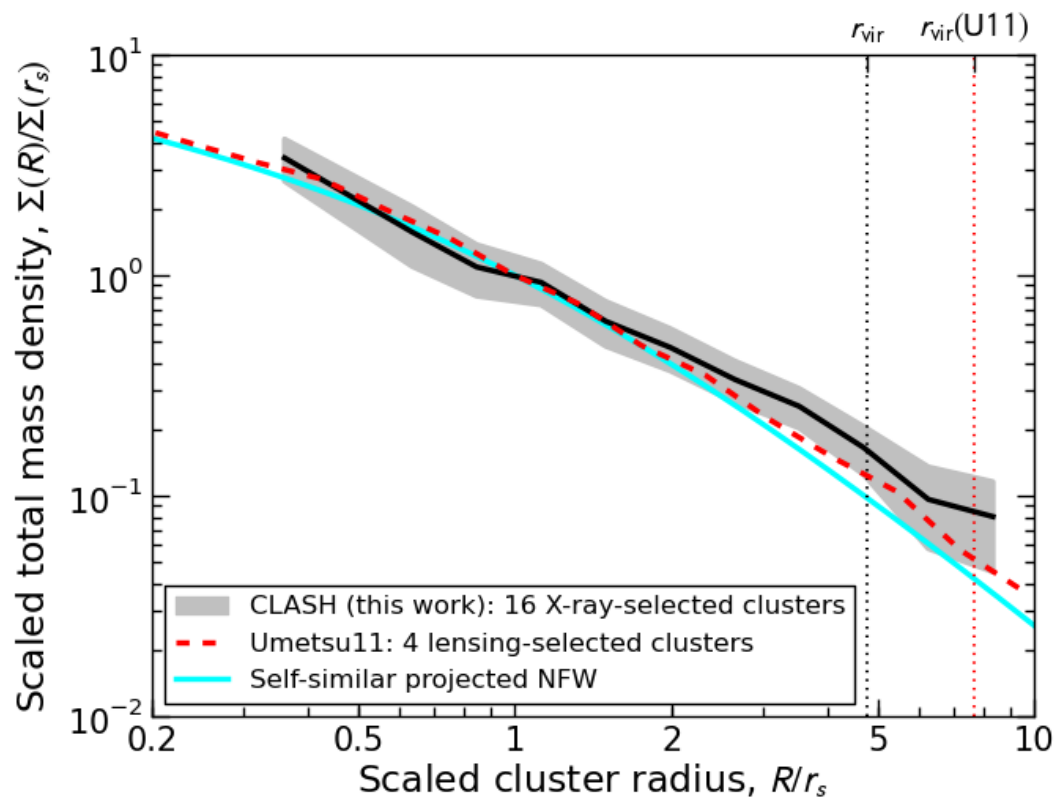


2D halo model decomposition:
smoothly-truncated NFW (BMO) + LCDM 2h-term



“Scaled” Mass Profile Shape

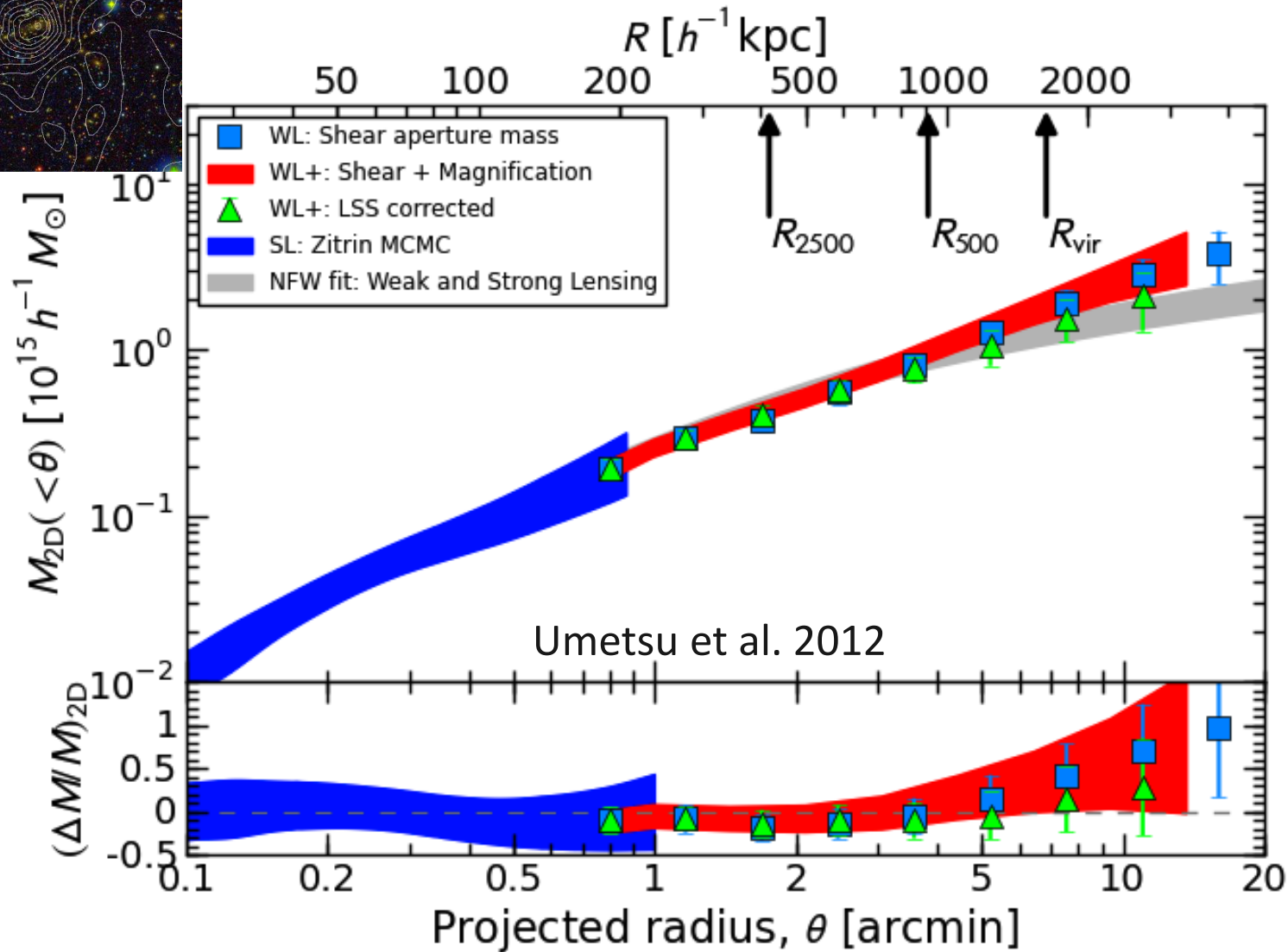
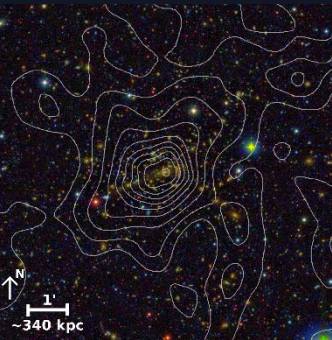
Strong-lensing (SL) vs. X-ray selected cluster samples



- When scaled, their ensemble-averaged mass profiles are consistent within errors.
- The SL clusters appear to have a steeper outer profile: i.e., less significant 2h-term in projection space.

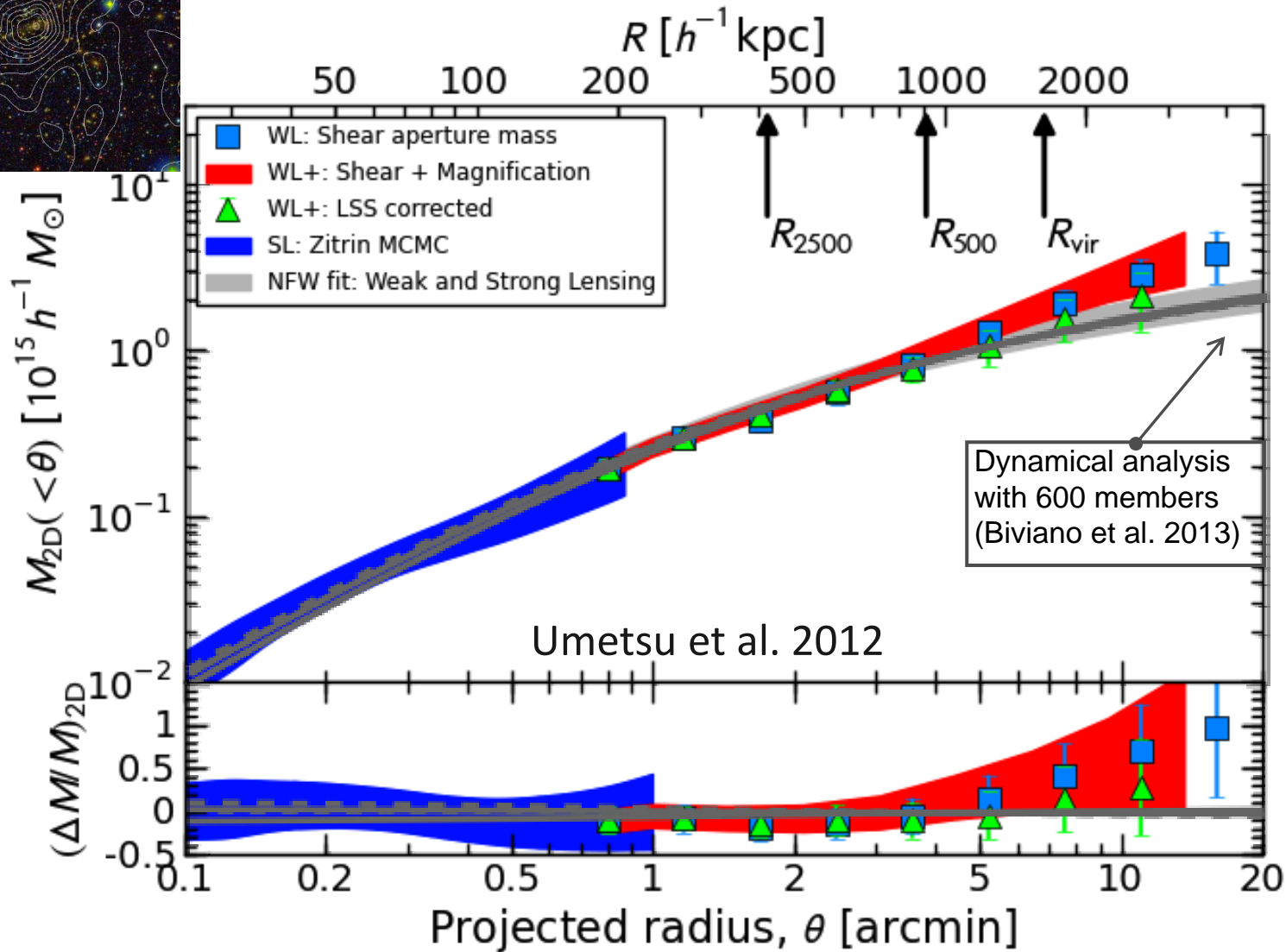
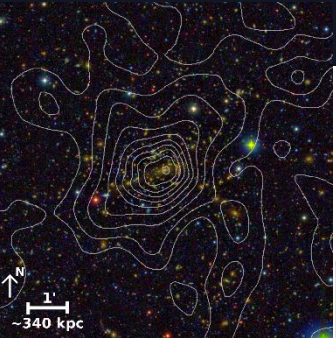
MACS1206 ($z=0.44$): A cluster with a high degree of dynamical relaxation

Total mass profiles from completely independent methods agree.



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Total mass profiles from completely independent methods agree.



Constraining the DM Equation of State

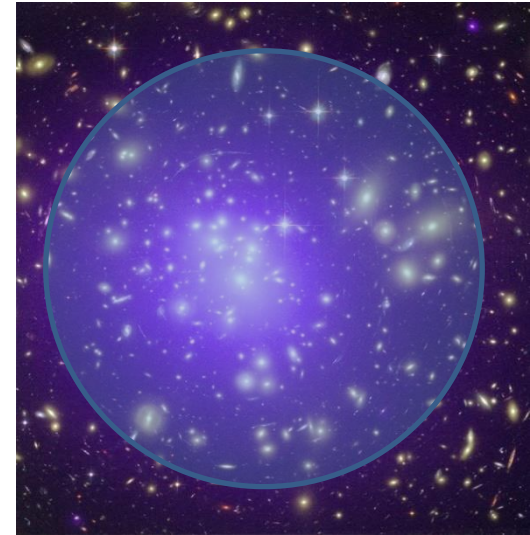
B. Sartoris et al., submitted to ApJ Letters

- By testing whether the intracluster DM is pressureless ($w=0$) using cluster mass profiles $M(<r)$ of MACS1206 determined from 2-independent ways:
 - **Gravitational lensing with HST+Subaru** (Umetsu+2012)
 - **Galaxy kinematics with VLT/VIMOS** (Biviano+2013)
- Test made possible by our high-quality CLASH data for an equilibrium cluster:

$$w(r) = \frac{p_r(r) + 2p_t(r)}{c^2 3\rho(r)}$$



Framework



Consider the static, spherically-symmetric metric within a DM halo of the form:

$$ds^2 = -e^{-2\Phi(r)} dt^2 + \left[1 - \frac{2Gm(r)}{r}\right]^{-1} dr^2 + r^2 d\Omega^2.$$

Consider an intracluster DM fluid with anisotropic pressure. In this metric, the Einstein field equations read:

$$\begin{aligned}\rho(r) &= \frac{1}{8\pi G} \frac{m'}{r^2}, \\ p_r(r) &= -\frac{1}{8\pi G} \frac{2}{r^2} \left[\frac{m}{r} - r\Phi' \left(1 - \frac{2m}{r}\right) \right], \\ p_t(r) &= \frac{1}{8\pi G} \left\{ \left(1 - \frac{2m}{r}\right) \left[\frac{\Phi'}{r} + \Phi'^2 + \Phi'' \right] - \left(\frac{m}{r}\right)' \left(\frac{1}{r} + \Phi'\right) \right\}.\end{aligned}$$

The equation of state of this DM fluid is defined as

$$w(r) = \frac{p_r + 2p_t}{3\rho}.$$

Consider the weak-field limit, $|\Phi| \ll 1$, $Gm/r \ll 1$.

DM EoS from kinematics+lensing

The Jeans equation provides a way to measure the cluster mass profile from **cluster galaxy kinematics**

$$m_K(r) = -\frac{r\sigma_r^2}{G} \left[\frac{d \ln n_g}{d \ln r} + \frac{d \ln \sigma_r^2}{d \ln r} + 2\beta \right],$$

where galaxies as the probe particles are non-relativistic, $\sigma_r, \sigma_t \ll 1$ with $\beta = 1 - \sigma_t^2/(2\sigma_r^2)$. In our metric, the kinematic mass profile is related to the potential by

$$m_K(r) = \frac{r^2}{G} \Phi' \approx 4\pi \int [1 + 3w(r)] r^2 \rho(r) dr.$$

Gravitational lensing is sensitive to g_{00} and g_{rr} . Hence, its potential and associated mass profile are defined by

$$2\Phi_l \equiv \Phi + G \int \frac{m(r)}{r^2} dr,$$
$$m_L(r) \equiv \frac{r^2}{G} \Phi_l' = \frac{1}{2} [m_K(r) + m(r)].$$

To first order, the DM equation of state is sensitive to the derivatives of the lensing and kinematic mass profiles:

$$w(r) \approx \frac{2 m'_K(r) - m'_L(r)}{3 m'_L(r) - m'_K(r)}.$$

$$\langle w \rangle = 0.00 \pm 0.14(\text{stat}) + 0.03(\text{syst})$$

Consistent with $w=0$

Negligible baryonic contribution

averaged in $R=0.5-2\text{Mpc}$



Summary

- Ensemble-averaged internal halo structure $\Delta\Sigma$ (1h) of relaxed CLASH clusters in good agreement with a family of standard (collisionless) DM predictions:
 - Halo mass: $M_{200}=(1.4 \pm 0.1) 10^{15}M_{\text{sun}}$ at $z=0.35$
 - Degree of curvature: $\alpha=0.25 \pm 0.07$ (Einasto)
 - Degree of concentration: $3.3 < c_{200} < 4.2$ at 1σ
- Total matter distribution Σ (1h+2h) around clusters determined from shear+magnification, being consistent with the shear-only prediction ($b_h \sim 9$), thus establishing consistency in the context of LCDM.



Summary (contd)

- CLASH HST (SL) + Subaru (WL) + VLT (kinematics), providing high-quality data to test DM models:
 - 20 CLASH clusters X-ray-selected to be relaxed
 - 5 CLASH clusters lensing-selected (merging clusters)
- For a relaxed cluster with no orientation bias (for lensing), lensing+kinematics (HST+Subaru+VLT) can be used to test the pressureless assumption of DM.
 - CLASH-VLT redshift survey is in progress (12 southern CLASH clusters at $0.3 < z < 0.6$), providing 500 members/cluster out to $> 3\text{Mpc}$.

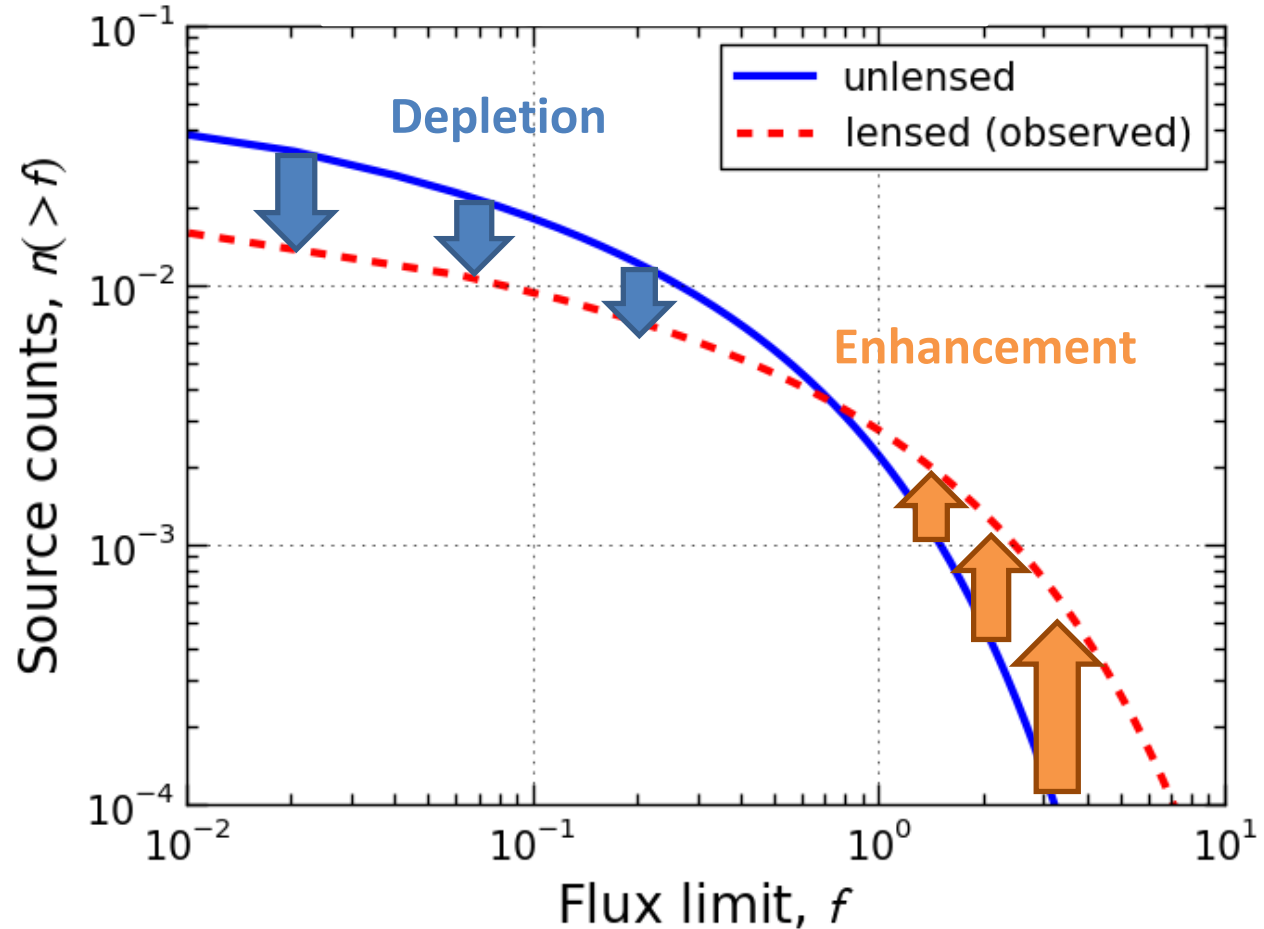
Supplemental Slides

Magnification bias effects

Flux-limited
source counts:

$$n_{\text{obs}}(> f) = \mu^{-1} n(> \mu^{-1} f)$$

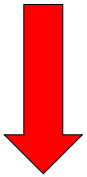
Broadhurst, Taylor &
Peacock 95



Flux amplification



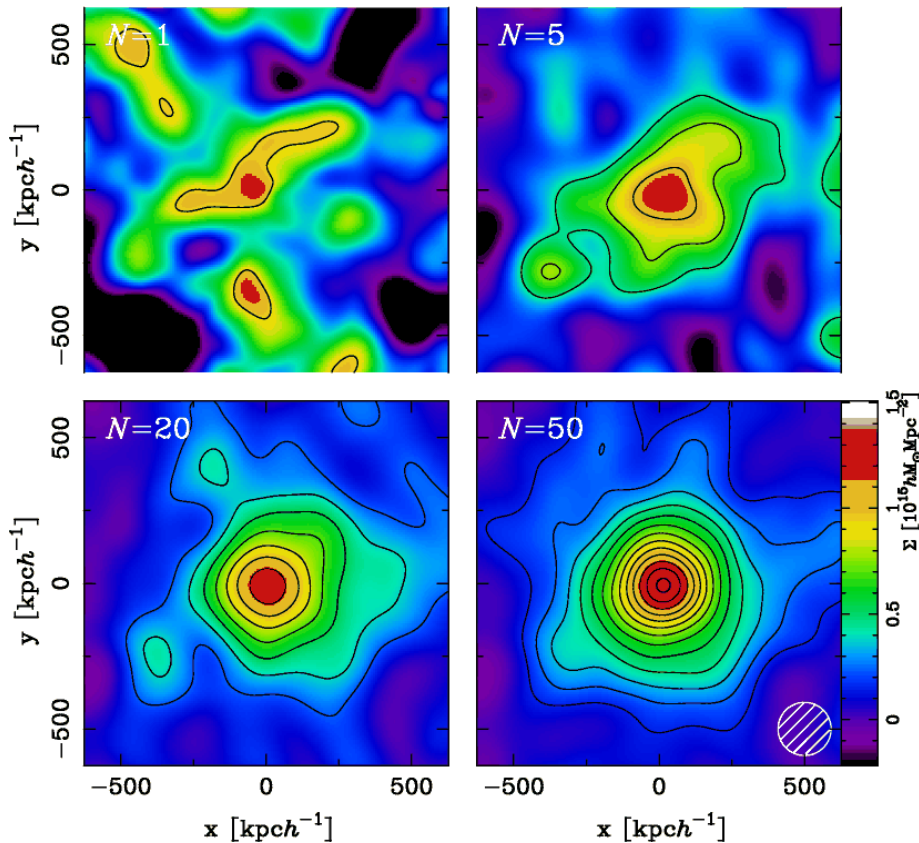
Geometric area
distortion



n/μ

Power of Stacking Analysis

Stacking lensing signals around a sample of clusters to average out projection effects due to halo asphericity, substructure, and uncorrelated LSS



November 25, 2013

PASCOS 2013

Mas Distribution in and around Galaxy Clusters from Strong-Lensing, Weak-Lensing Shear and Magnification

Keiichi Umetsu (ASIAA, Taiwan)
with the CLASH team



