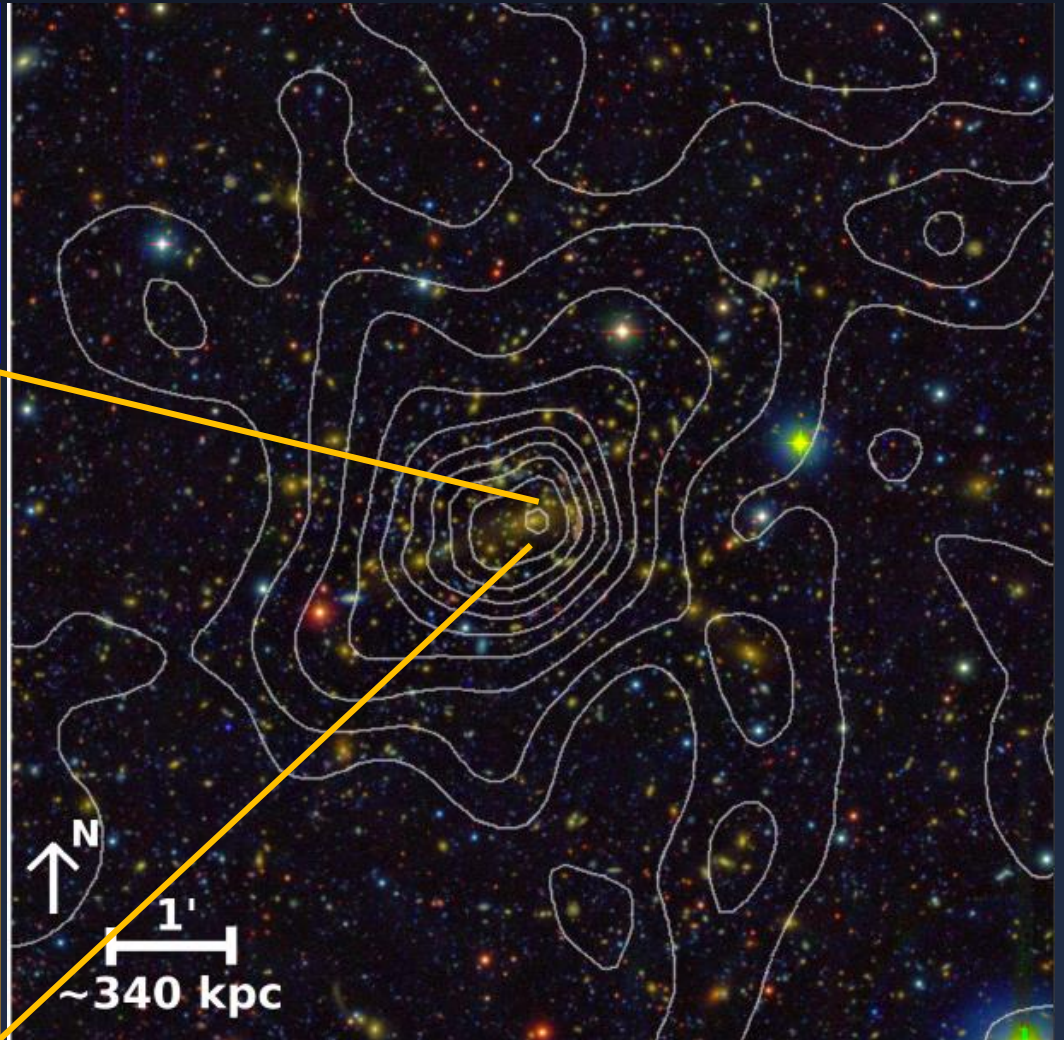
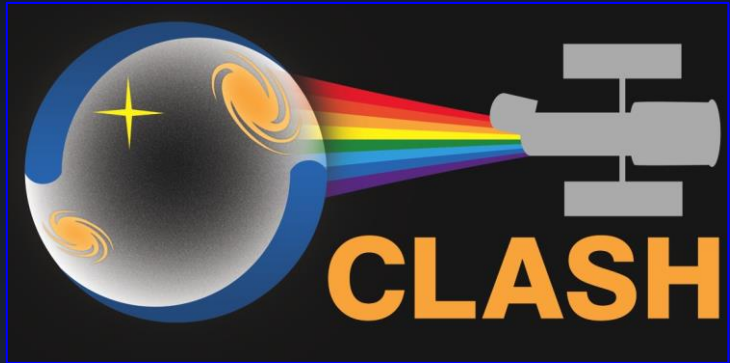


# CLASH: Subaru Weak-Lensing Results

Cluster **L**ensing **A**nd **S**upernova survey with **H**ubble



Keiichi Umetsu (ASIAA, Taiwan) with the CLASH team

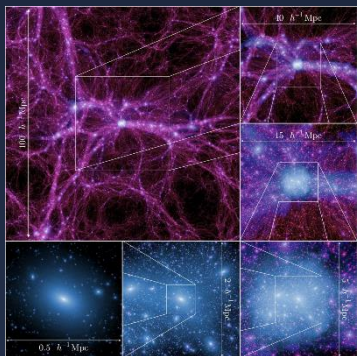


# CLASH: Observational + Theory Efforts

A 524-orbit *HST* Multi-Cycle Treasury Program designed to place new constraints on the fundamental components of the cosmos: dark matter, dark energy, and baryons (Postman+CLASH 2012)



**Wide-field Subaru imaging** ( $0.4 - 0.9 \mu\text{m}$ ) plays a unique role in complementing deep *HST* imaging of cluster cores.



**MUSIC-2** (hydro + N-body re-simulation) provides an accurate characterization of CLASH sample with testable predictions (Meneghetti+14, arXiv:1404.1384)



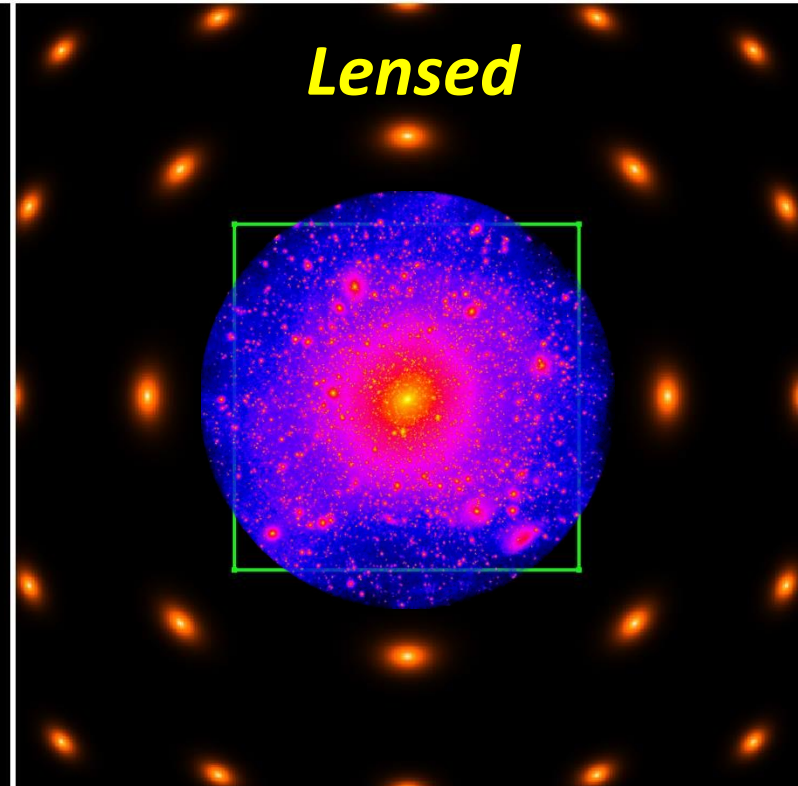
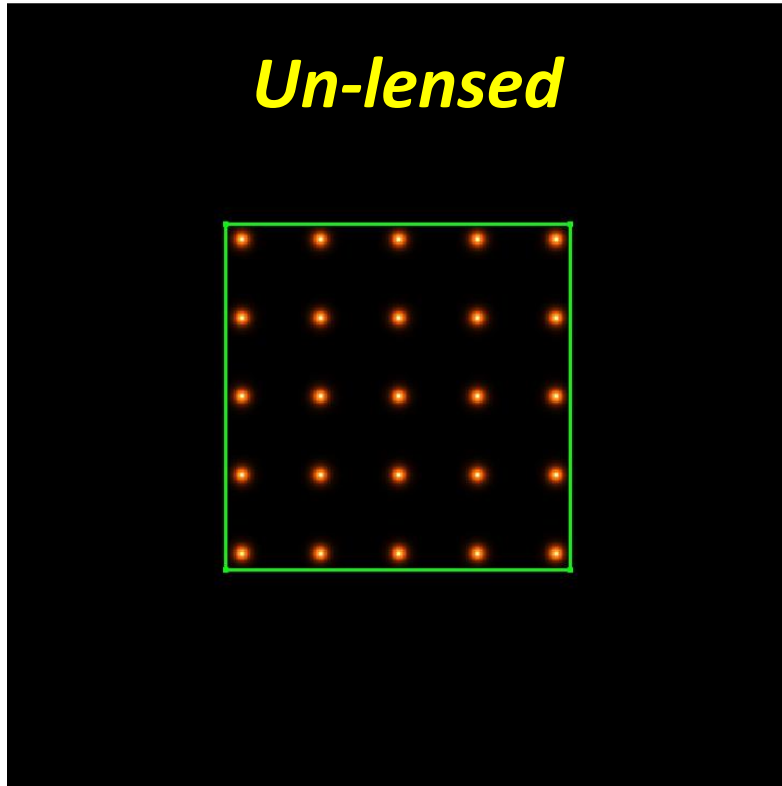
# CLASH X-ray-selected subsample

- Redshift coverage
  - $0.18 < z < 0.90$
- X-ray morphology +  $T_x$  selection
  - $T_x > 5\text{keV}$
  - Small BCG to X-ray-peak offset,  $\sigma_{\text{off}} \sim 10\text{kpc/h}$
  - Smooth regular X-ray morphology

→ **Optimized for radial-profile analysis ( $R > 2 \sigma_{\text{off}} \sim 20\text{kpc/h}$ )**

- CLASH theoretical predictions (Meneghetti+CLASH 14)
  - Composite relaxed (70%) and unrelaxed (30%) clusters
  - Mean  $\langle c_{200c} \rangle = 3.9$ ,  $\sigma(c_{200c}) = 0.6$ ,  $c_{200c} = [3, 6]$

# Lensing Shear and Magnification



- **Shear**

*Sensitive to “modulated” matter density*

✓ Geometric shape dist:  $\delta e_+ \sim \gamma_+$

$$\Sigma_{\text{crit}} \gamma_+ = \Delta \Sigma(R) \equiv \Sigma(< R) - \Sigma(R)$$

- **Magnification**

*Sensitive to “total” matter density*

✓ Flux amplification:  $\mu F$

✓ Geometric area dist:  $\mu \Delta \Omega$

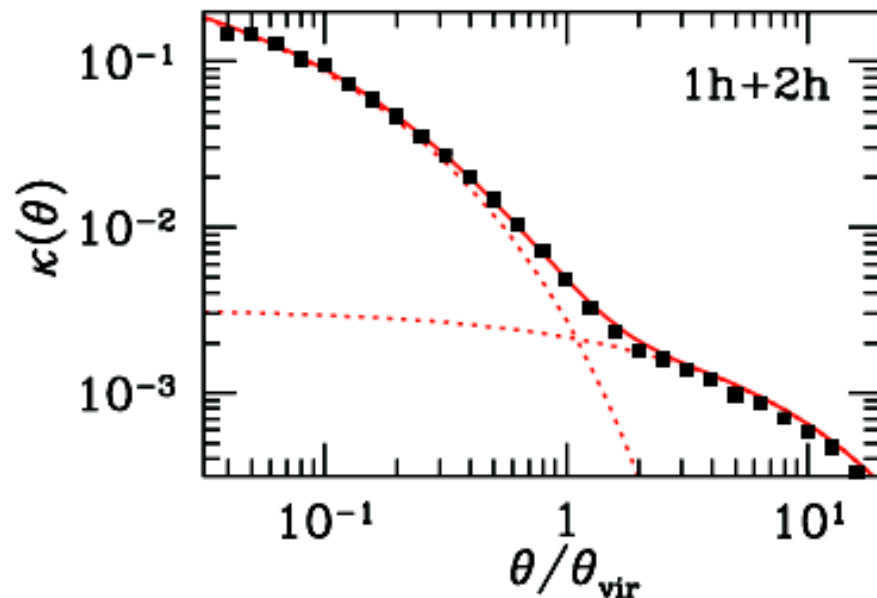
$$\mu \approx 1 + 2\kappa; \quad \Sigma_{\text{crit}} \kappa = \Sigma(R)$$

# Shear doesn't see mass sheet

Averaged lensing profiles in/around LCDM halos (Oguri+Hamana 11)

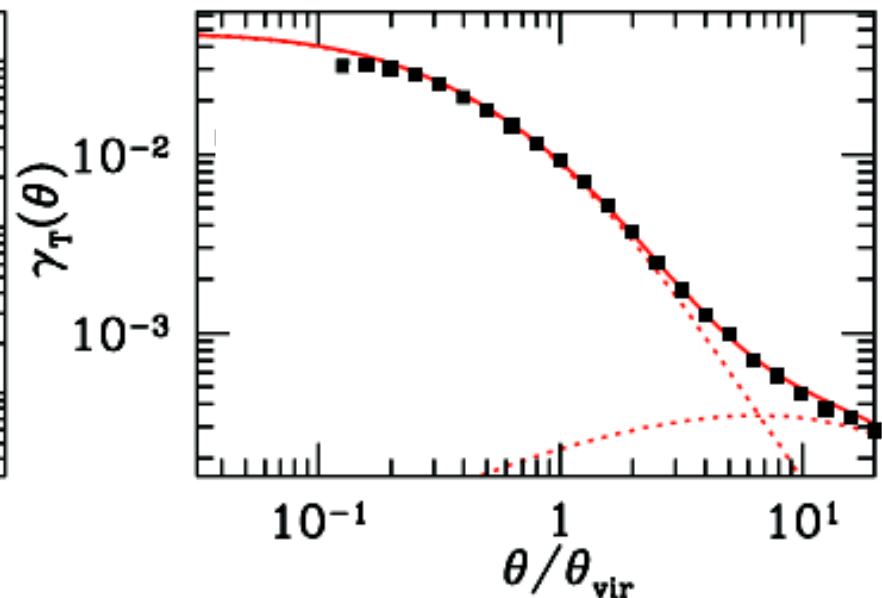
Total

$$\kappa = \Sigma(R) / \Sigma_{\text{crit}}$$



Modulated

$$\gamma_+ = \Delta\Sigma(R) / \Sigma_{\text{crit}}$$



- Tangential shear is a powerful probe of **1-halo term**, or **internal halo structure**.
- Shear alone cannot recover absolute mass, known as **mass-sheet degeneracy**



# CLASH-WL Results (1)

Ensemble-averaged internal halo structure:

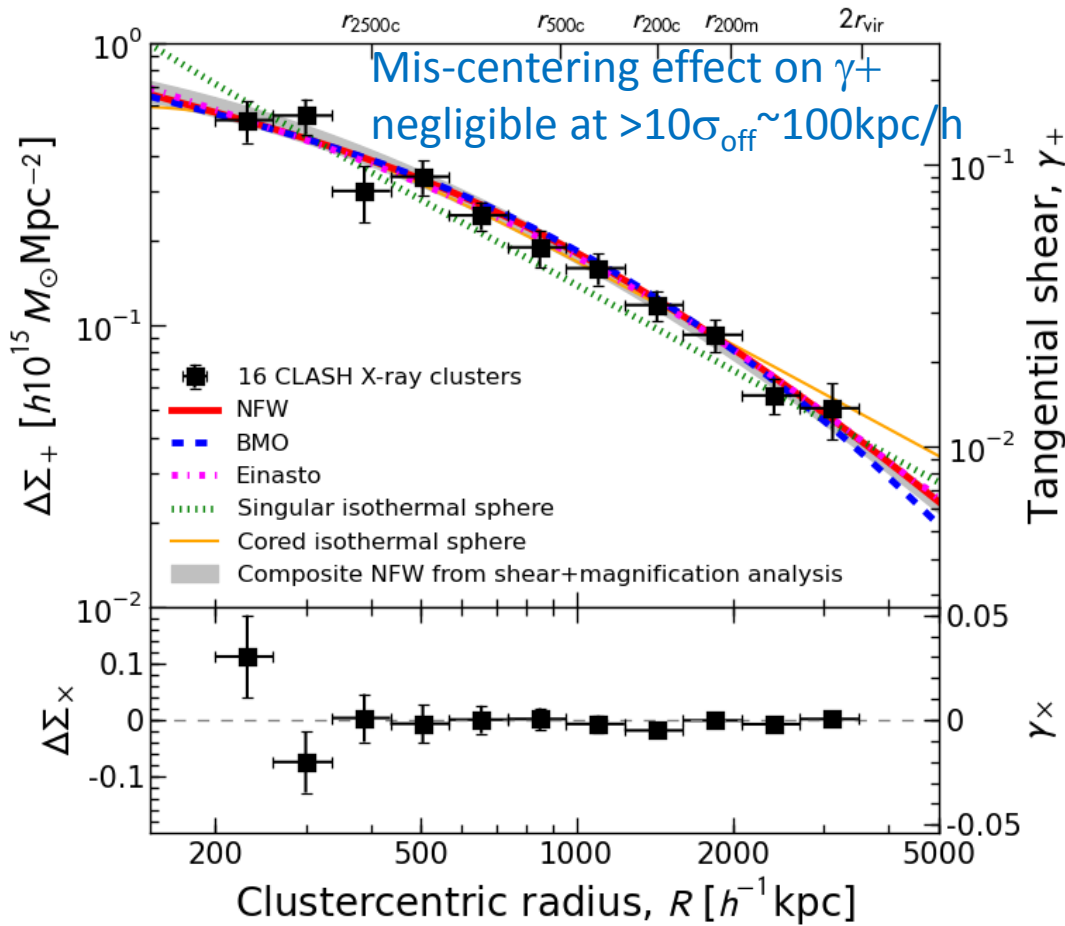
- Halo mass density profile,  $\langle \Delta \Sigma(R) \rangle$
- Degree of mass concentration,  $\langle c_{200} \rangle$

from ***stacked WL-shear-only*** analysis of CLASH  
X-ray-selected sample (**16 clusters**)

Umetsu, Medezinski, Nonino+CLASH 14, arXiv:1404.1375



# Stacked halo density profile $\Delta\Sigma(R)$



Stacked shear-only analysis provides a net 1-halo-only constraint ( $\gamma_{+,2h} < 1e-3$ )

NFW an excellent fit (PTE = 0.66)

- $M_{200c} = (1.3 \pm 0.1) 10^{15} M_{\text{sun}}$
- $c_{200c} = 4.01 (+0.35, -0.32)$  at  $\langle z \rangle = 0.35$
- $b_h = 9 \pm 2$  (WMAP7+Tinker10)

Corresponding to  $\theta_{\text{Ein}} = (15'' \pm 4'')$  at  $z_s = 2$ , consistent w SL analysis,  $\langle \theta_{\text{Ein}} \rangle \sim 20''$  (Zitrin+14, in prep)

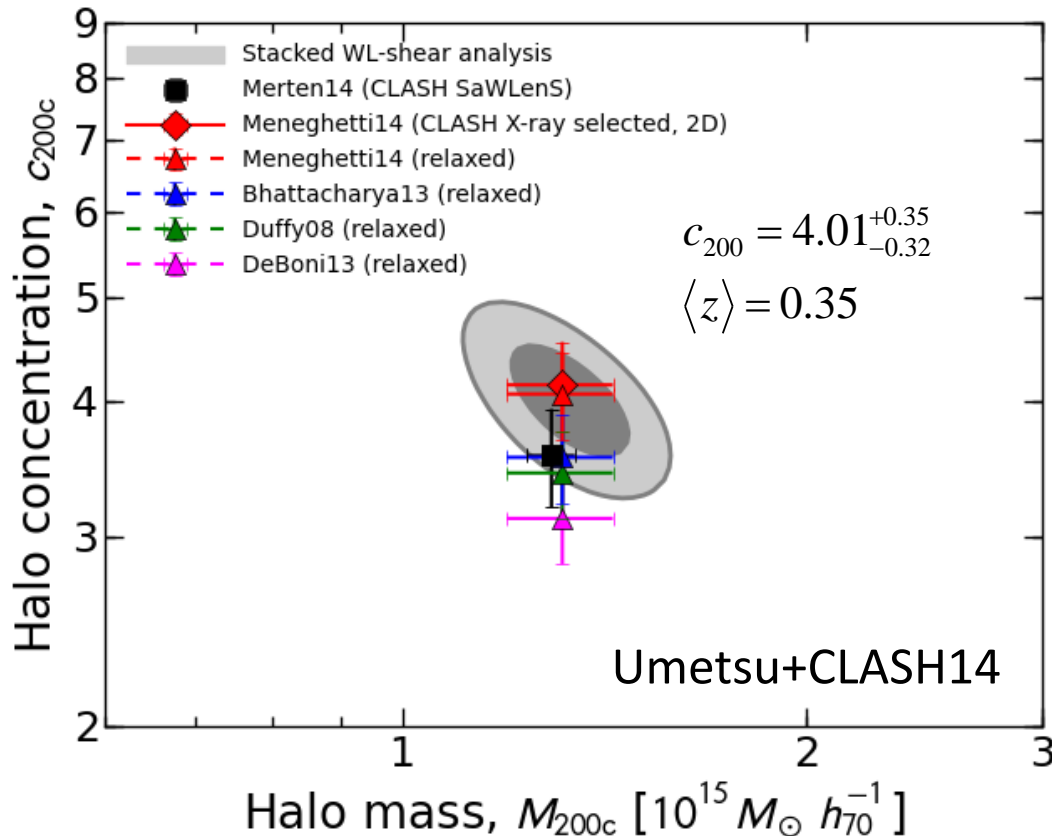
Consistent w a family of density profiles for collisionless DM halos (NFW, variants of NFW, Einasto)



# Integrated constraints on $c(M_{200c}, z)$

**Theoretical predictions  
for stacked  $c(M, z)$**

$$\langle c \rangle = \frac{\int dM \int dz N(M, z) \hat{c}(M, z)}{\int dM \int dz N(M, z)} \approx \frac{\sum_n \text{tr}(W_n) \hat{c}(M_n, z_n)}{\sum_n \text{tr}(W_n)}$$



**Variance in theory due to different cosmology and mass resolution**

M14 (MUSIC-2):  $\sigma_8 = 0.82$

Bhat13:  $\sigma_8 = 0.8$

Duffy08:  $\sigma_8 = 0.8$

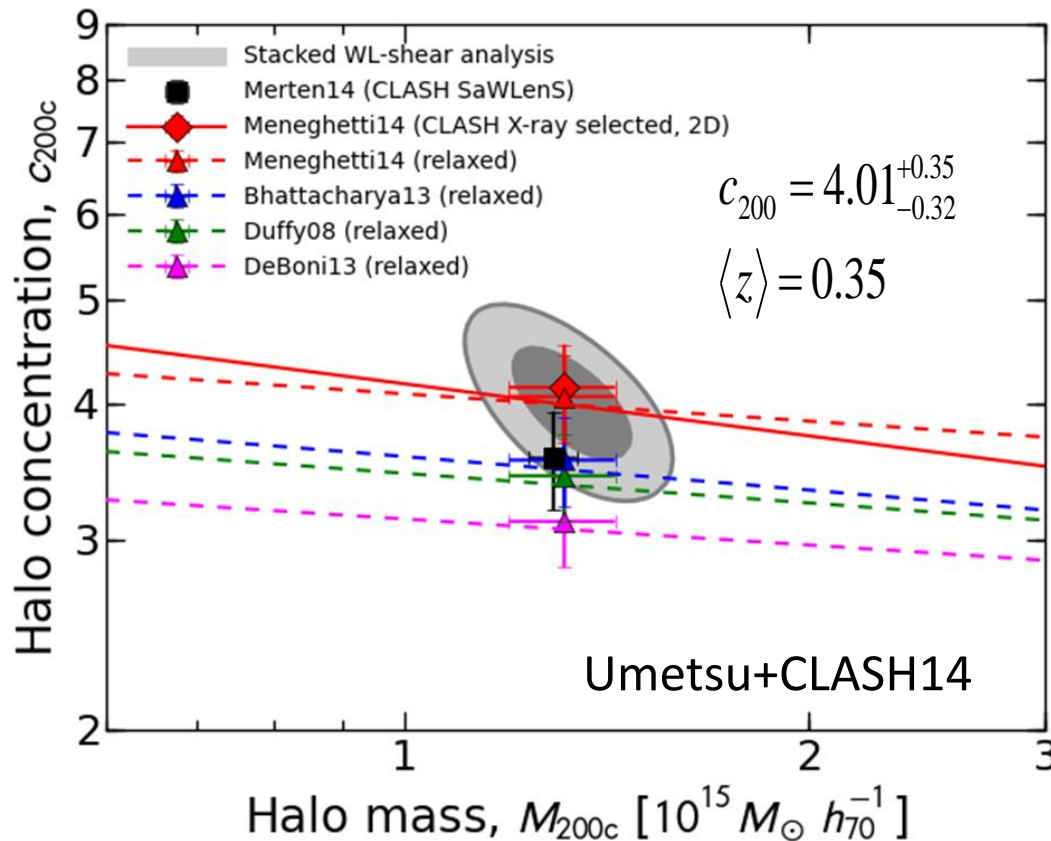
DeBoni13:  $\sigma_8 = 0.78$

- Excellent agreement w CLASH predictions (M14),  $c_{200c} \sim 4$
- Consistent w Bhatt13, Duffy08 (relaxed) predictions at  $1\sigma$ ,  $c_{200c} \sim 3.6$





# CLASH-WL vs. c-M relations



M14 (MUSIC-2):  $\sigma_8=0.82$

Bhat13:  $\sigma_8=0.8$

Duffy08:  $\sigma_8=0.8$

DeBoni13:  $\sigma_8=0.78$

At low  $M_{200}$ , X-ray selection picks up clusters with higher concentrations (Meneghetti+14)



# CLASH-WL Results (2)

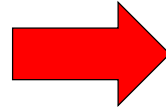
- Individual mass profile reconstruction of 20 CLASH clusters from joint Shear+Magnification analysis (**16 X-ray + 4 lensing clusters**)

Umetsu, Medezinski, Nonino+CLASH 14, arXiv:1404.1375

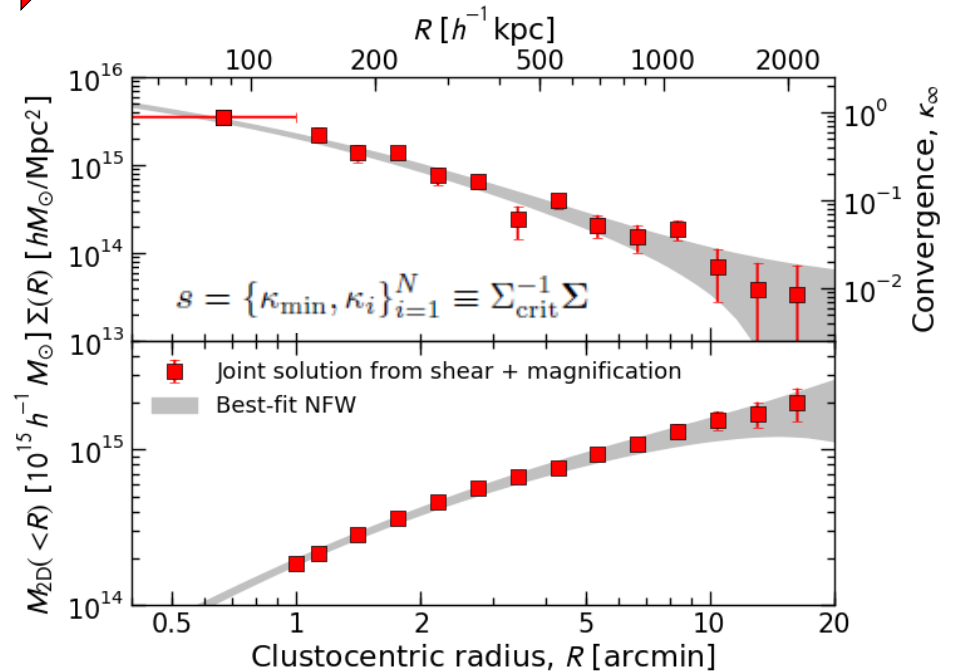
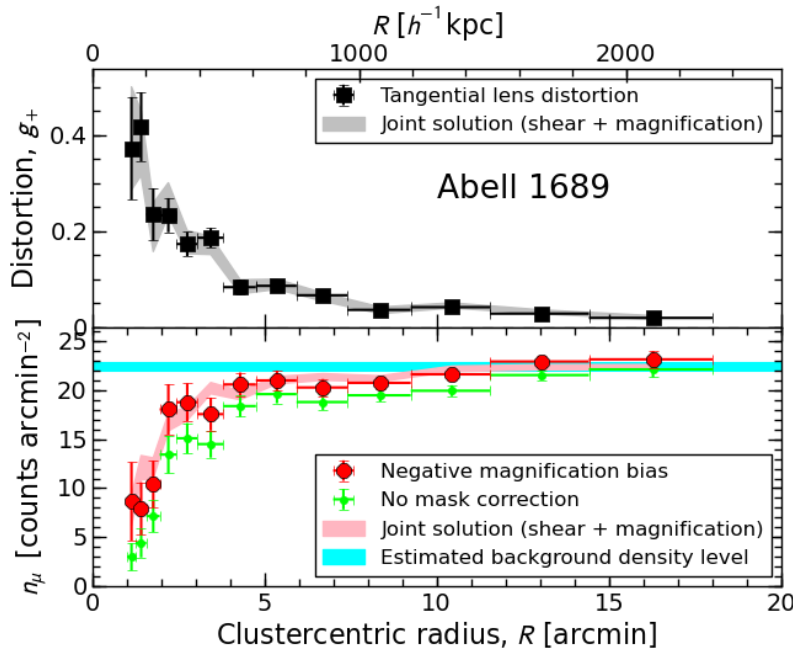
# Method: Combining Shear & Magnification

**Bayesian joint-likelihood approach** (Umetsu+11a; Umetsu 13)

Shear + magnification



Non-parametric  $\Sigma(R)$  solution



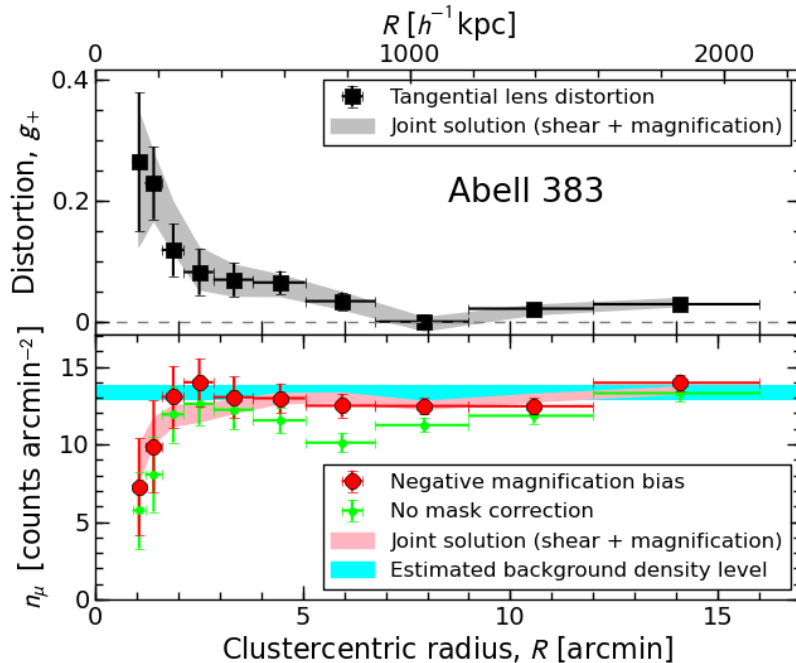
- Mass-sheet degeneracy broken
- Total statistical precision improved by  $\sim 20\text{-}30\%$
- Calibration uncertainties marginalized over:  $c = \{\langle W \rangle_s, f_{W,s}, \langle W \rangle_\mu, \bar{n}_\mu, s_{\text{eff}}\}$ .



# CLASH-WL: Joint Shear + Magnification Analysis

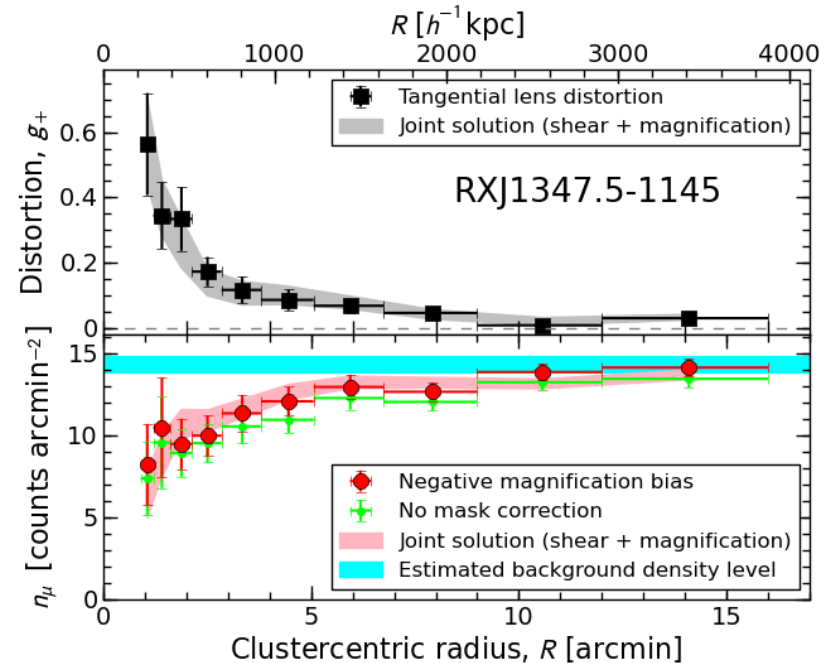
## CLASH low mass

$M_{200c} = 6e14 M_{\text{sun}}/h$  ( $z=0.19$ )



## CLASH high mass

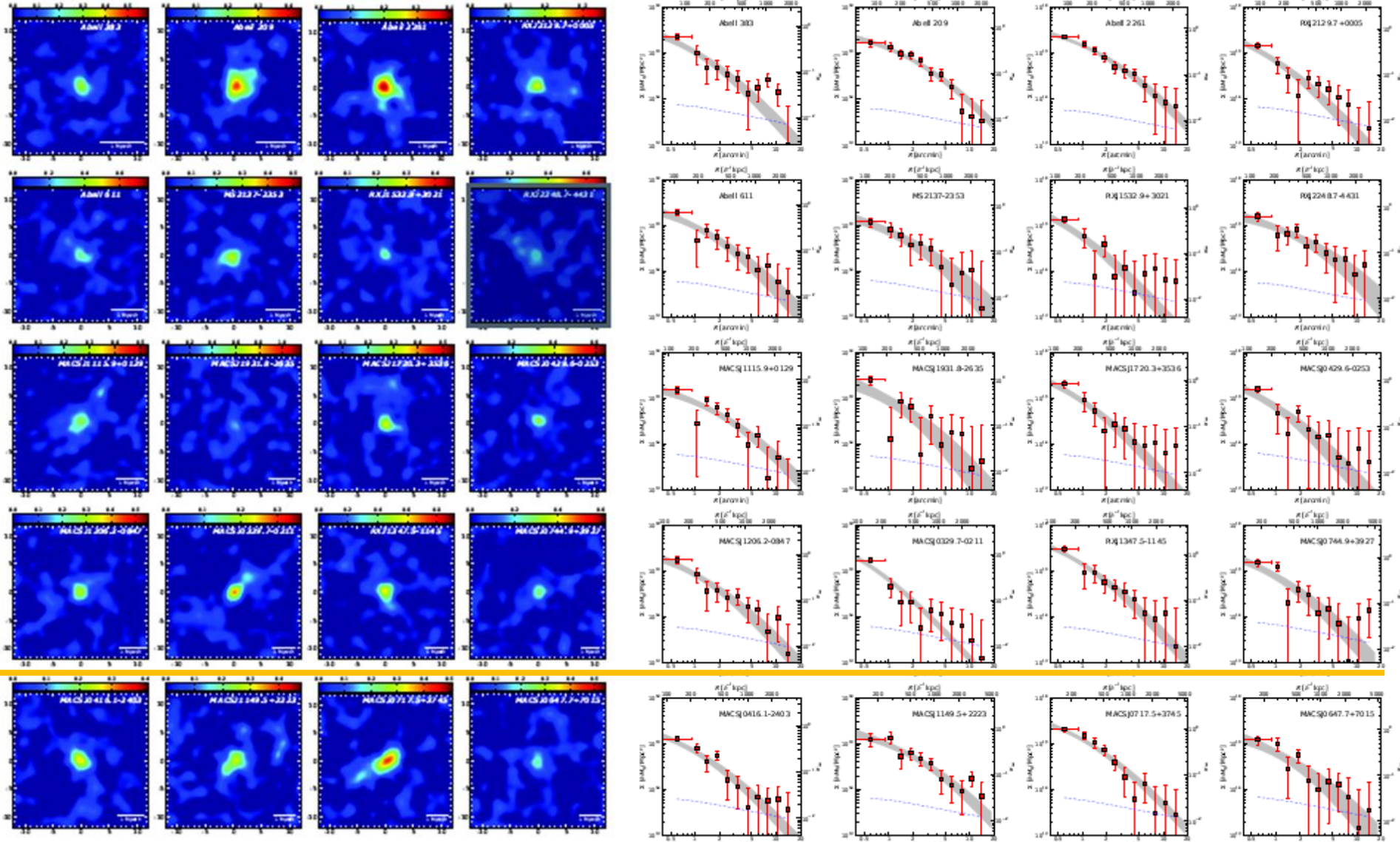
$M_{200c} = 20e14 M_{\text{sun}}/h$  ( $z=0.45$ )



Shear-magnification consistency:  $\langle \chi^2/\text{dof} \rangle = 0.92$  for 20 CLASH clusters

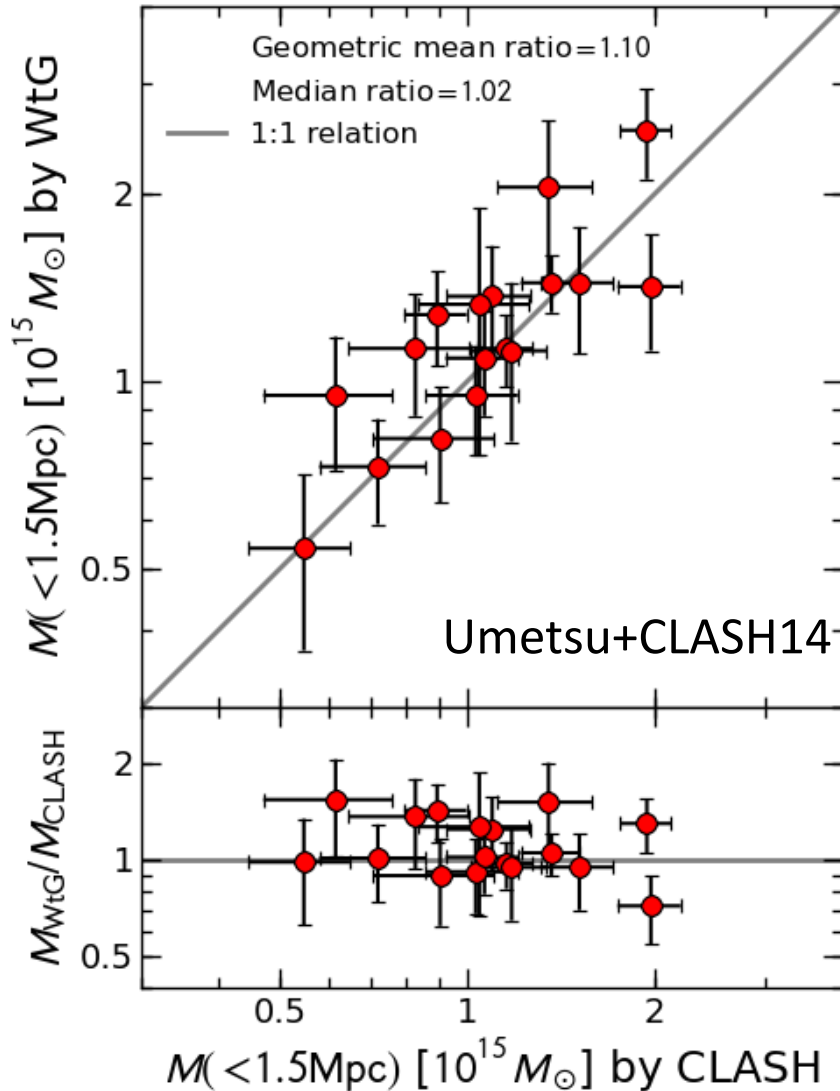


# Mass Density Profile Dataset





# Comparison with WtG @R=1.5Mpc



17 clusters in common (Subaru):

- **WtG**: shear-only (Applegate+14), NFW  $c_{200c}=4$  prior
- **CLASH**: shear + magnification, NFW log-uniform:  $0.1 < c_{200c} < 10$

**Un-weighted geometric mean mass ratio ( $\langle Y/X \rangle = 1/\langle X/Y \rangle$ )**

- $\langle M_{\text{WtG}}/M_{\text{CLASH}} \rangle = 1.10$
- Median ratio = 1.02

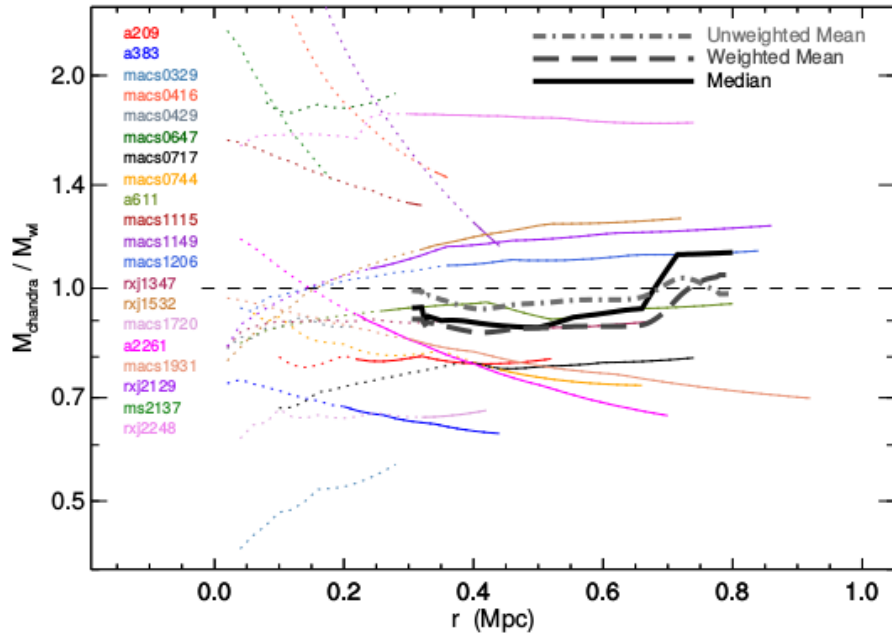
Systematic uncertainty in the overall mass calibration of 8% from shear-magnification consistency (Umetsu+14)

No mass dependent bias  
No tension

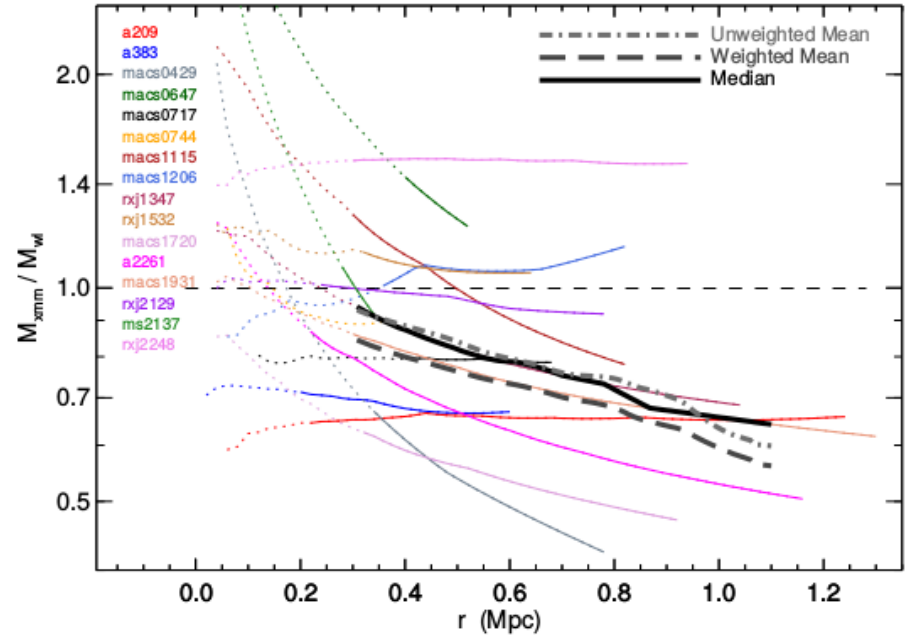


# CLASH Comparisons with X-ray masses

## Chandra HSE / Subaru-WL



## XMM HSE / Subaru-WL



### X-ray to WL comparison at R=0.5Mpc

- bias =  $1 - \langle M_{\text{chandra}} / M_{\text{wl}} \rangle = 0.05 \pm 0.07$  (11 clusters)
- bias =  $1 - \langle M_{\text{xmm}} / M_{\text{wl}} \rangle = 0.16 \pm 0.06$  (14 clusters)

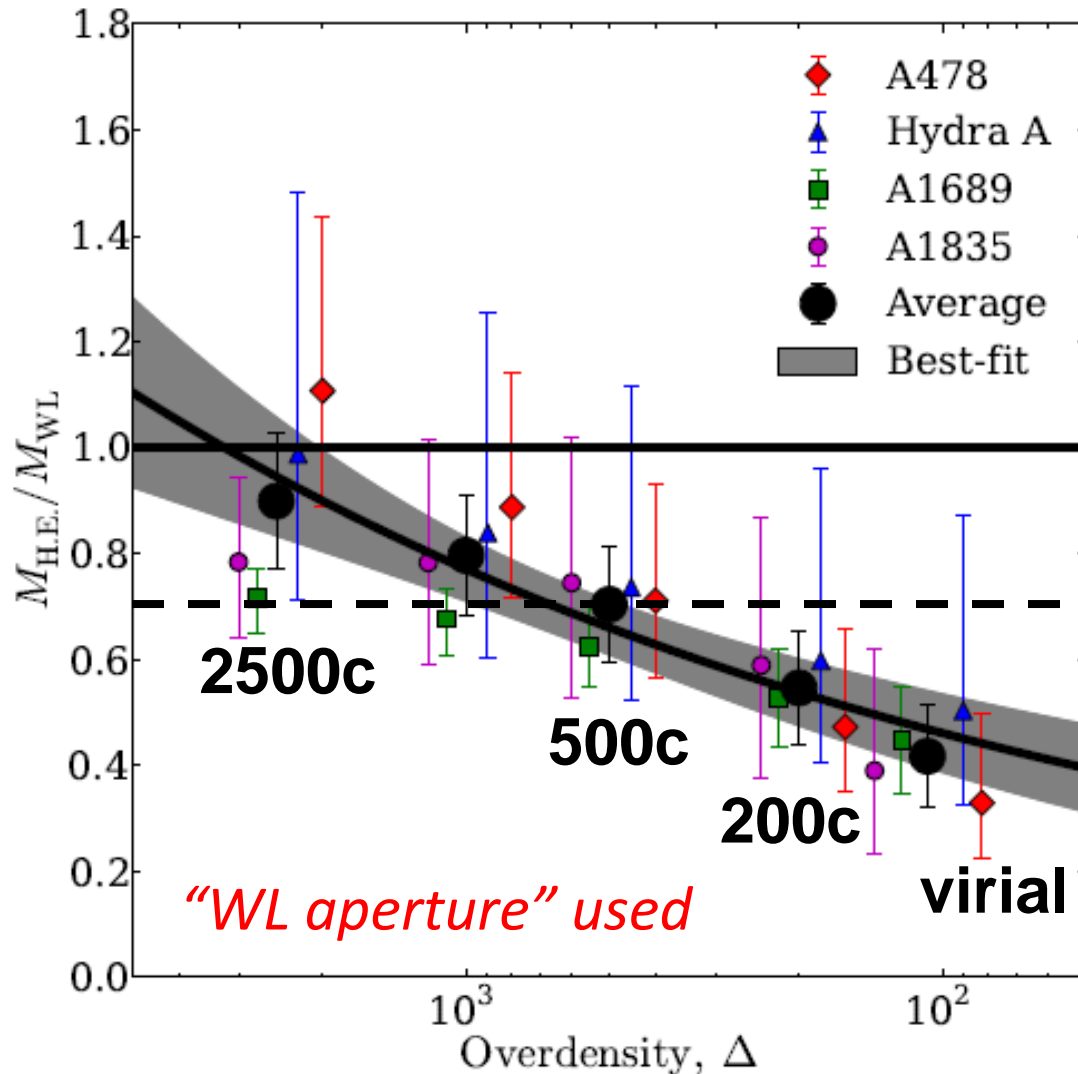
*Un-weighted means quoted*

### X-ray to WL comparison at $r_{500}$ [no aperture correction]

- bias =  $1 - \langle M_{\text{chandra}} / M_{\text{wl}} \rangle = 0.09 \pm 0.12$  (20 clusters)
- bias =  $1 - \langle M_{\text{xmm}} / M_{\text{wl}} \rangle = 0.41 \pm 0.07$  (16 clusters)

Donahue+CLASH 14  
(arXiv:1405.7876)

# Suzaku-X HSE vs. Subaru WL



Independent *Suzaku*-HSE vs. Subaru-WL results, consistent with XMM-HSE vs. Subaru-WL of CLASH collaboration

Okabe, Umetsu, ..  
Matsushita+14  
(arXiv:1406.3451)





# Shear + Magnification + “Zitrin-SL”

Total mass density profile

$$\Sigma(R) = \Sigma_{1h}(R) + \Sigma_{2h}(R)$$

around the CLASH “X-ray-selected” sample

Clustering of matter  
around halos with  $M$ :

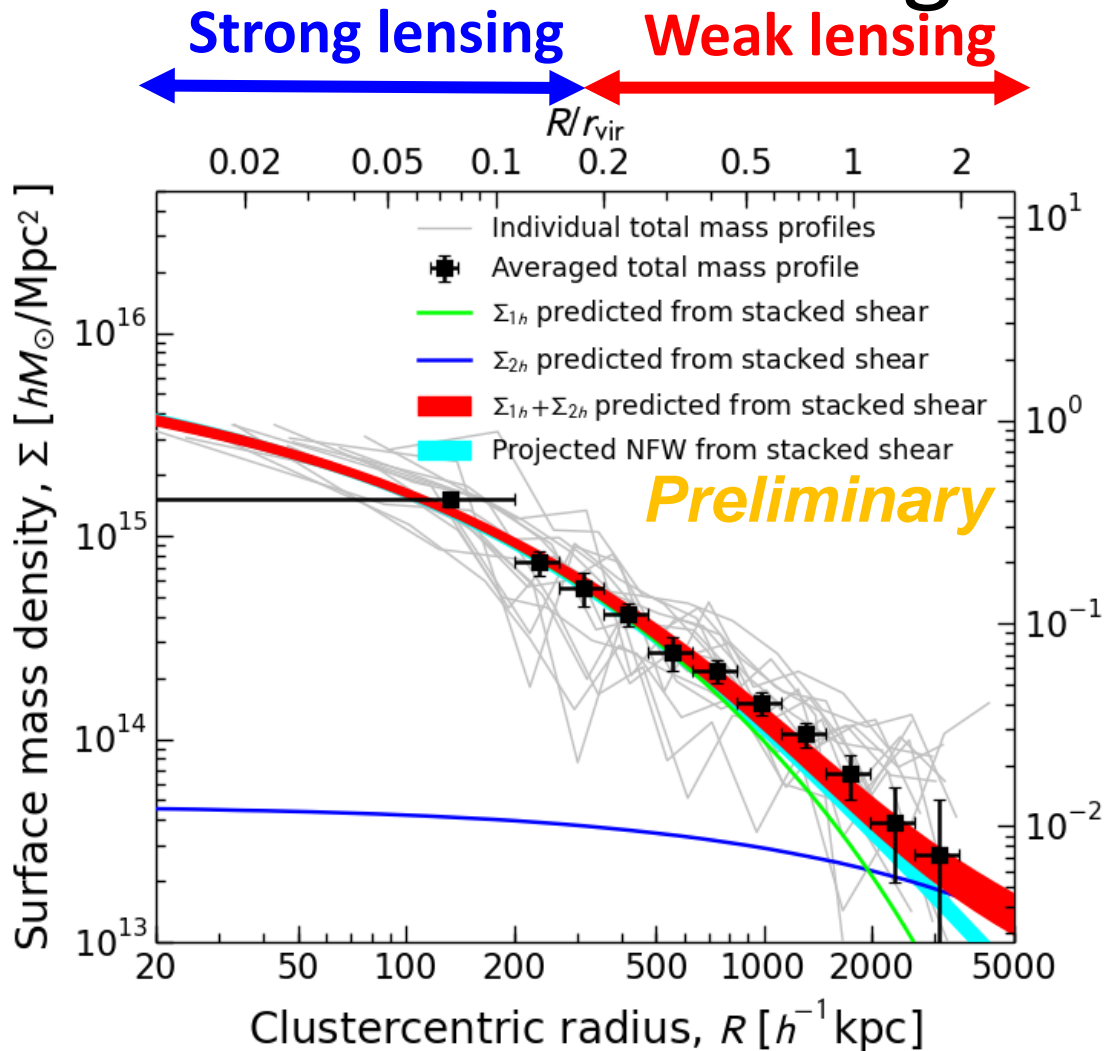
$$\xi_{hm}(r | M) = \frac{\langle \rho_{1h}(r | M) \rangle}{\bar{\rho}} + b_h(M) \xi_{mm}(r)$$

**1h term**

**2h term**



# Averaged cluster (1h) + LSS (2h) from WL shear + magnification + SL



Adding *HST* SL tightly  
constrains the inner density  
profile ( $R < 100 \text{ kpc}/h$ )

Inner mass profiles from SL  
follow 1h prediction from  
outer WL-shear information

Recovered mass-sheet (LSS),  
consistent w the shear-based  
halo model prediction,  $b_h = 9$   
 $\pm 2$  (WMAP7+Tinker10)



# CLASH-WL Summary

- Ensemble-averaged halo structure  $\Delta\Sigma$  (1h) of X-ray-regular CLASH clusters is consistent with a family of standard (collisionless) DM predictions:
  - $M_{200c} = (1.3 \pm 0.1) 10^{15} M_{\text{sun}}, \langle z \rangle = 0.35$
  - NFW (PTE=0.66):  $c_{200c} = 4.01 (+0.35, -0.32)$
  - Einasto (PTE=0.51): degree of curvature,  $\alpha_E = 0.19 \pm 0.07$
- The stacked-mean concentration agrees with:
  - theoretical expectation,  $\langle c_{200c} \rangle \sim 3.9$ , which takes into account CLASH selection function and projection effects (Meneghetti+14)
  - Measured effective Einstein radius,  $\langle \theta_{\text{Ein}} \rangle = 20''$  ( $z_s = 2$ ), from independent HST-SL analysis (Zitrin+CLASH 14, in prep)



# CLASH-WL Summary (contd.)

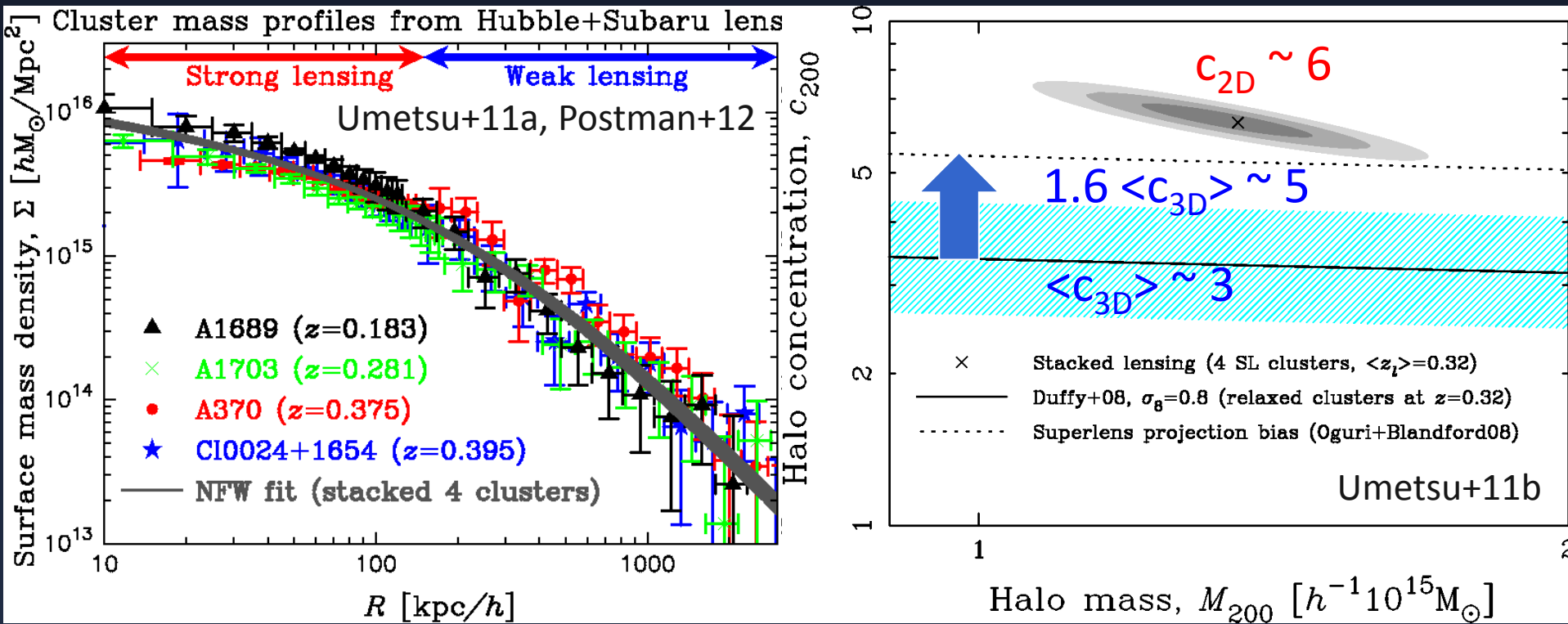
- Consistent geometric shear vs. magnification measurements allow for accurate cluster mass profile measurements for 20 CLASH clusters with  $\pm 8\%$  systematic mass-calibration uncertainty.
- Total matter distribution  $\Sigma$  (1h+2h) recovered from full-lensing analysis (SL + shear + magnification) is consistent with shear-based halo model predictions ( $b_h = 9 \pm 2$  at  $M_{200} = 1.3e15 M_{\text{sun}}$ ,  $z = 0.35$ ), establishing further consistency in the context of LCDM.

# Supplemental Slides



# CLASH Motivation

Before CLASH, deep-multicolor Strong (*HST*) + Weak (Subaru) lensing data only available for a handful of strong-lens clusters ( $\theta_E > 30''$ ,  $z_s=2$ )

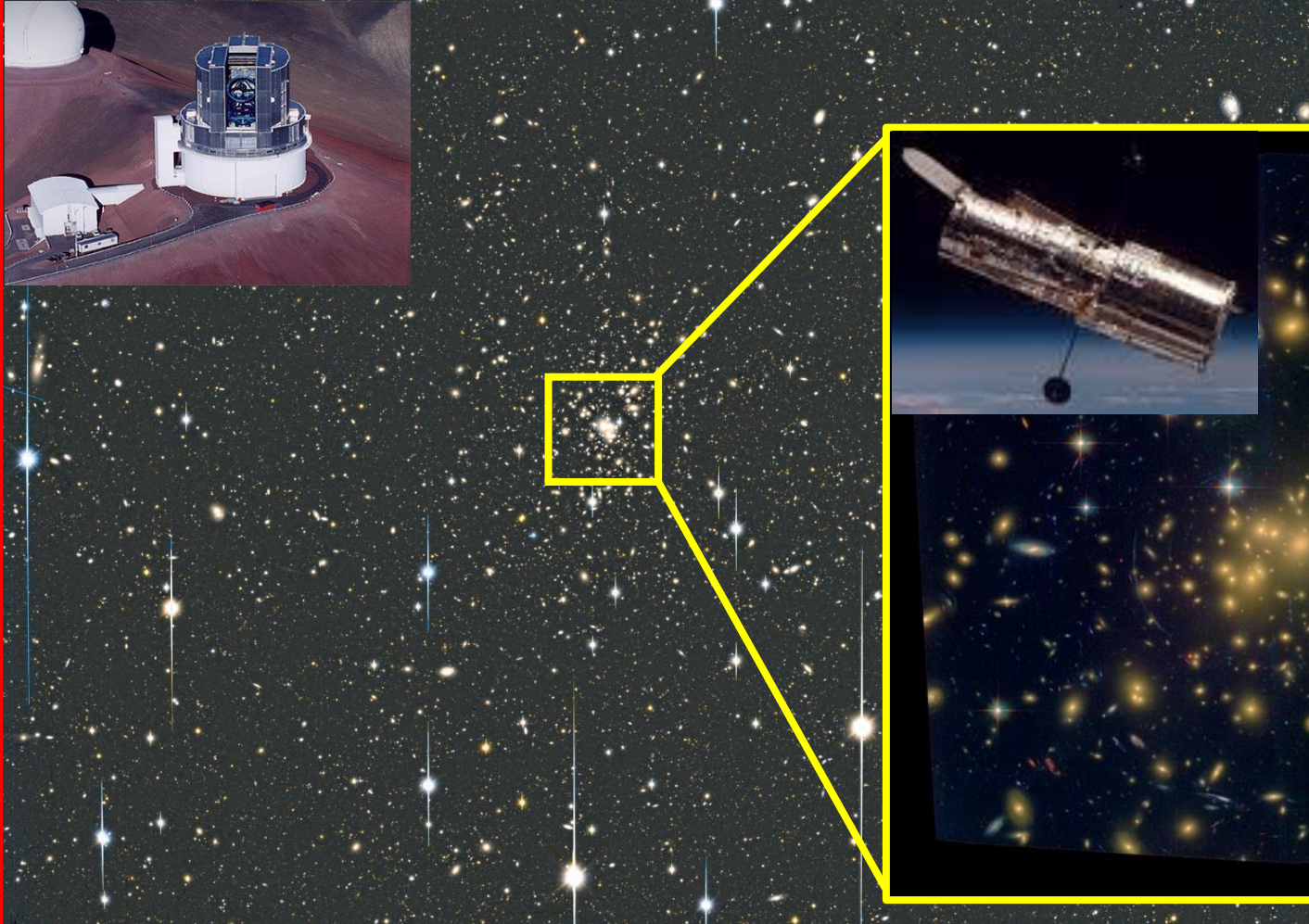


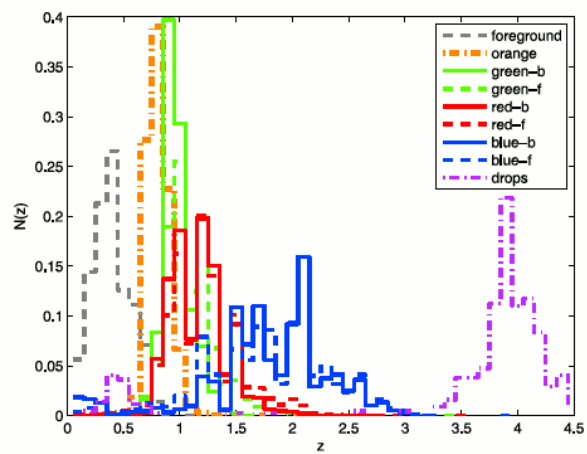
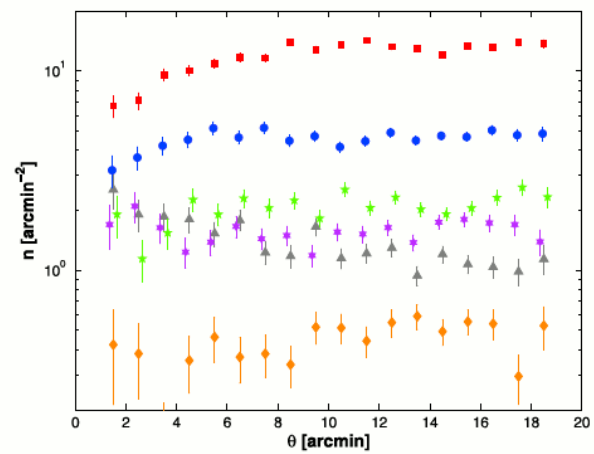
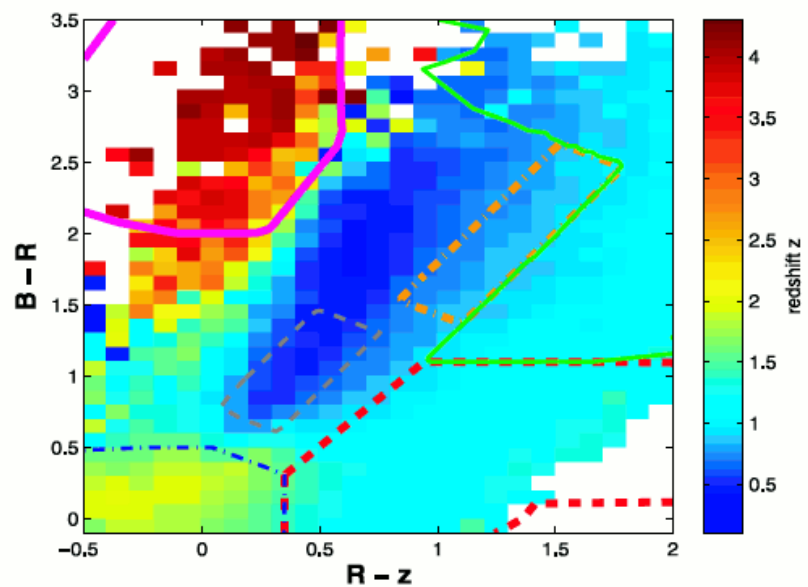
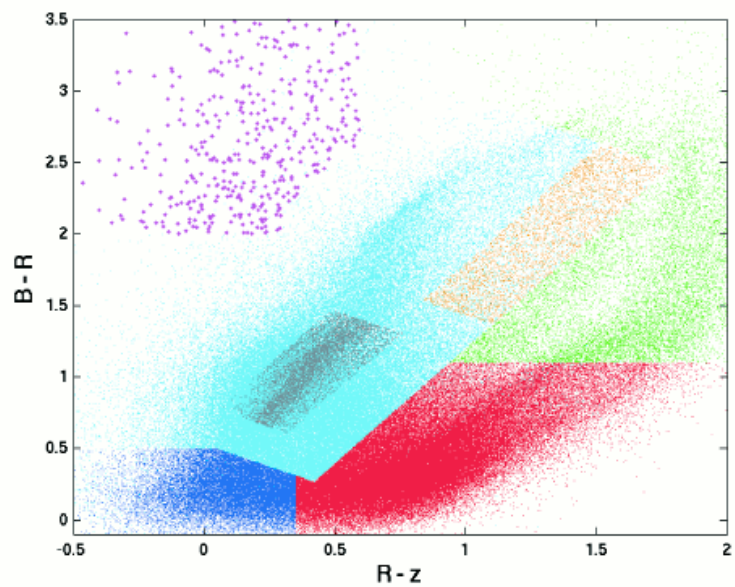
**Total mass profile shape:** consistent w self-similar NFW (cf. Newman+13; Okabe+13)

**Over concentration?:** maximum superlens correction (<60%) not enough if  $\langle c_{\text{LCDM}} \rangle \sim 3$ ?

***SUBARU* multi-color maging for wide-field weak lensing**

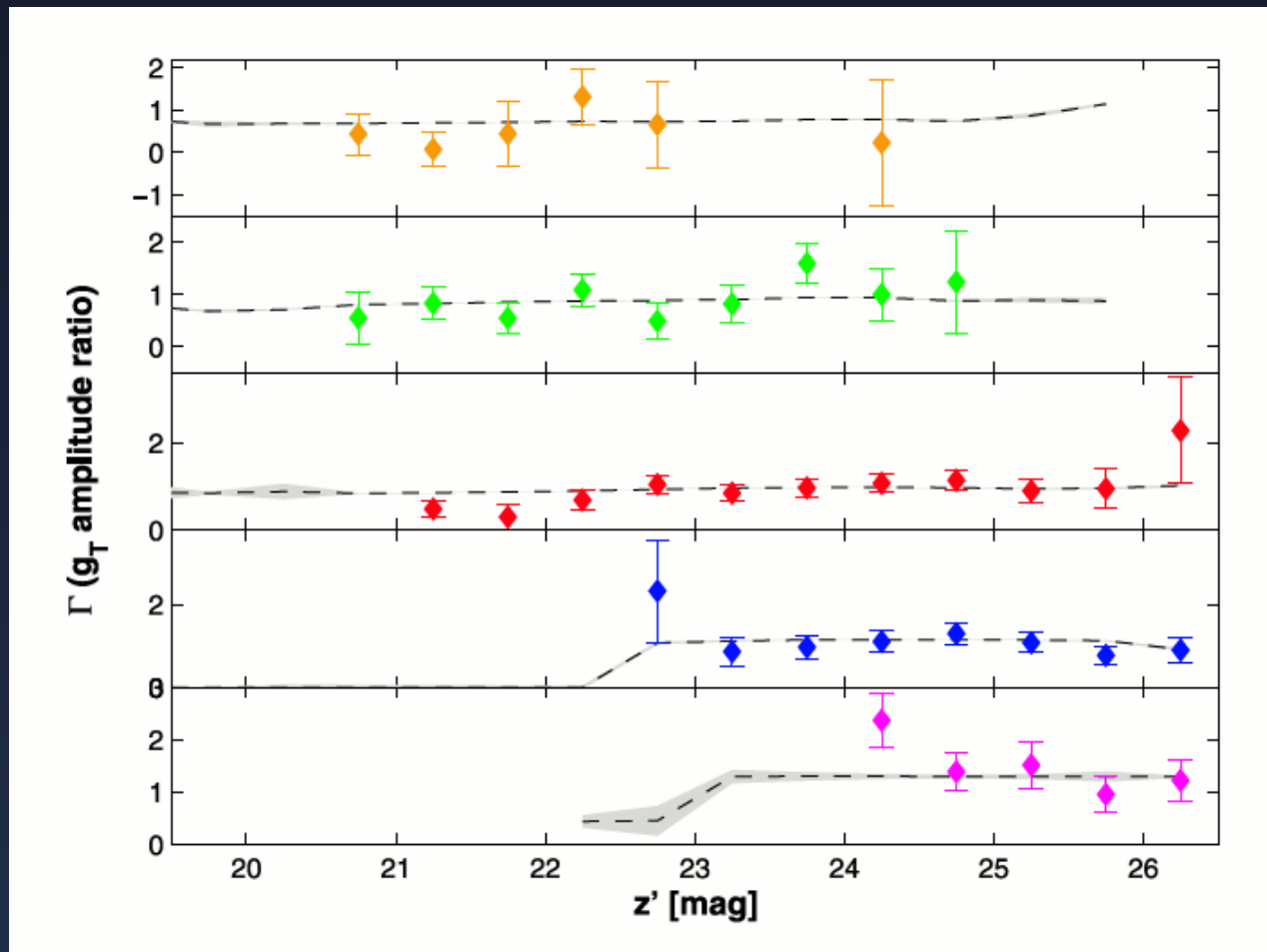
**High-resolution space imaging with *Hubble* for strong lensing**







# SUBARU shear strength as a function of magnitude

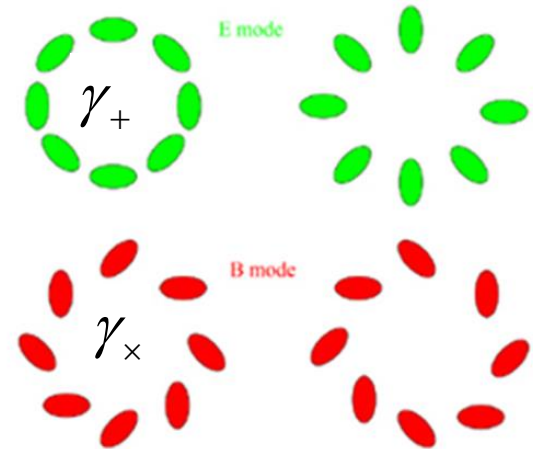


# Tangential Shear

Azimuthally-averaged tangential coherence of elliptical distortions around a given point (Kaiser 95):

$$\gamma_+(R) = \Delta\Sigma(R) / \Sigma_{\text{crit}}$$

$$\gamma_\times(R) = 0$$



$\Delta\Sigma(R)$  is the *radially-modulated surface mass density*:

$$\Delta\Sigma(R) = \Sigma(< R) - \Sigma(R)$$

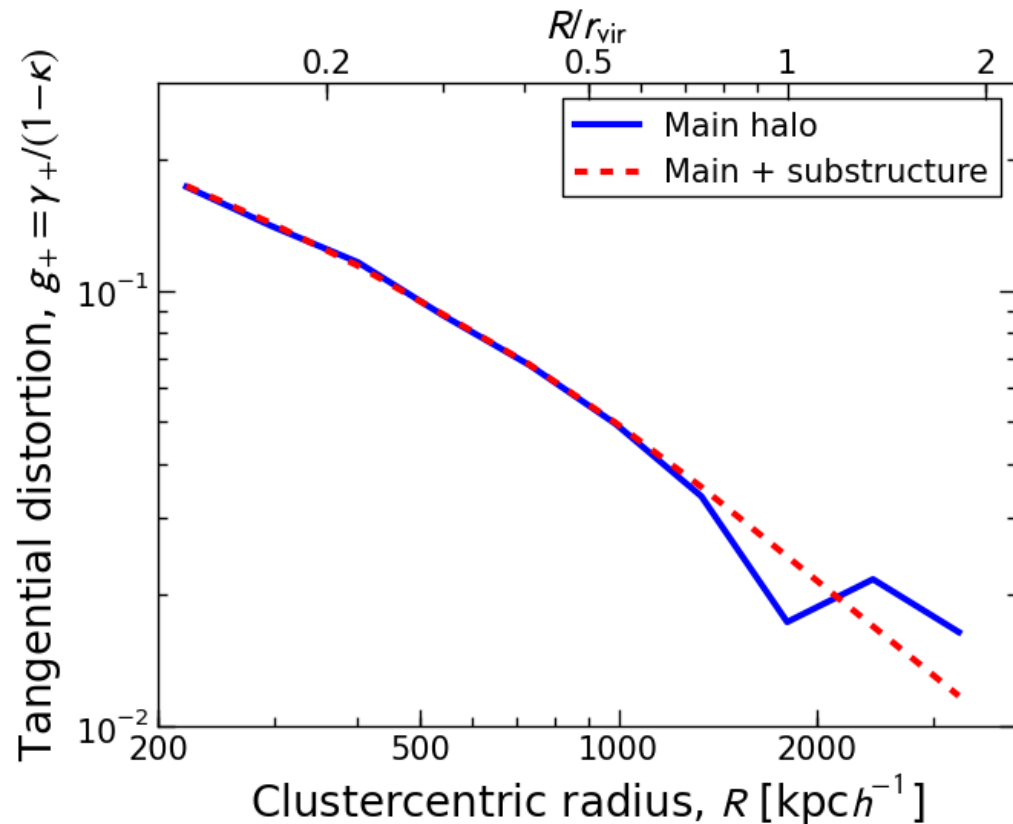
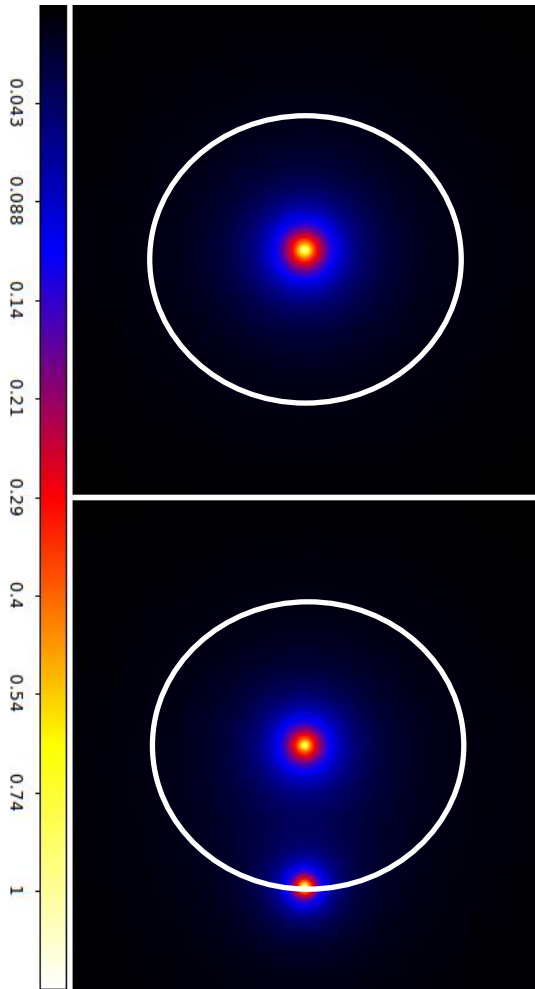
Sensitive to interior mass

$$\Sigma = \int dl \delta\rho$$

$\Sigma_{\text{crit}}(z_l, z_s)$  is the *critical surface mass density of lensing*

# Non-local substructure effect

A substructure at  $R \sim r_{\text{vir}}$  of the main halo, modulating  $\Delta\Sigma(R) = \Sigma(< R) - \Sigma(R)$



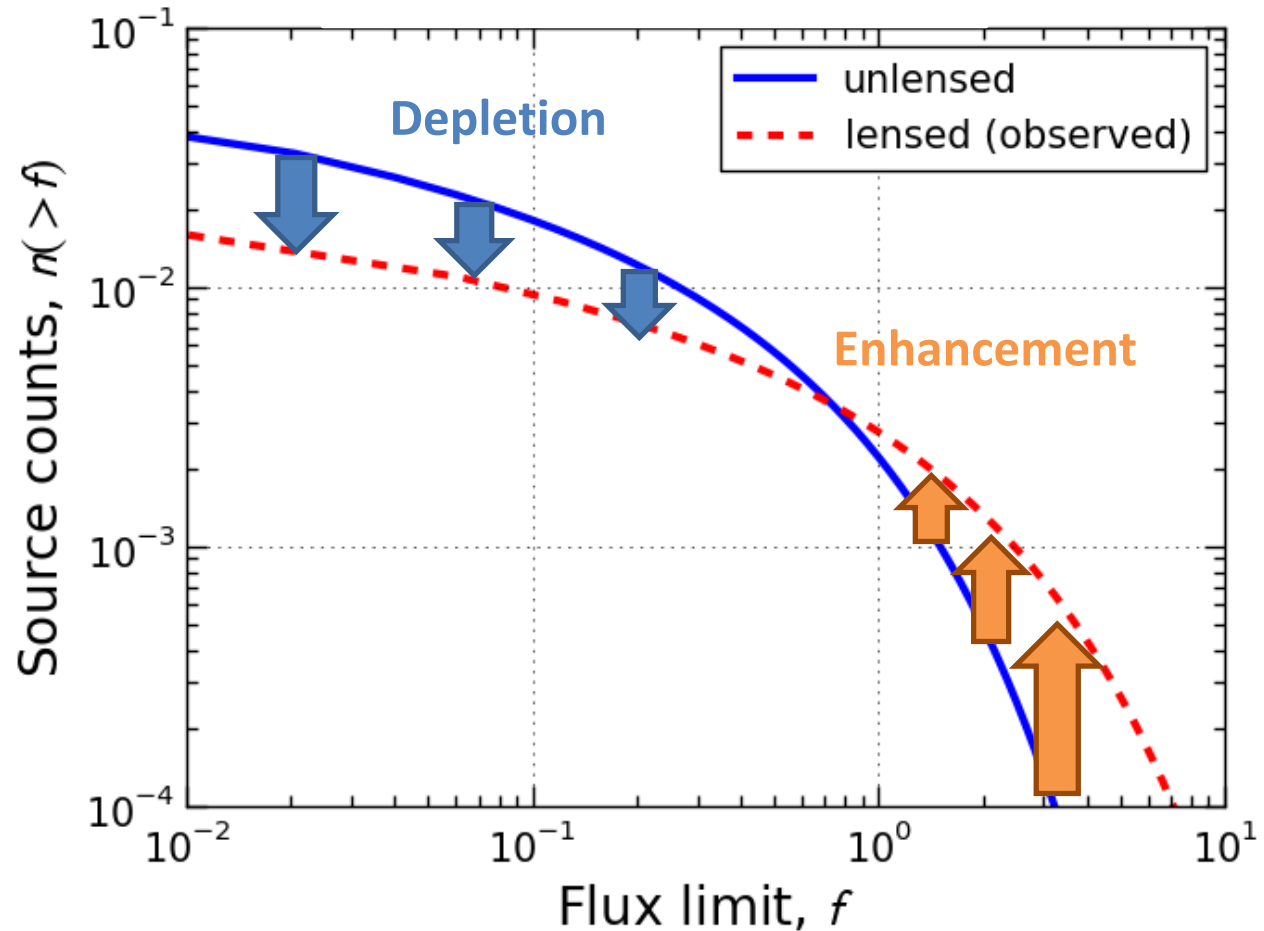
Known  $\sim 10\%$  negative bias in mass estimates from tangential-shear fitting, inherent to clusters sitting in substructured field (Rasia+12)

# Magnification bias effects

Flux-limited  
source counts:

$$n_{\text{obs}}(> f) = \mu^{-1} n(> \mu^{-1} f)$$

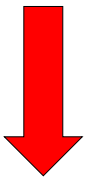
Broadhurst, Taylor &  
Peacock 95



Flux amplification

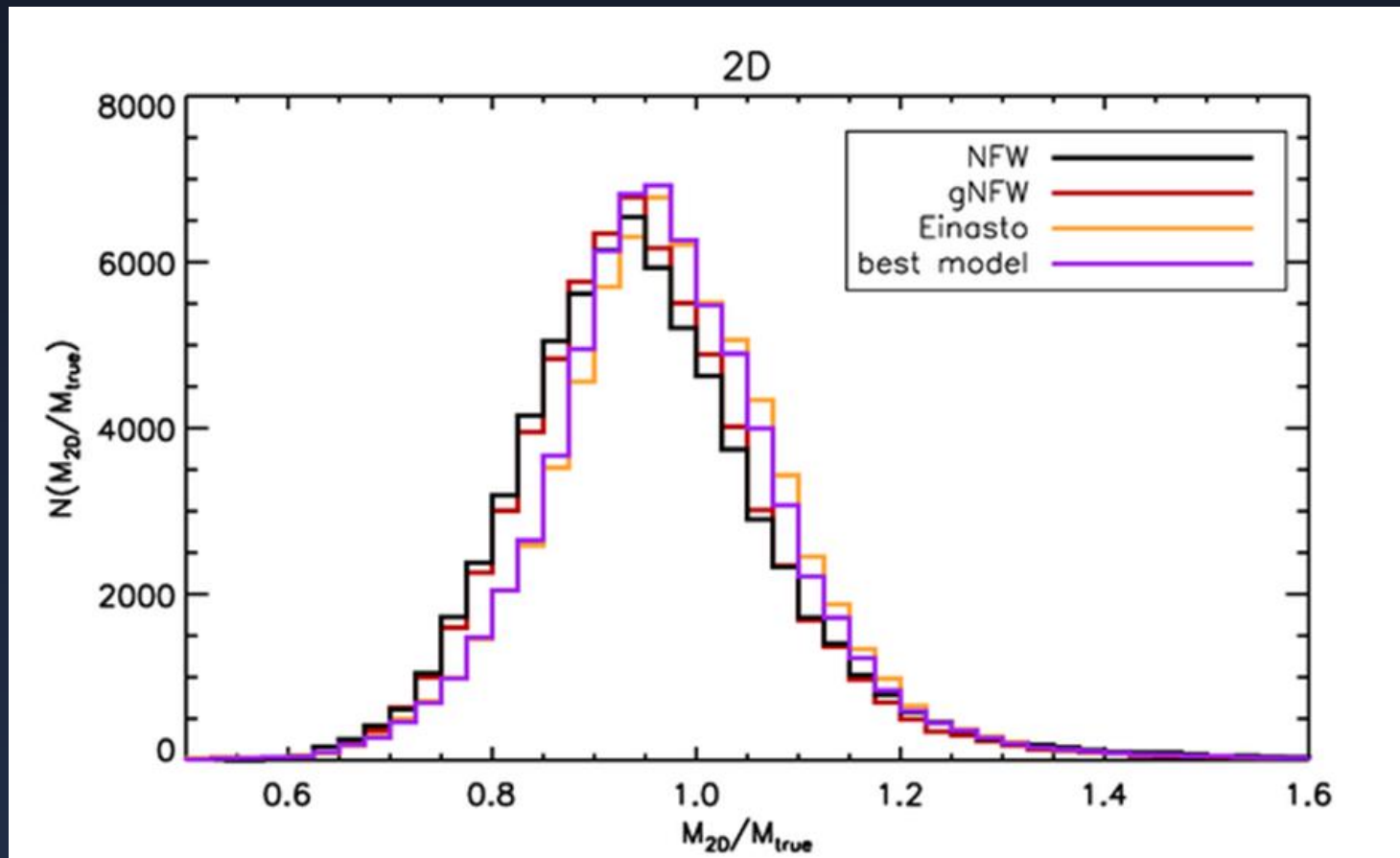


Geometric area  
distortion



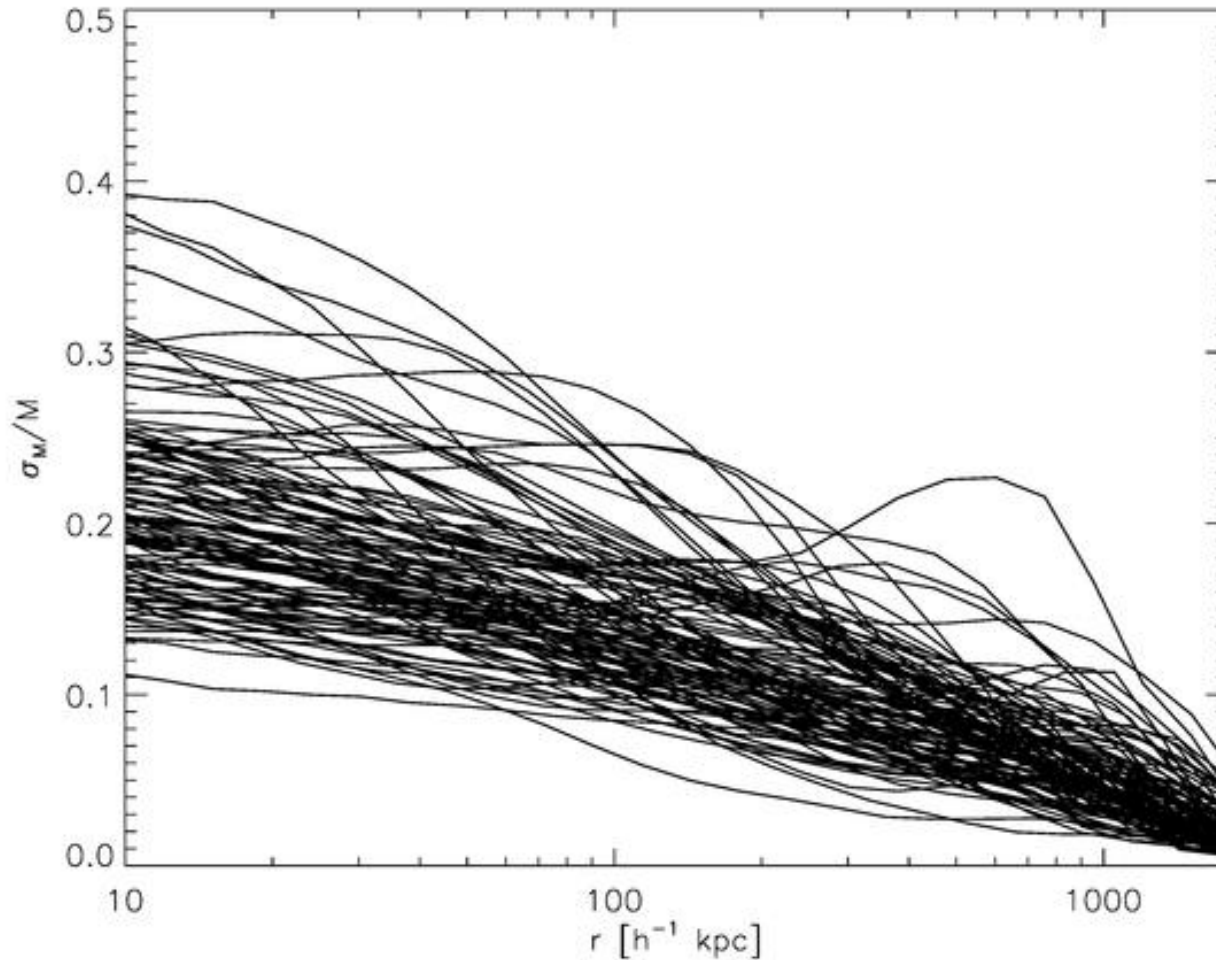
$n/\mu$

# Cluster masses recovered from lensing analysis





# Scatter in $M_{2D}(R)$ by halo triaxiality



MUSIC-2 simulation by Massimo



# Ensemble-averaged DM halo (1h) density profile

Stacking of weak-lensing signals by weighting individual clusters according to the sensitivity kernel matrix:

$$\langle\langle \widehat{\Delta\Sigma}_+ \rangle\rangle = \left( \sum_n \mathcal{W}_{+n} \right)^{-1} \left( \sum_n \mathcal{W}_{+n} \widehat{\Delta\Sigma}_{+n} \right),$$

with the individual sensitivity matrix

$$(\mathcal{W}_{+n})_{ij} \equiv \Sigma_{c,n}^{-2} (C_{+n}^{-1})_{ij}$$

defined with the total covariance matrix

$$C_+ = C_+^{\text{stat}} + C_+^{\text{sys}} + C_+^{\text{lss}}.$$

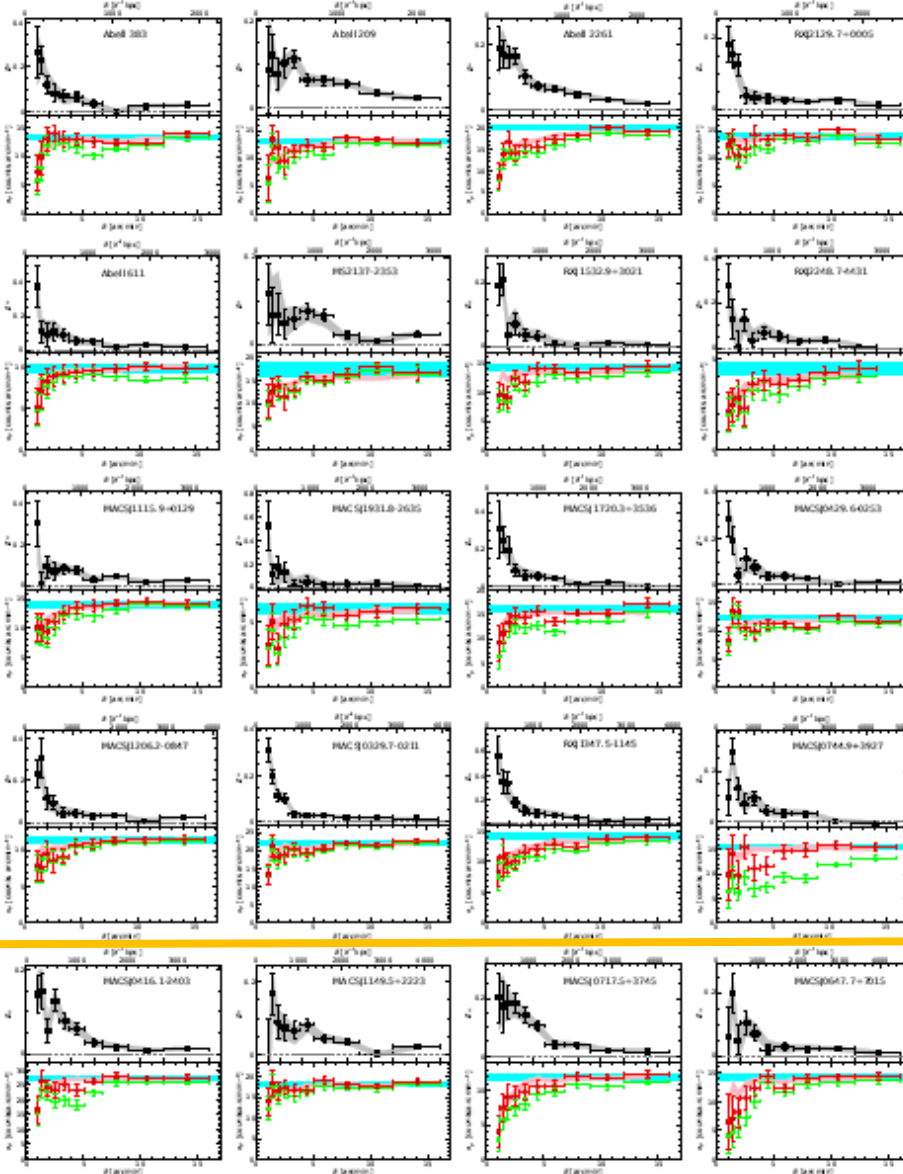
**With “trace-approximation”, averaging is interpreted as**

$$\langle\langle \Sigma_c^{-1} \rangle\rangle = \frac{\sum_n \text{tr}(\mathcal{W}_{+n}) \Sigma_{c,n}^{-1}}{\sum_n \text{tr}(\mathcal{W}_{+n})},$$

Umetsu+CLASH 14,  
arXiv:1404.1375



# 20 CLASH clusters in Umetsu+14



## 16 X-ray-selected clusters

- 15 clusters from 8.3m Subaru Telescope
- 1 southernmost cluster (RXJ2248) from 2.2m ESO/MPG
- $0.18 < z < 0.69$

**$\langle \chi^2/\text{dof} \rangle = 0.92$  for 20 CLASH clusters**

## 4 high-magnification clusters

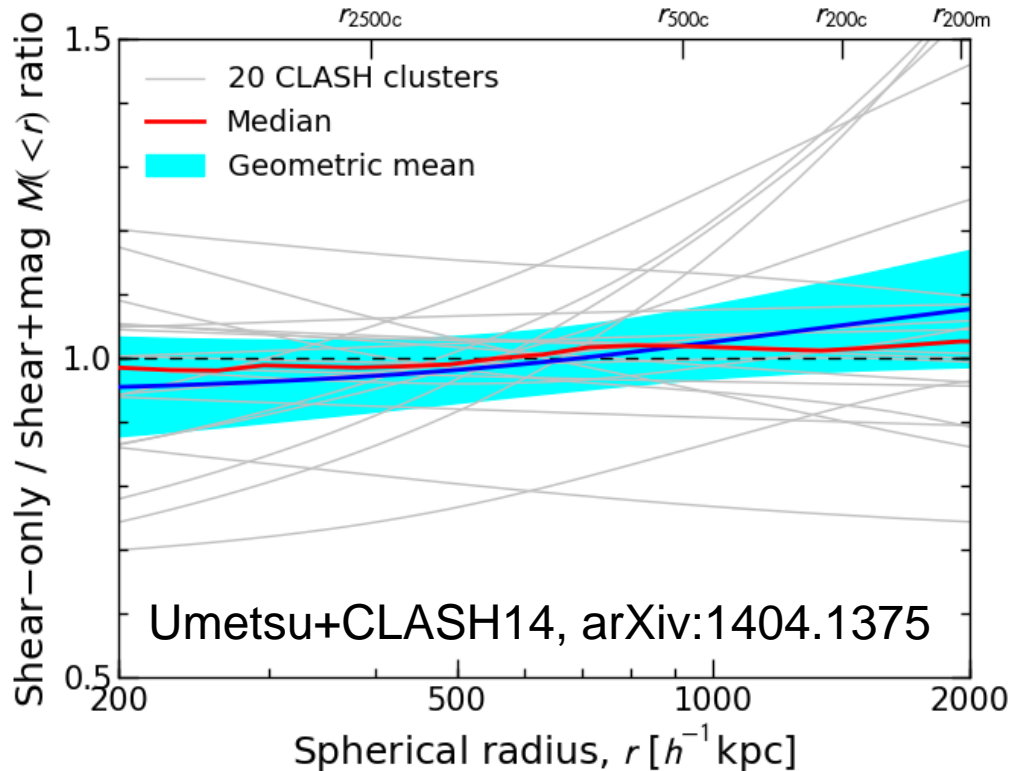
- All 4 clusters from 8.3m Subaru Telescope





# Shear-Magnification Consistency

$M(<r)$  de-projected assuming spherical NFW (20 CLASH clusters)

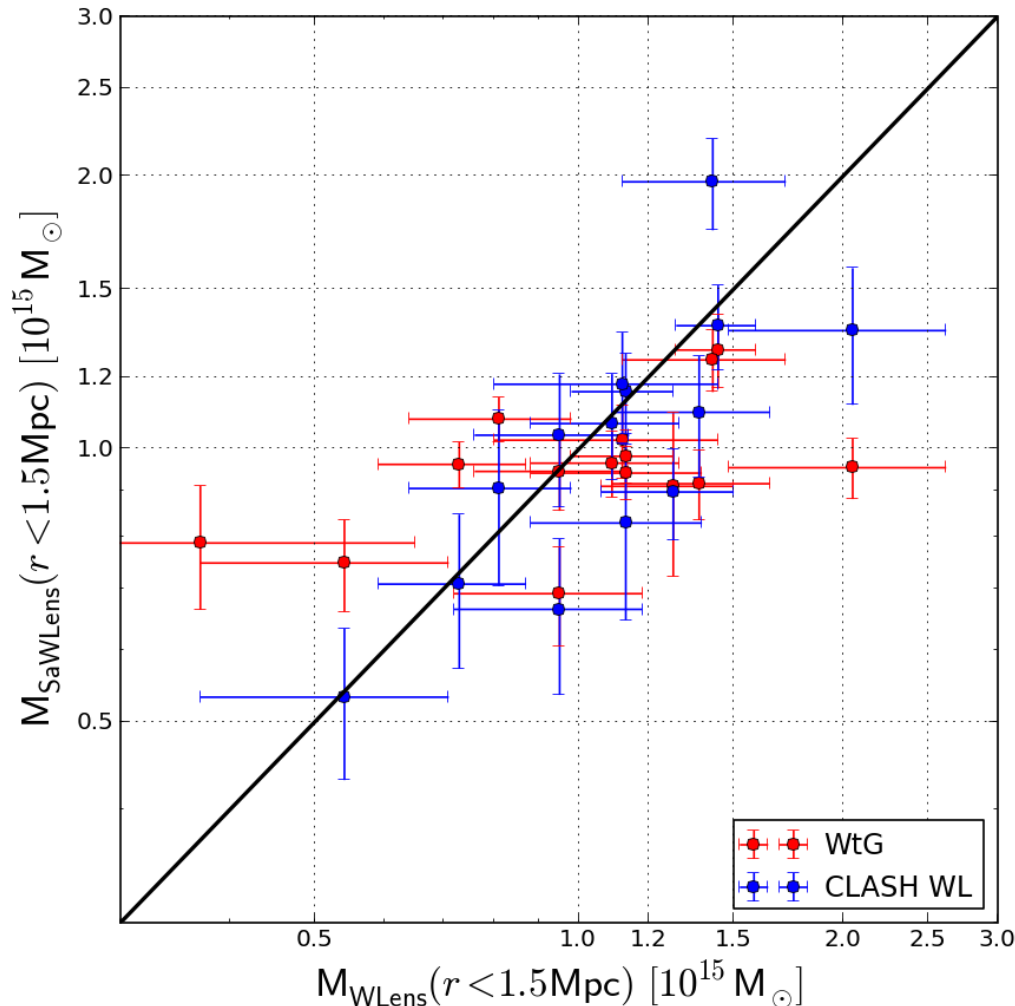


Internal systematic uncertainty in the overall mass calibration, empirically derived to be about  $\pm 8\%$



# Mass Comparisons @ R=1.5Mpc

Merten+CLASH 14



Un-weighted geometric mean mass ratios ( $\langle Y/X \rangle = 1/\langle X/Y \rangle$ )

- $\langle \text{SaWLens} / \text{WL} \rangle = 0.96$
- $\langle \text{WL} / \text{WtG} \rangle = 0.91$
- $\langle \text{SaWLens} / \text{WtG} \rangle = 0.88$

**WL (Umetsu+14)**

→ shear+mag (Subaru)

**SaWLens (Merten+14)**

→ SL + shear (HST+Subaru)

**WtG (Applegate+14)**

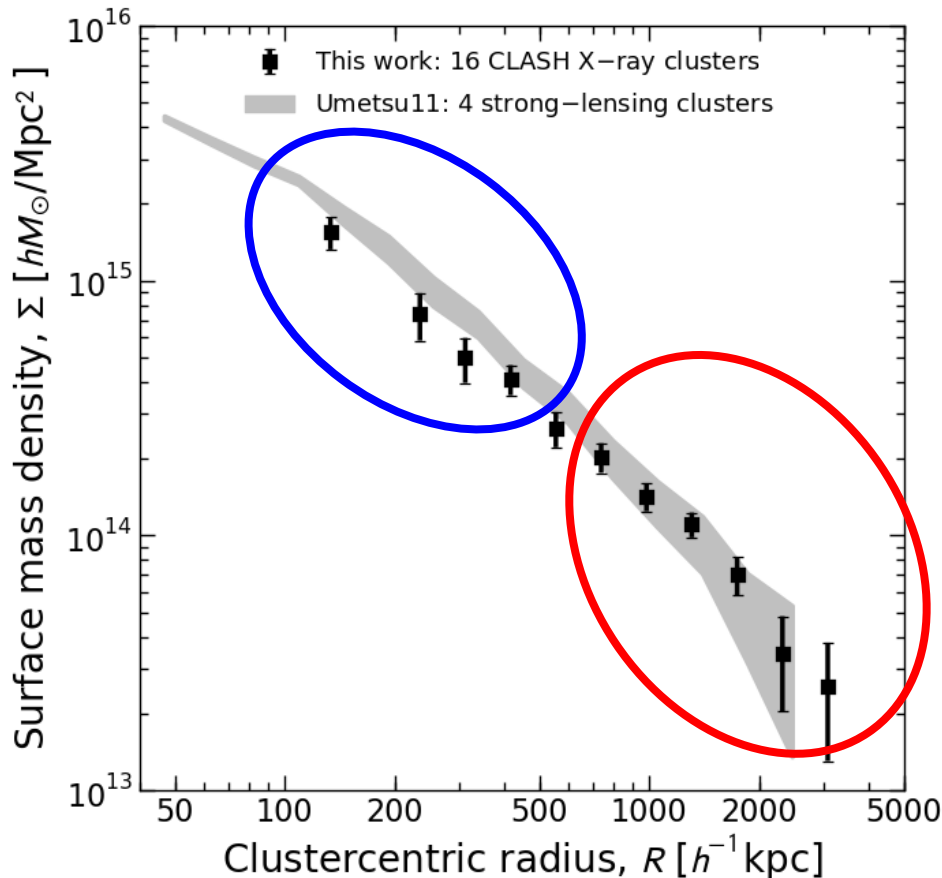
→ shear (Subaru)

Note: WL mass calibration uncertainty of 8 percent



# Comparison with pre-CLASH results

- $C_{200}$  vs  $\theta_E$  relation, consistent with triaxial CDM halos (Oguri+12)
- **Similar  $v$  (MAH), similar  $\Sigma$  in outskirts (Diemer & Kravtsov 14)**
- **Increased  $\Sigma$  at  $R < 0.5 \text{ Mpc}/h$ , consistent w orientation bias (Gao+12)**



## CLASH X-ray-selected sample

- $M_{200} = 1.3e15 M_{\text{sun}}$
- $\underline{C_{200} = 4.0}$
- $\underline{\theta_E \sim 15'' (z_s=2)}$
- $\underline{v=3.8 (b_h \sim 9)}$

## Umetsu11b sample

- $M_{200} = 1.7e15 M_{\text{sun}}$
- $\underline{C_{200} = 6.1}$
- $\underline{\theta_E \sim 36'' (z_s=2)}$
- $\underline{v=4.1 (b_h \sim 11)}$