- Suppose a durable good exhibits positive network effect, and transition to new standard is graduate, what are its implications on efficiency of adoption of new technology?
- Both excess inertia (in which consumers fail to efficiently adopt a new technology) and excess momentum (in which consumers inefficiently adopt a new technology) can occur.
- Tactics to compete include preannouncement and predatory pricing.

- ► Continuous time. Continuous inflow of new users, continuous time.
- Before T*, only technology U is available. At T*, a new technology V arrives.
- ► Those who had adopted *U* before *T**cannot switch. Only newly arrived consumers can choose.
- Consumers arrive at a rate $n(t) \ge 0$, and $N(t) \equiv \int_0^t n(t')dt'$.
- u(x): utility of consuming U when the measure of size of U is x.
 u'(x) > 0. v(x) is the corresponding utility of using V.

- First consider two extreme cases: (1) Nobody from T* on adopts V; and (2) everybody does so.
- A user adopting U at time T, when everyone that follows also does so, has a utility of

$$\bar{u}(T) \equiv \int_{T}^{\infty} u(N(t)) e^{-r(t-T)} dt;$$

where r is discount rate.

▶ If a user at *T* is the last one to adopt *U*, his utility is

$$\tilde{u}(T) \equiv u(N(t)) \int_{T}^{\infty} e^{-r(t-T)} = u(N(T))/r.$$

► If a user adopts V at T ≥ T* when everyone that follows also does so, his utility is

$$ar{v}(T)=\int_T^\infty v(N(t)-N(T^*))e^{-r(t-T)}dt, \ T\geq T^*.$$

- $\tilde{v}(T)$ can be defined analogously.
- ► A linear example:

$$n(t) = 1, N(t) = t, u(x) = a + bx, v(x) = c + dx = c + d(t - T^*).$$

In this case

$$\overline{u}(T)(a+bT)/r+b/r^2.$$

 $\widetilde{u}(T) = (a+bT)/r, \ \overline{v}(T) = (c+d(T-T^*))/r+b/r^2.$

► The linear case illustrated:



FIGURE 1: THE LINEAR EXAMPLE

- ► In linear case V can be superior to U in either of two ways: It might offer higher network-independent benefits (c > a), or it might have higher network-generated benefit (d > b).
- We only have to consider the two extreme cases listed above, because of bandwagon effect.
- Adoption of V is SPE if $\overline{v}(T^*) \geq \widetilde{u}(T^*)$.
- If v
 (T*) < u
 (T*) the dominant strategy for users close to T* is to choose U, and U will stay forever.</p>

- If $\bar{u}(T^*) \geq \tilde{v}(T^*)$, non-adoption is SPE.
- If u
 (T^{*}) < v
 (T^{*}) it is dominant strategy for early choosers, and thus all that follow, to adopt V.
- Adoption is SPE if $\bar{v}(T^*) \geq \tilde{u}(T^*)$. Nonadoption is SPE if $\bar{u}(T^*) \geq \tilde{v}(T^*)$.

They may hold simultaneous, so that there are multiple equilibria.

- If V is adopted, each user for whom $\bar{v}(T) > \bar{u}(T)$ gains $\bar{v}(T) \bar{u}(T)$.
- Two groups of losers:
 - (a) Early adopters lose $\bar{u}(T) \bar{v}(T)$.

(b) Old users.

Present value of welfare change in linear case is

$$G \equiv \int_{T}^{\infty} [\bar{v}(t) - \bar{u}(t)] e^{-r(t-T^*)} dt - bT^*/r^2.$$

- The first term is change in welfare for those arrive after T*. The 2nd term is loss to the installed base.
- ▶ In linear case, G can be calculated to equal to

$$[2(d-b)-2rbT^*+r(c-a)]/r^3.$$

• Adoption is an equilibrium if $\bar{u}(T^*) \geq \tilde{u}(T^*)$, that is

$$r(c-a)-rbT^*\geq -d.$$

• Adoption is unique equilibrium if $\tilde{v}(T^*) > \tilde{u}(T^*)$, that is,

r(c-a)-rb>b.



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- There can be excess inertia and excess momentum, depending on the relative importance of installed base, network independent utility, and network-dependent utility.
- Competitive tactics implied by above theory: Preannouncement and predatory pricing.

- Suppose new product is announced at T^{*} − τ, and consumers in [T^{*} − τ, T^{*}] can pre-adopt V.
- If all adopt V after time $T^* \tau$, the utility of user arriving at $t \ge T^*$ is $\bar{v}(t + \tau)$.
- If $\tilde{v}(T^*) < \tilde{u}(T^*)$ and $\tilde{v}(T^* + \tau t')\bar{e}^{-rt'} > \bar{u}(T^* t')$ for all $t' \in [0, \tau]$, then

(1) Non-adoption is unique equilibrium without preannouncement.

(2) Adoption is equilibrium with pre-announcement.

Preannouncement can reduce welfare.

- By charging lower price, the manufacturer of U can prevent the potentially early users of V from adopting it, and drive out then new technology from market, even if it is efficient to adopt V.
- Suppose U is monopolistically supplied and V is competitively supplied.

A low price of U starting at time T* can induce users to adopt U (when otherwise they should adopt V). If installed base of V is built up, then V will never be adopted.

