

ASloP Colloquium Talk

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***Galaxy Cluster Gravitational  
Lensing as Cosmological Probes***

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- Clusters of galaxies

## 2. Cluster Gravitational Lensing

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- Strong and Weak lensing in clusters

## 3. Observational Cluster Lensing Highlights

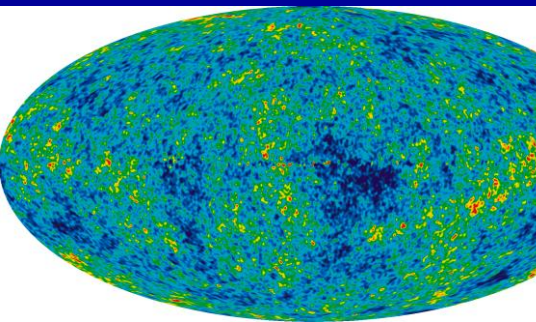
- Combined weak and strong lensing analyses of high-mass clusters using Hubble + Subaru observations

## 4. Summary

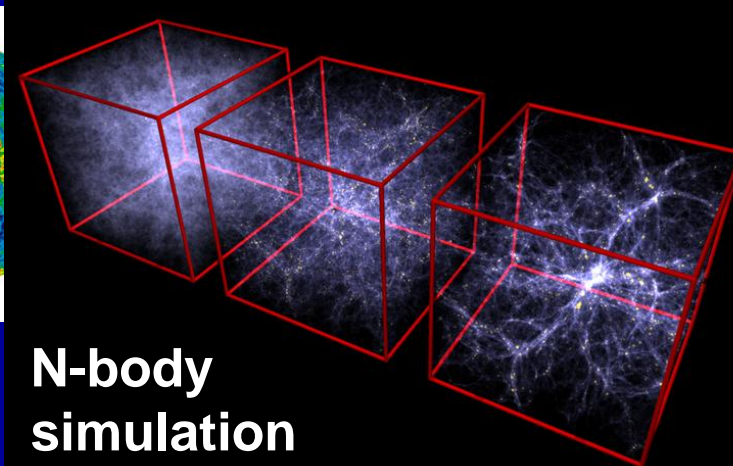
# 1. Structure Formation Scenario

## Current paradigm of structure formation: Lambda Cold Dark Matter (LCDM)

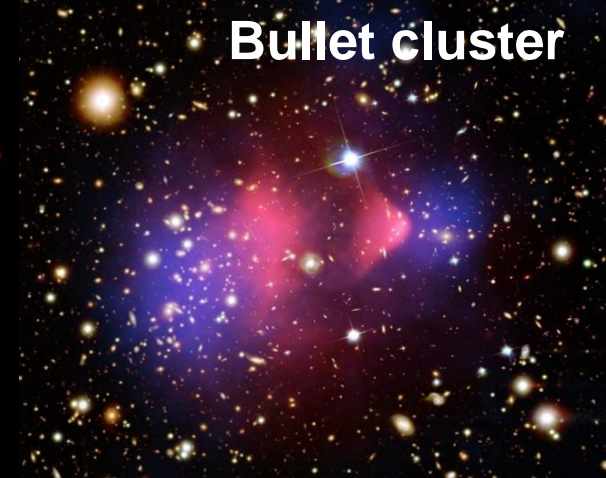
- Background geometry and Initial conditions, successfully constrained by linear theory & large-scale astrophysical observations:
  - CMB, large-scale clustering of galaxies, and SNIa distance measurements
- >70% of the “*present-day*” energy density is in **Dark Energy**, leading to an accelerated cosmic expansion → suppressing structure growth in later epochs
- ~85% of our “*material universe*” is composed of **DM** – the majority of which being non-relativistic (small FS length), collisionless on astrophysical scales
- Study **nonlinear hierarchical** structure formation due to **gravitational instability** using N-body simulations + perturbation theory ( $0 < z < z_{\text{dec}} \sim 1100$ )



Cosmic seeds in CMB (WMAP)

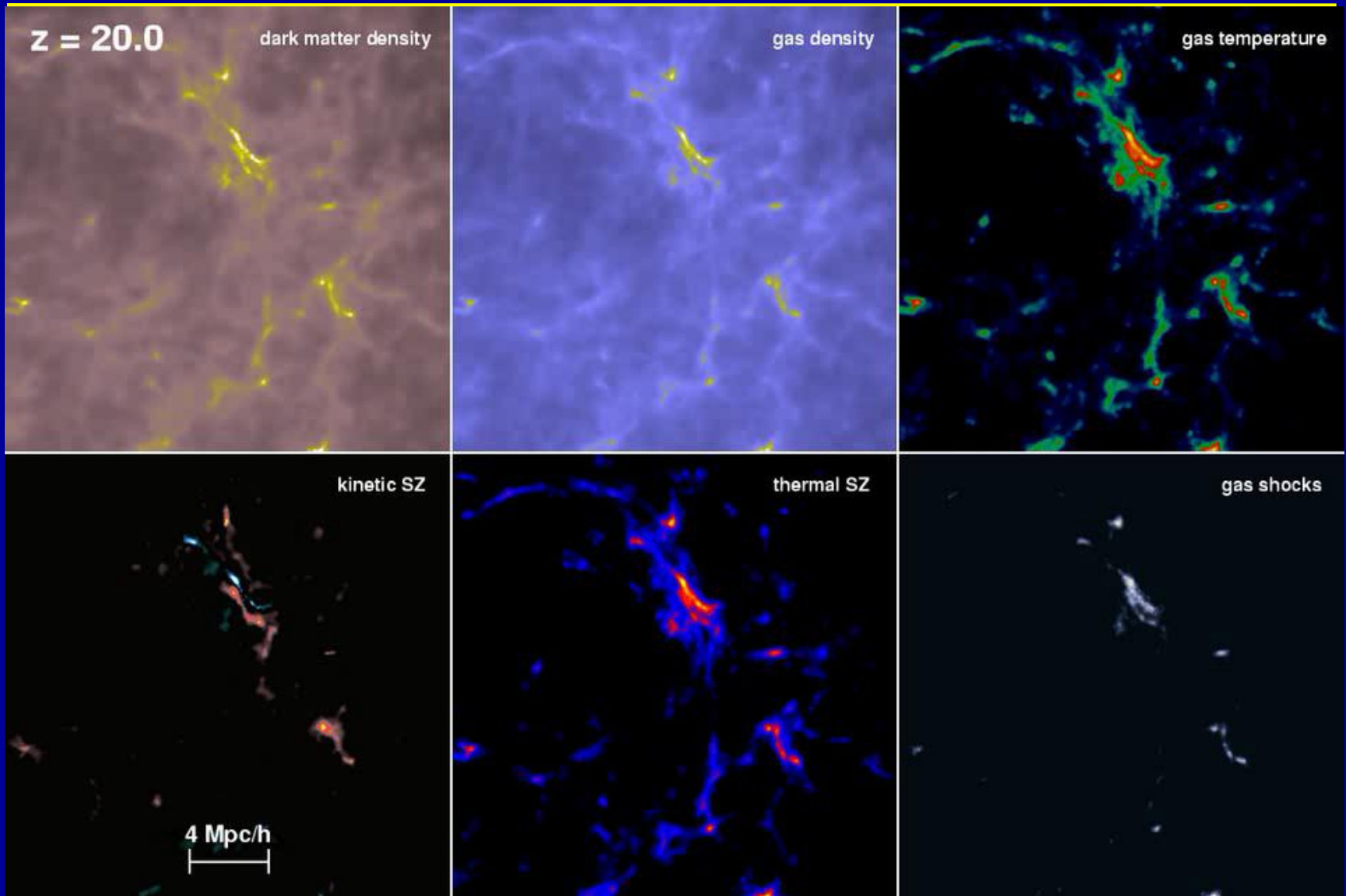


N-body simulation



Bullet cluster

# Simulated Cluster Formation (LCDM)

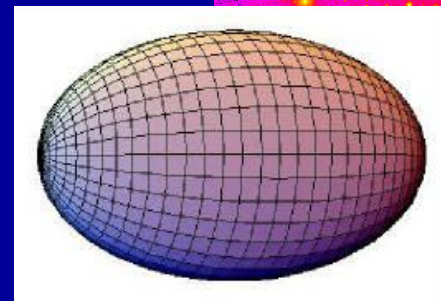
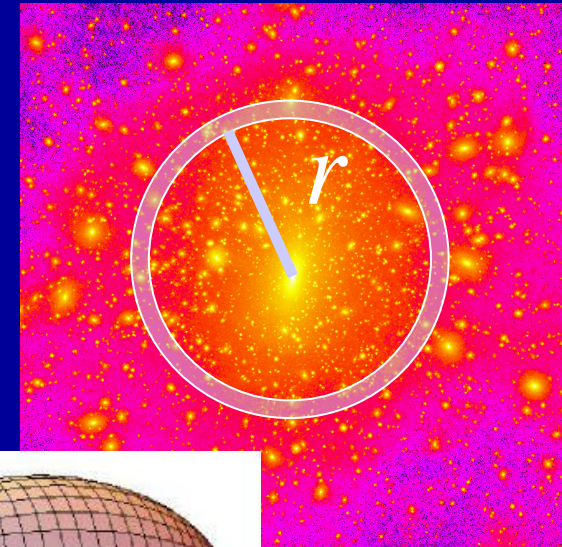


Credit: Volker Springel (*Data Visualization*)

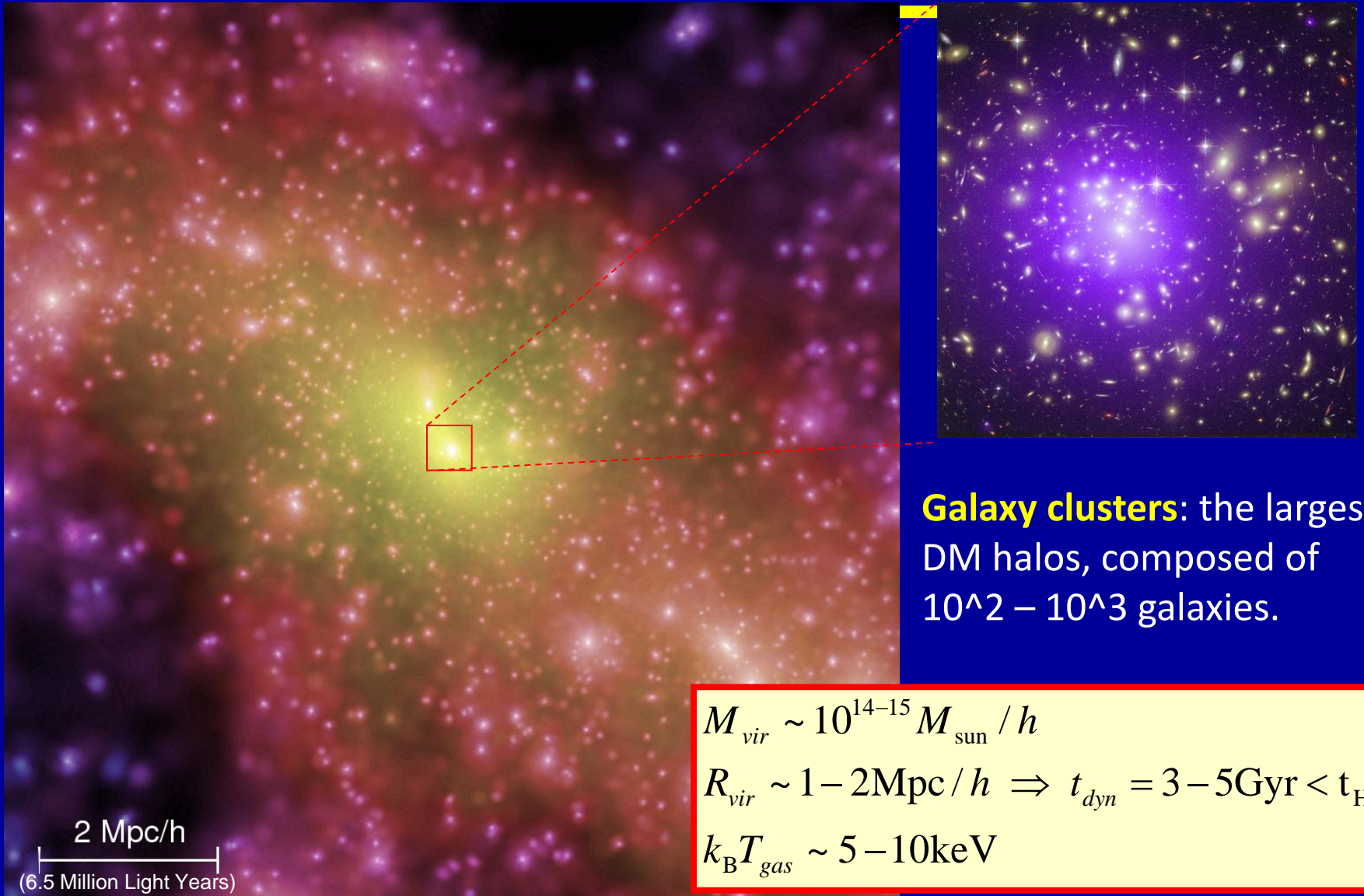
# Predicted properties of CDM halos

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- CDM mass profiles  $\rho(r)$  are nearly **universal**
  - **Shape** is approximately independent of halo mass (**self-similar**)
  - **Normalization**: the more massive a halo, the LESS concentrated it is.
  - Origin of the universal profile?
- CDM halos are **cuspy**,  $\rho(r) \sim r^{-\alpha}$  ( $\alpha \sim < 1$ ) at  $r \rightarrow 0$ 
  - Progressively steepening with radius
  - Annihilation signal?
- CDM halos are **clumpy**
  - Abundant substructure ( $\sim 20\%$  in mass)
  - Overabundance of galactic satellites in LCDM?
- CDM halos are **triaxial**
  - Preference for prolate configuration
  - Asphericity increasing toward the center

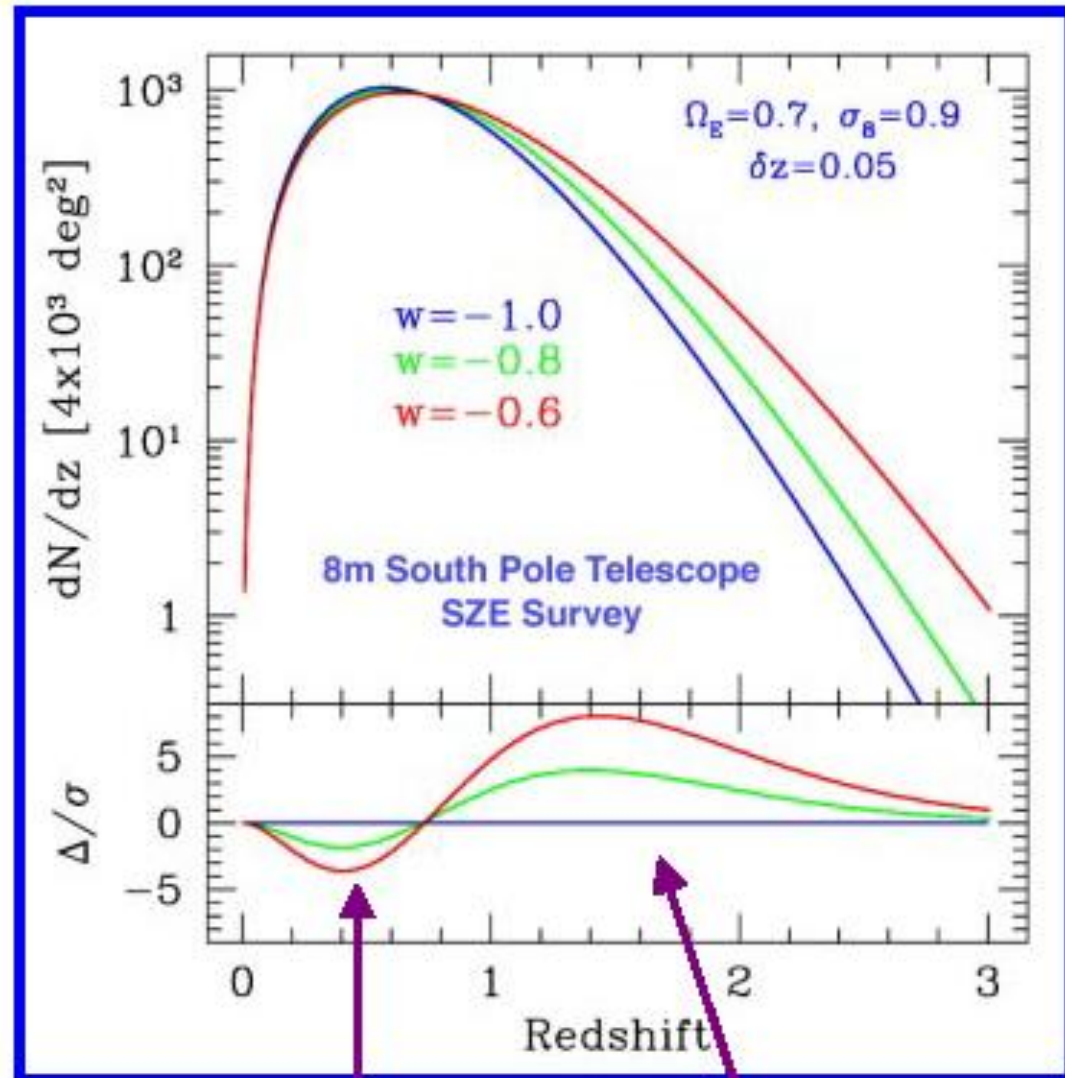


# Clusters of Galaxies



Simulation of dark matter around a forming cluster (Springel et al. 2005)

# Clusters as Cosmological Probes



$dV/d\Omega/dz$

Volume effect

$\Delta(t) = \Delta\rho/\rho \sim D_+(t)$

Growth effect

[Left] Cluster counts  $dN(z)/dz$  predictions for different DE EoS,  $w = P/(\rho c^2)$ , normalized to the local Universe

**Cosmological test with structure formation in  $0 < z < 3$ , complementary to CMB, BAO, SNe.**

The key is accurate determination of cluster mass and internal mass profile (aka, halo model) in any cluster cosmology.

Simulation by the SPT team

# Fundamental Questions in Cluster Cosmology

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## 1) Quasi-Equilibrium mass profile shape of DM halos:

“How the shape of a cluster’s DM potential depends on cluster mass and redshift?”

## 2) DM vs. Baryons:

“How the baryons distribute within the gravitational potential wells of clusters?”

## 3) DM and Dark Energy (DE):

“How the number of clusters of a given mass should increase with time? How its growth rate depends on the background cosmology?”

## 4) Primordial non-Gaussianity:

“What is the degree of non-Gaussianity in primordial density fluctuations?”

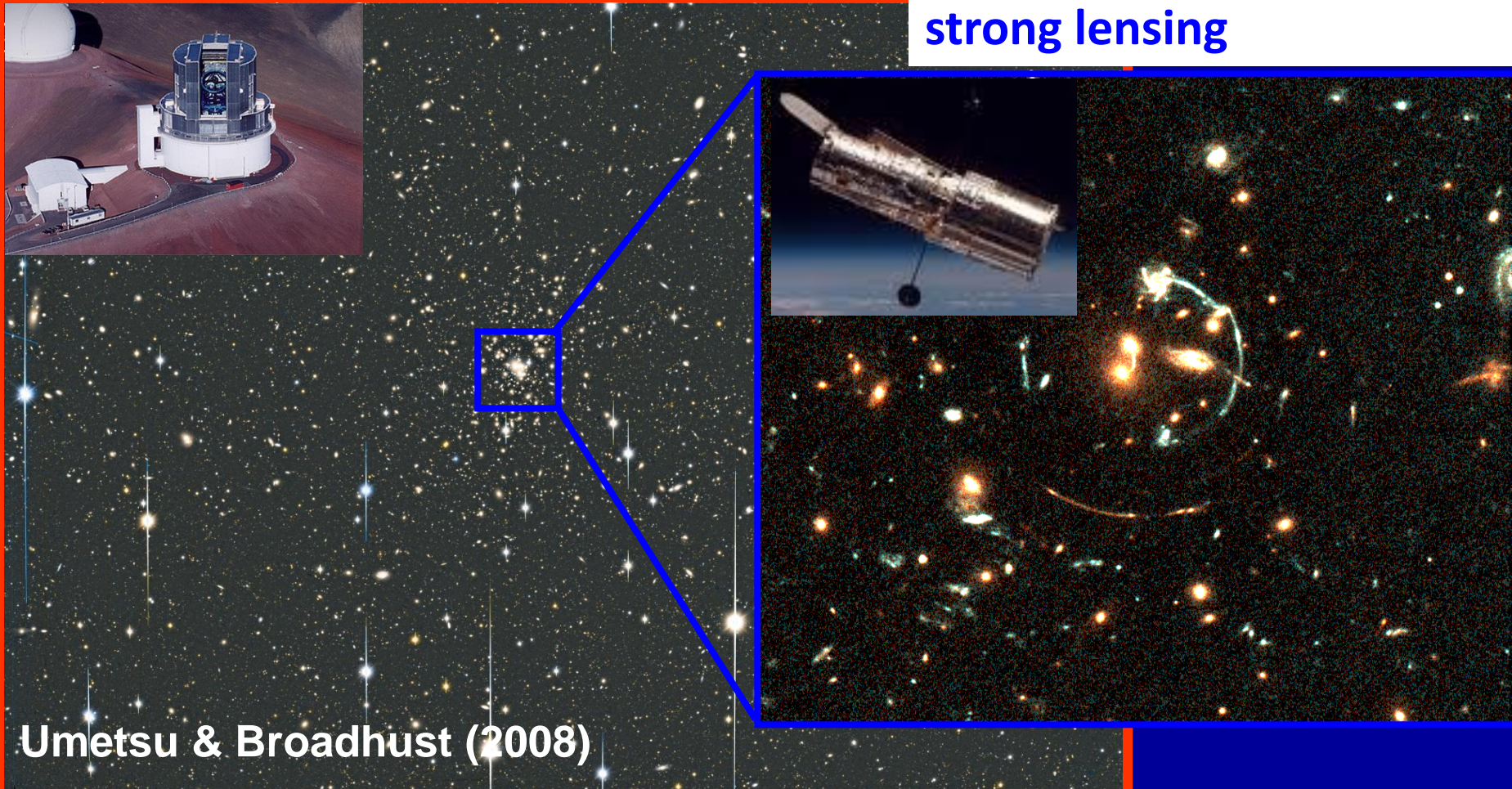
*Compare complementary cluster observations with testable predictions of models of structure formation*



# My Approach: Cluster Gravitational Lensing

*SUBARU* wide-field imaging  
(*Suprime-Cam*) for weak lensing

High-resolution space  
imaging with *Hubble* for  
strong lensing



Umetsu & Broadhurst (2008)

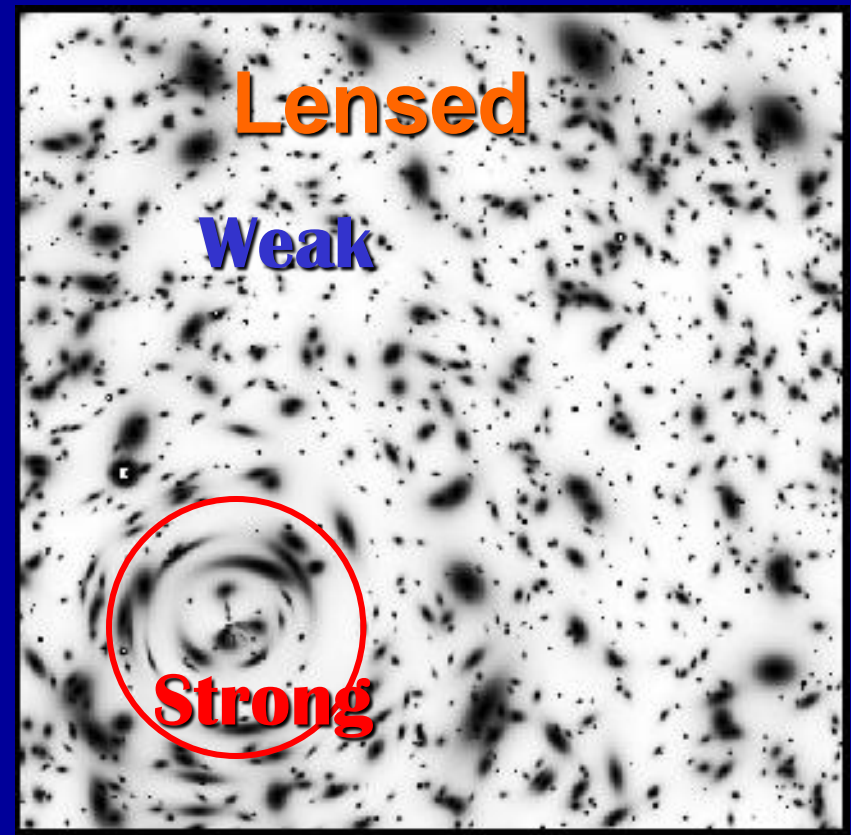
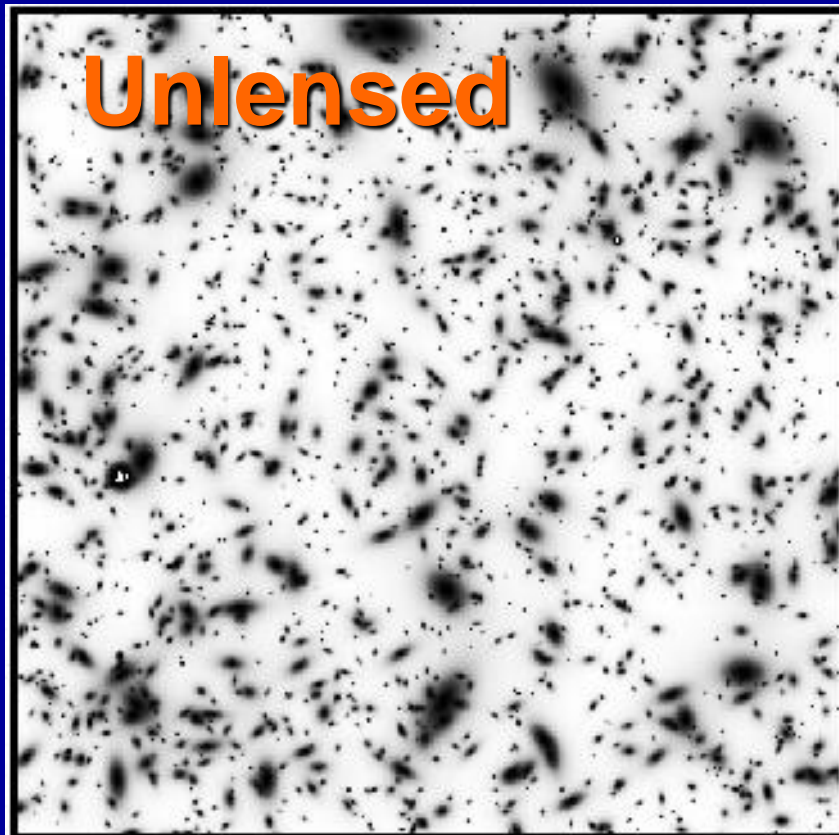
Observable deformation of background galaxy shapes and expansion of the sky can be used to map the DM distribution in large scale structure in the Universe.

## 2. Gravitational Lensing

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Gravitationally-lensed images of background galaxies carry the imprint of  $\Phi(x)$  of intervening cosmic structures:

Gravitational lensing is based only on gravity, so is the most direct method to study the Dark Side of the Universe!



Fort & Mellier

# Gravitational Bending of Light Rays

**Gravitational deflection angle** in the weak-field limit ( $|\Phi|/c^2 \ll 1$ )

Light rays propagating in an inhomogeneous universe will undergo **small transverse excursions** along the photon path:  
i.e., **light deflections**

*Gravitational field of deflecting matter*

$$\delta\hat{\alpha} \approx \frac{\delta p_{\perp}}{p_{\parallel}} = -\frac{2}{c^2} \nabla_{\perp} \Psi(x_{\parallel}, x_{\perp}) \delta x_{\parallel}$$

*Small transverse excursion of photon momentum*

$$\hat{\alpha}^{\text{GR}} = 2\hat{\alpha}^{\text{Newton}} \rightarrow \frac{4GM}{c^2 r} = 1.75 \left( \frac{M}{M_{\text{sun}}} \right) \left( \frac{r}{R_{\text{sun}}} \right)^{-1}$$

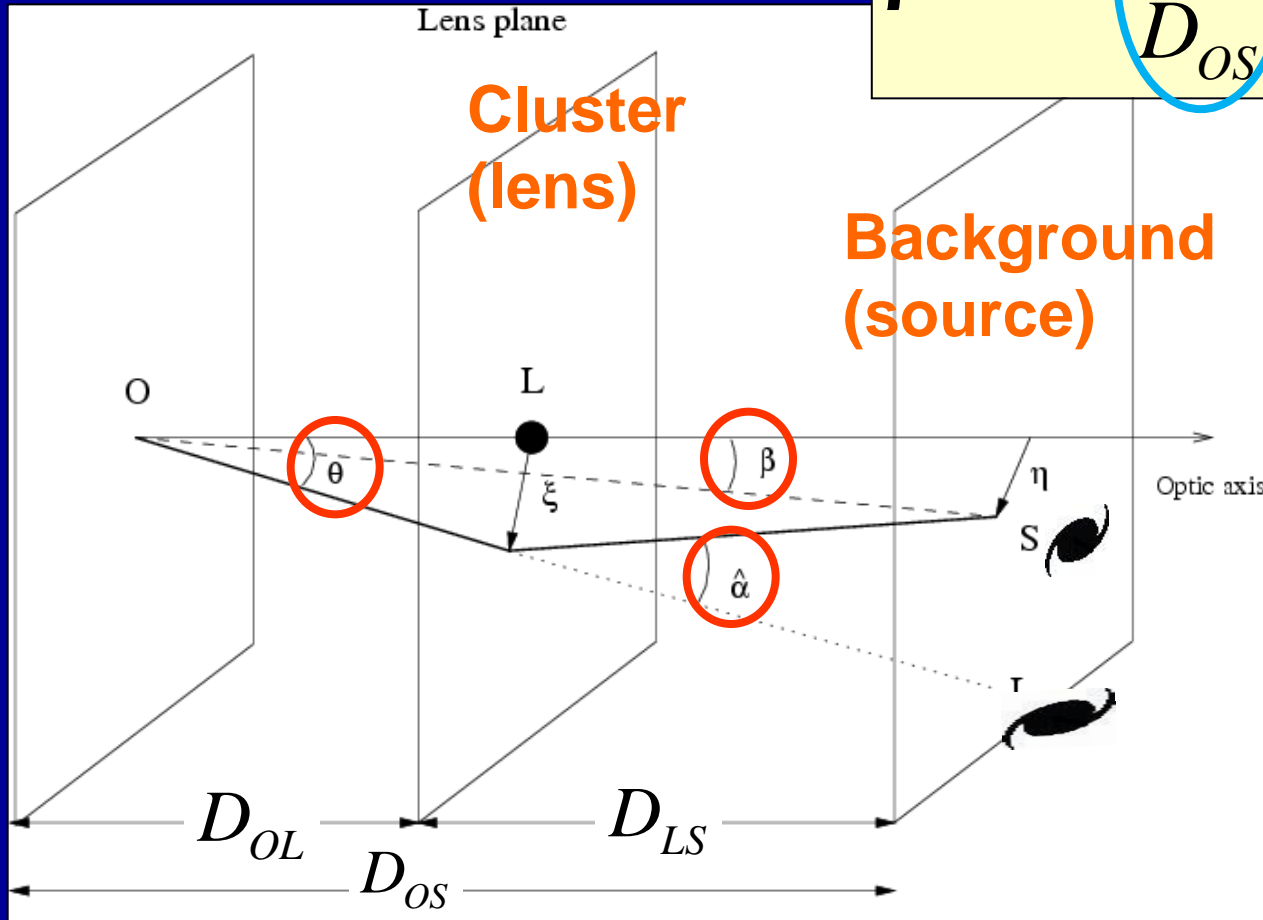
# Lens Equation (for cluster lensing)

Cosmological lens equation + single/thin-lens approximations

$\beta$ : true (but unknown) source position

$\theta$ : apparent image position

$$\beta - \theta = \frac{D_{LS}}{D_{OS}} \int \delta \hat{\alpha}(\theta) \equiv \nabla \psi(\theta)$$



Angular diameter distances:

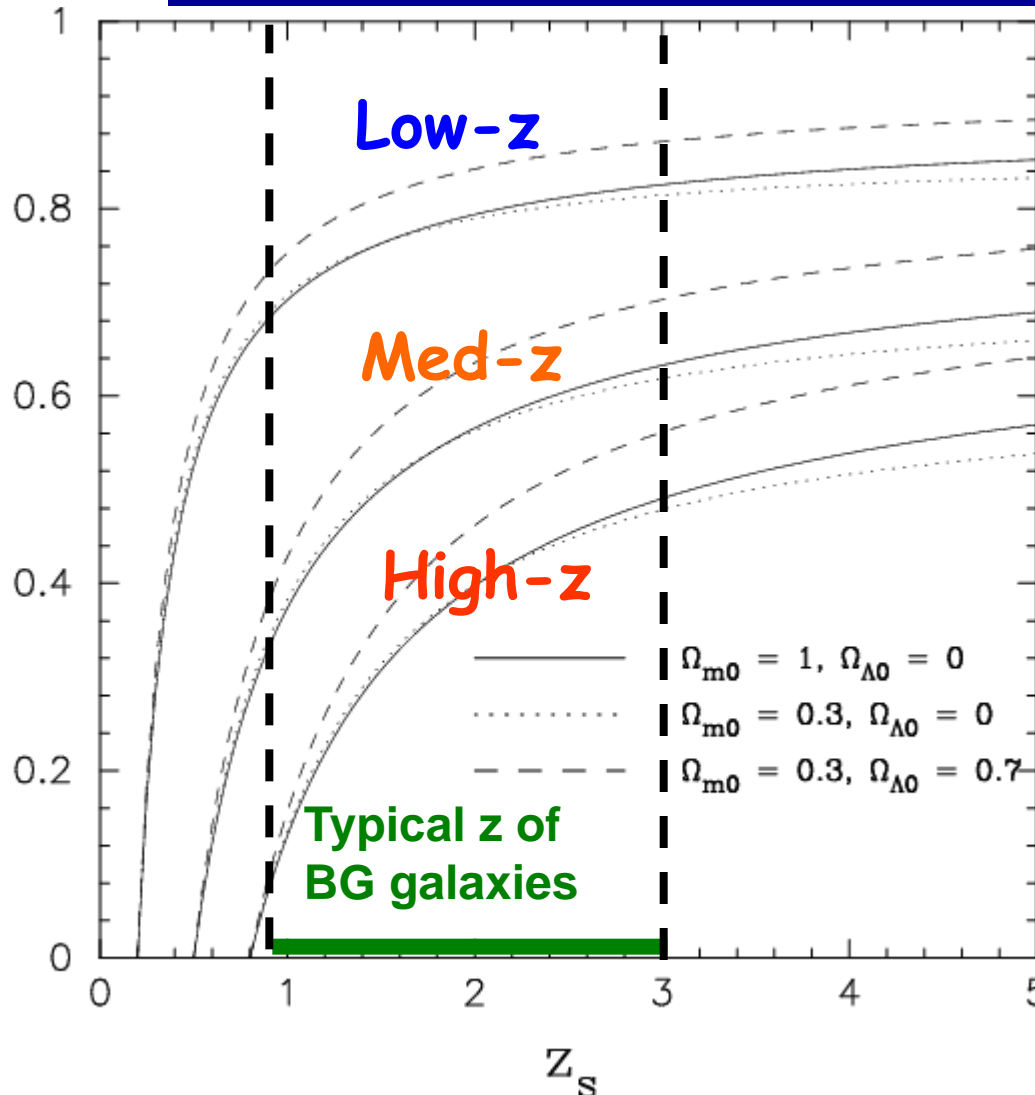
$$D_{OL}, D_{LS}, D_{OS} \sim O(c/H_0)$$

For a rigid derivation of cosmological lens eq., see, e.g., Futamase 95

# Geometric Scaling of Lensing Signal

$$D_{LS} / D_{OS}$$

Distance ratio as a function of source  $z$ ,  $z_s$



Per-source sensitivity for a given lens

**Low-z lens:**

$$z_L = 0.2$$

**Med-z lens:**

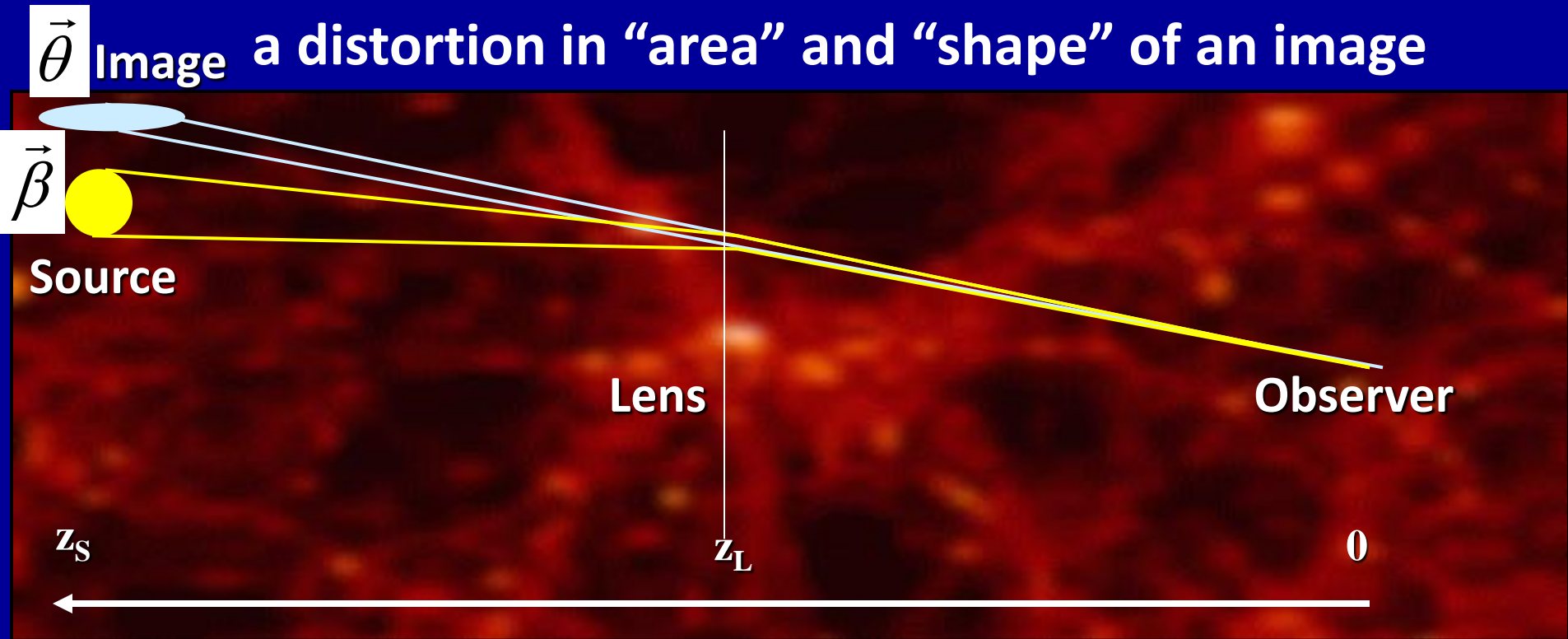
$$z_L = 0.5$$

**High-z lens:**

$$z_L = 0.8$$

# Shape and Area Distortions

Differential deflection due to tidal force causes a distortion in “area” and “shape” of an image



Deformation of an image

$$\delta\beta_i = (\delta_{ij} - \psi_{,ij})\delta\theta_j + O(\delta\theta^2)$$

$$\approx \left[ (1 - \kappa)\delta_{ij} - \Gamma_{ij} \right] \delta\theta_j$$

Magnification of flux (solid angle)

$$\mu = \det\left(\frac{\partial\boldsymbol{\beta}}{\partial\boldsymbol{\theta}}\right)^{-1} = \frac{1}{(1 - \kappa)^2 + \det\Gamma}$$

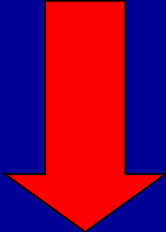
# Physical Meaning of $\kappa$

**Lens Convergence:** weighted projection of mass overdensity  $\delta\rho$

$$\kappa(\boldsymbol{\theta}) \equiv \frac{1}{2} \Delta^{(2)} \psi(\boldsymbol{\theta}) = \int dD \delta\rho \left( \frac{c^2}{4\pi G} \frac{D_{OS}}{D_{OL} D_{LS}} \right)^{-1} \approx \frac{\Sigma(\boldsymbol{\theta})}{\Sigma_{\text{crit}}}$$

**Critical surface mass density**

$$\Sigma_{\text{crit}}(z_L, z_S; \Omega_m, \Omega_\Lambda, H_0) = \frac{c^2}{4\pi G} \frac{D_{OS}}{D_{OL} D_{LS}}$$

<b>Strong lensing</b>	$\kappa \sim 1$	@ cluster cores ( $r < 100\text{kpc}/h$ )	probability
<b>Weak lensing</b>	$\kappa \sim 0.1$	@ outside cluster cores ( $r > 100\text{kpc}/h$ )	
<b>Cosmic shear</b>	$\kappa \sim 0.01$	@ large scale structure	

*Note, this is only a crude definition, as lensing also depends on the (trace-free) tidal shear field,  $\Gamma$ .*

# Gravitational Shear Field

**Shear matrix** with 2-DoF can be expressed with 2 independent scalar potentials (e.g., Crittenden+2002):

$$\Gamma_{ij} = \left( \partial_i \partial_j - \frac{1}{2} \delta_{ij} \Delta^{(2)} \right) \psi_E + \frac{1}{2} \left( \varepsilon_{kj} \partial_i \partial_k + \varepsilon_{ki} \partial_j \partial_k \right) \psi_B$$

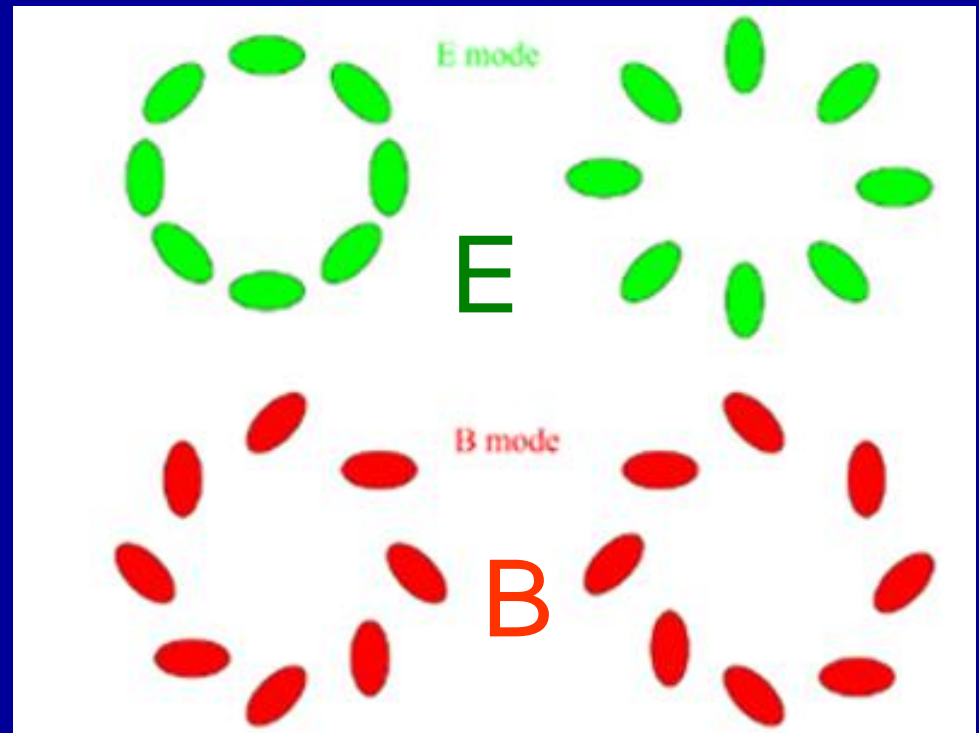
$$\psi_E = \psi \text{ (lens potential)}$$

$$\psi_B = 0$$

**In the weak-lensing limit,  
B-mode = 0**

B-mode “signal” can be used to monitor residual systematic effects in lensing measurements:

e.g., residual PSF anisotropies

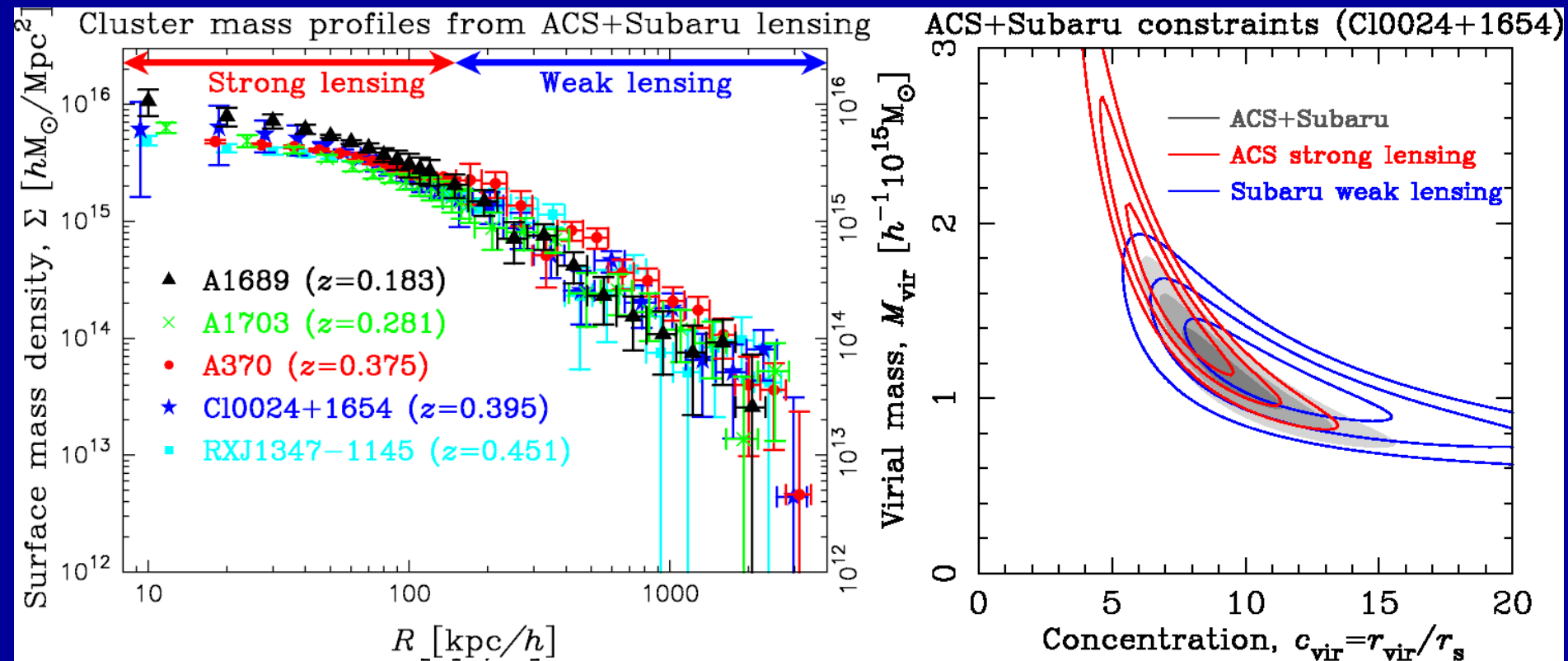




# Both Strong and Weak Lensing are needed

## Combining complementary Weak and Strong Lensing:

→ Probing cluster mass profiles in the full range [0.5%, 150%]  $R_{\text{vir}}$



# Strong and Weak Lensing

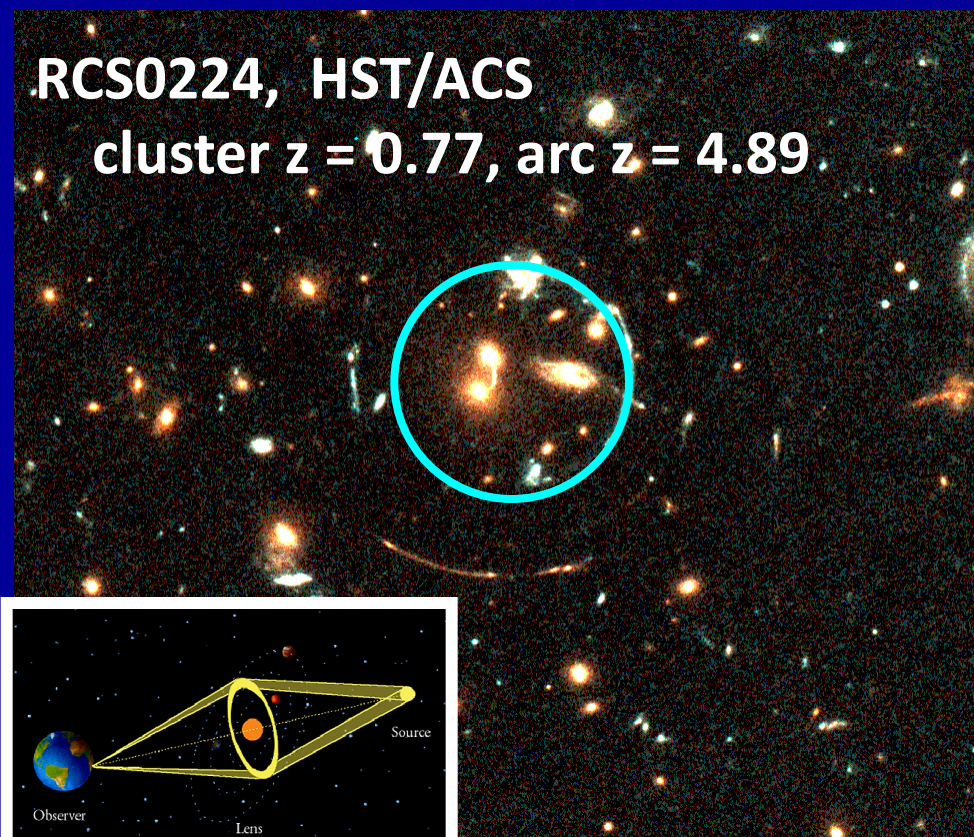
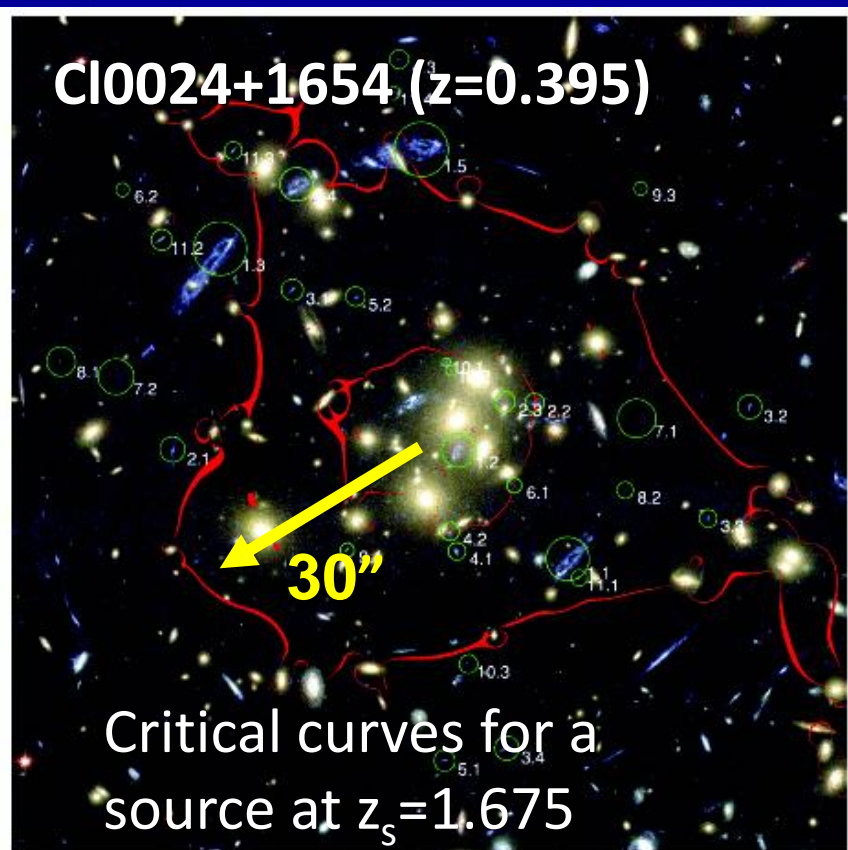
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- **Strong Gravitational Lensing (SL)**
- **Weak Gravitational Lensing (WL)**
  - *Tangential shear*
  - *Magnification bias*
  - *Stacked lensing analysis*

# Cluster Strong Lensing

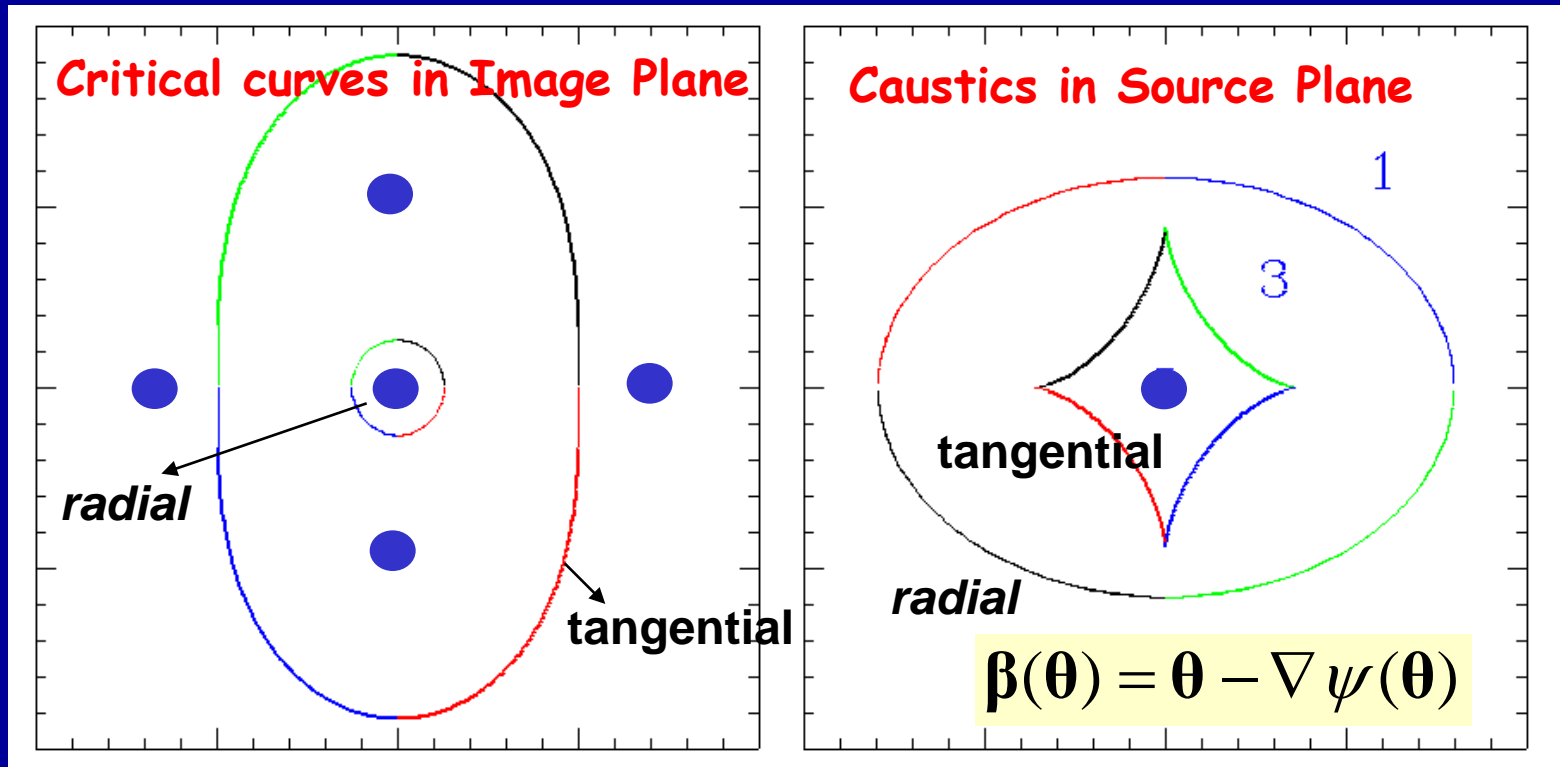
**SL phenomena include:** multiple imaging, high flux amplification, curved image features due to gravitational light deflection of the order 1-60 arcsec in cluster cores

[Left] 33 lensed images of 11 BG galaxies identified in HST multiband images by SL analysis (Zitrin, Broadhurst, Umetsu+09, MNRAS, 396, 1985)



# Critical Curves and Caustics

## A general elliptical lens potential



# Multiple Imaging and Magnification

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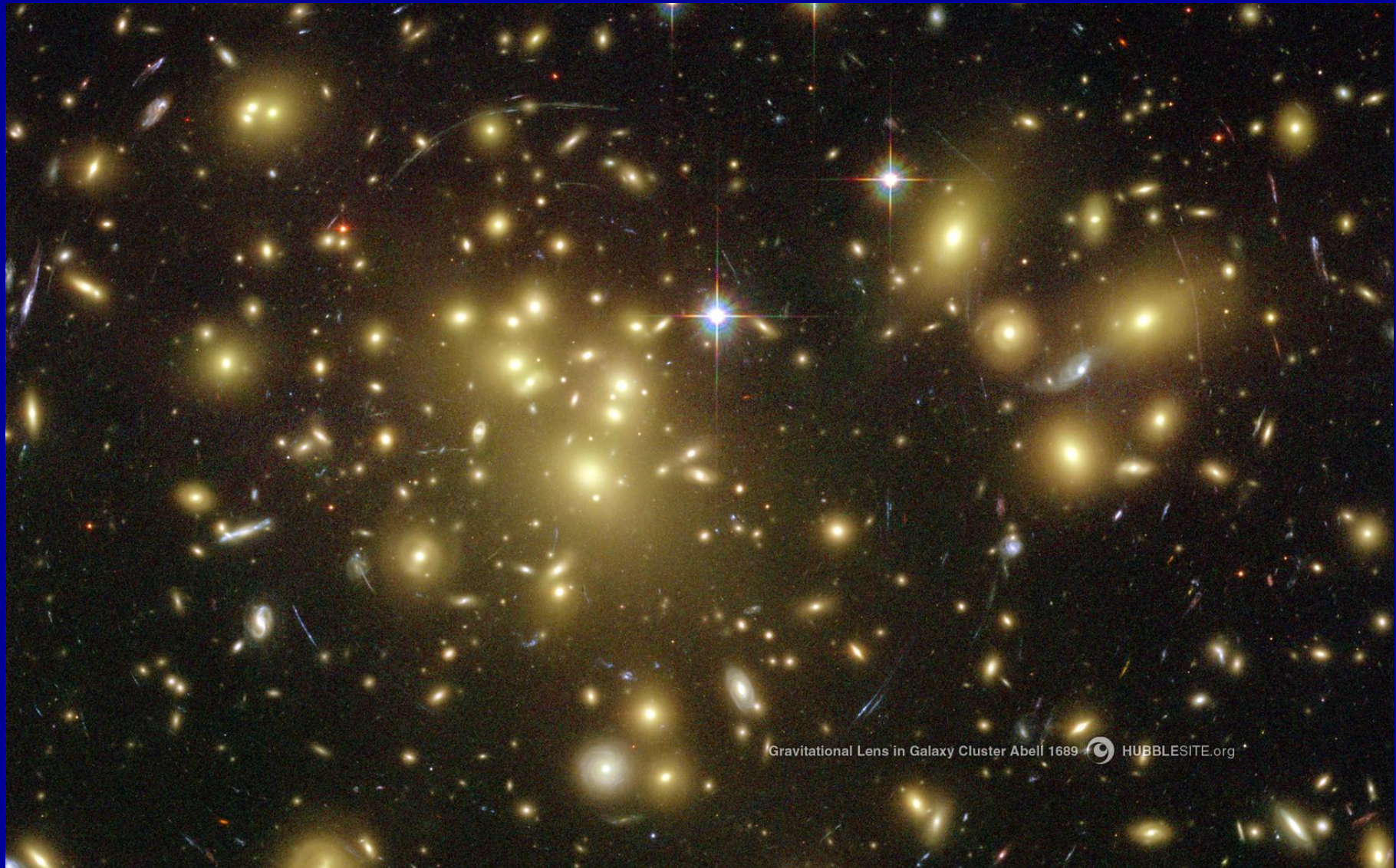


*A source galaxy at  $z=1.675$  has been multiply lensed into 5 apparent images*

**CL0024+1654  
( $z=0.395$ )**

**HST/WFPC2**

# Tangential arcs and multiple imaging



Gravitational Lens in Galaxy Cluster Abell 1689  HUBBLESITE.org

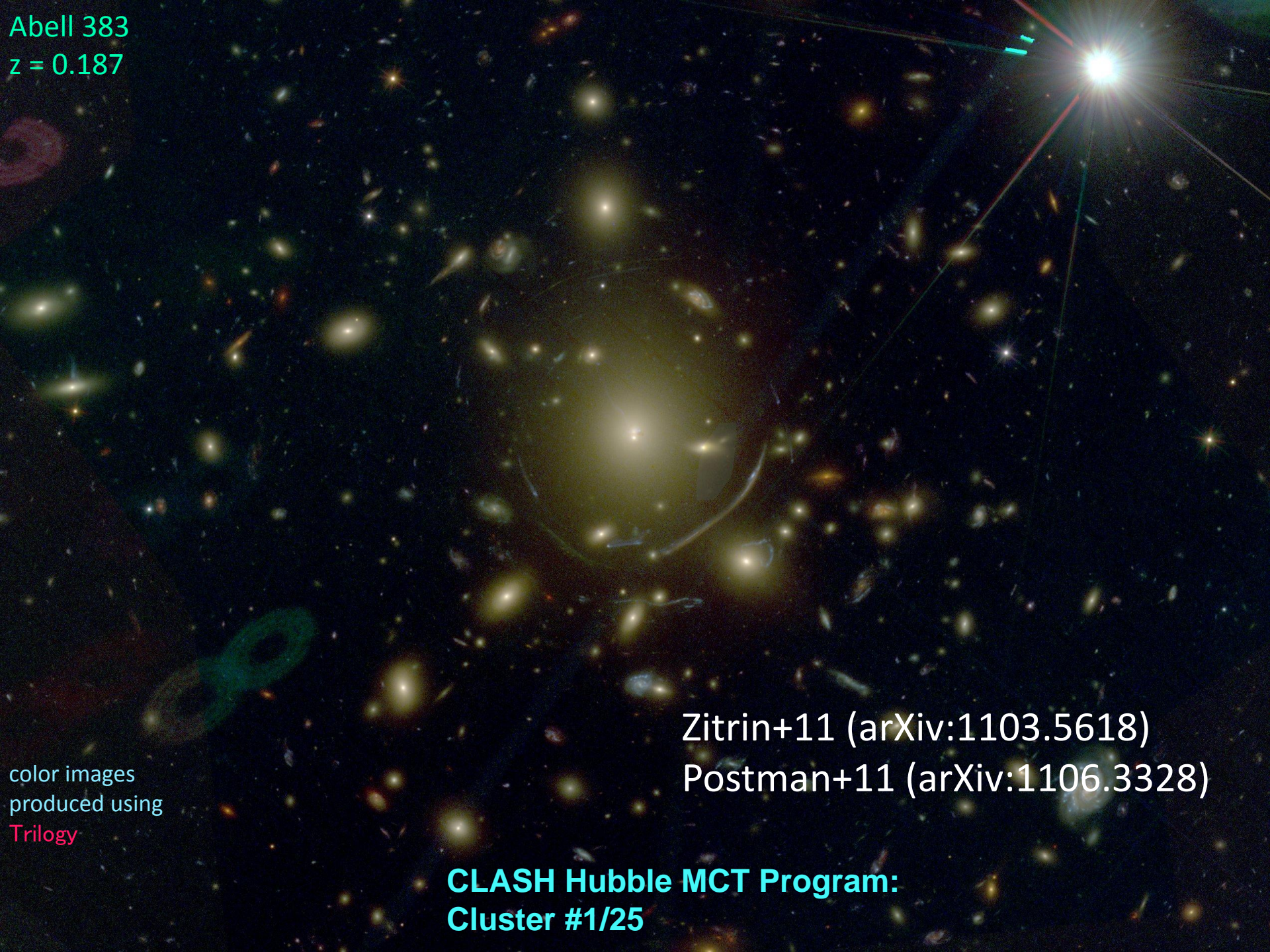
*A1689 ( $z=0.183$ ): One of the most massive clusters known. A total of  $>100$  lensed images of  $\sim 30$  BG galaxies identified by SL modeling (Broadhurst+05)*

Abell 383  
 $z = 0.187$

color images  
produced using  
Trilogy

Zitrin+11 (arXiv:1103.5618)  
Postman+11 (arXiv:1106.3328)

**CLASH Hubble MCT Program:  
Cluster #1/25**

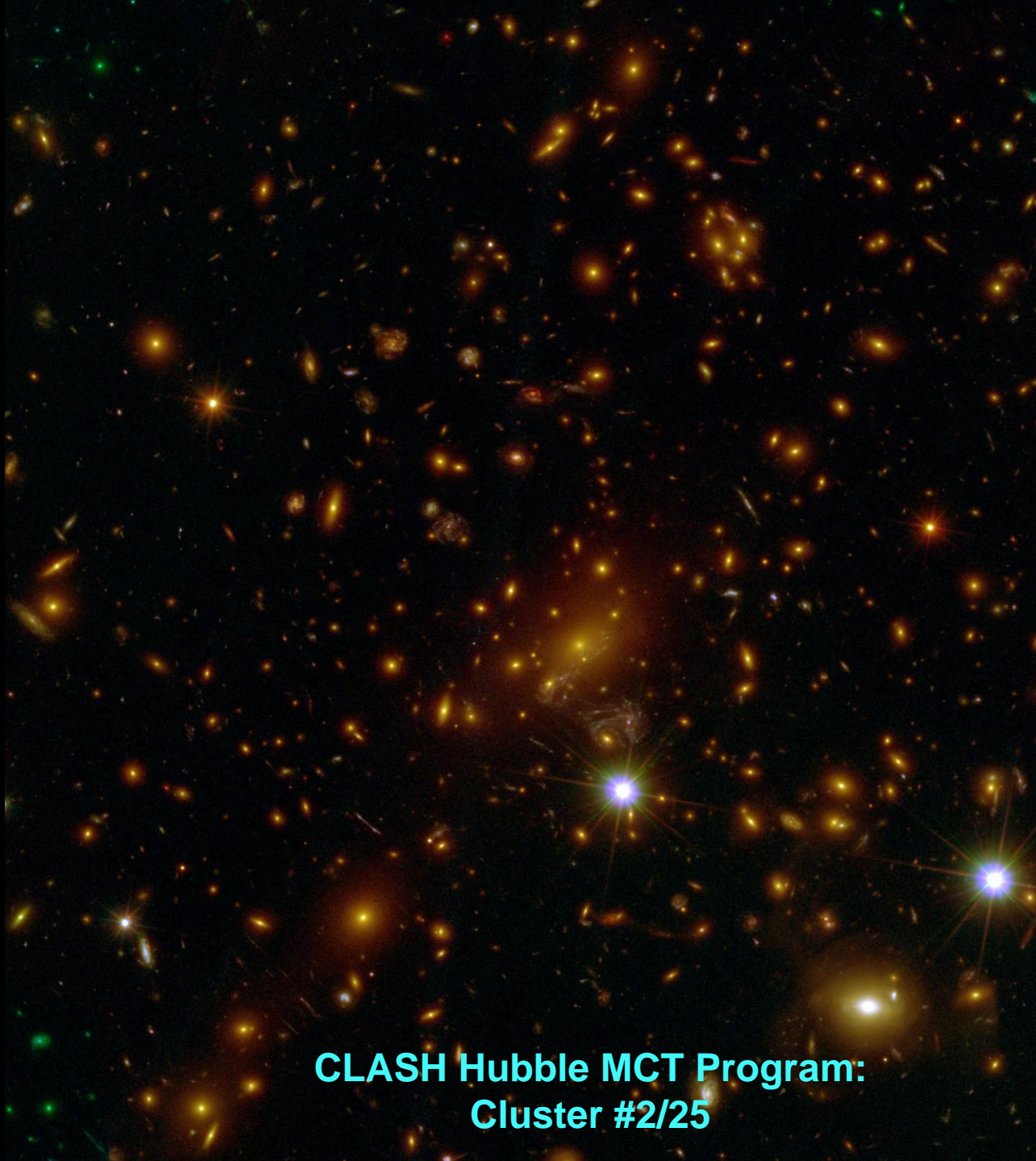


MACSJ1149

$z = 0.544$

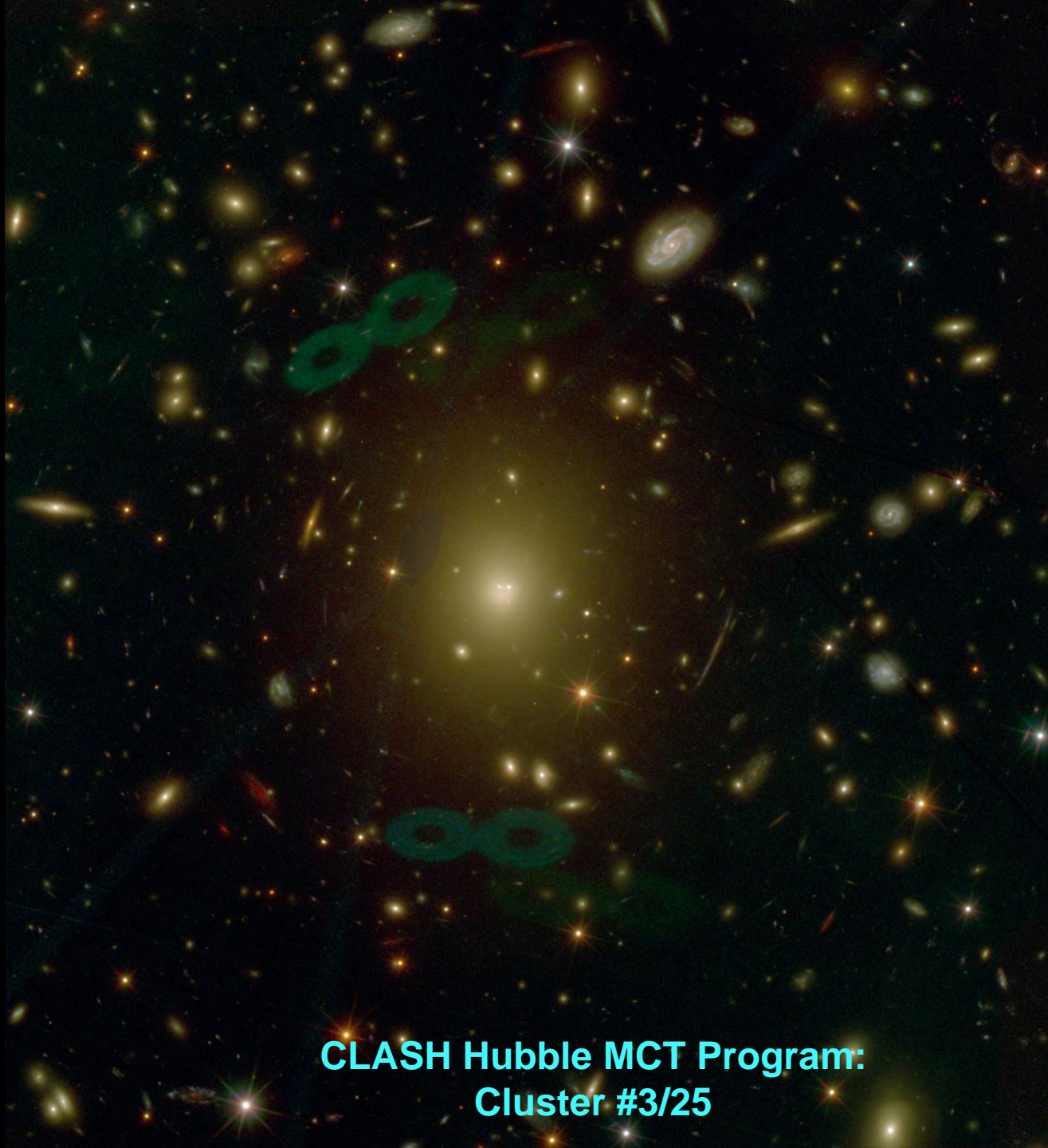
color images  
produced using  
*Trilogy*

**CLASH Hubble MCT Program:  
Cluster #2/25**





Abell 2261  
 $z = 0.224$



color images  
produced using  
Trilogy

**CLASH Hubble MCT Program:  
Cluster #3/25**

# Cluster Weak Lensing

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## Toward highest-possible lensing precision:

- ① Tangential Shear (Distortion)
- ② **Magnification** bias (Depletion)
- ③ **Stacked** Weak Lensing Analysis

See my lecture notes on

**“Cluster Weak Gravitational Lensing”**

from the “International School of Physics Enrico Fermi 2008, Italy”  
(also found at the Net Advance of Physics) [arXiv:1002.3952](https://arxiv.org/abs/1002.3952)

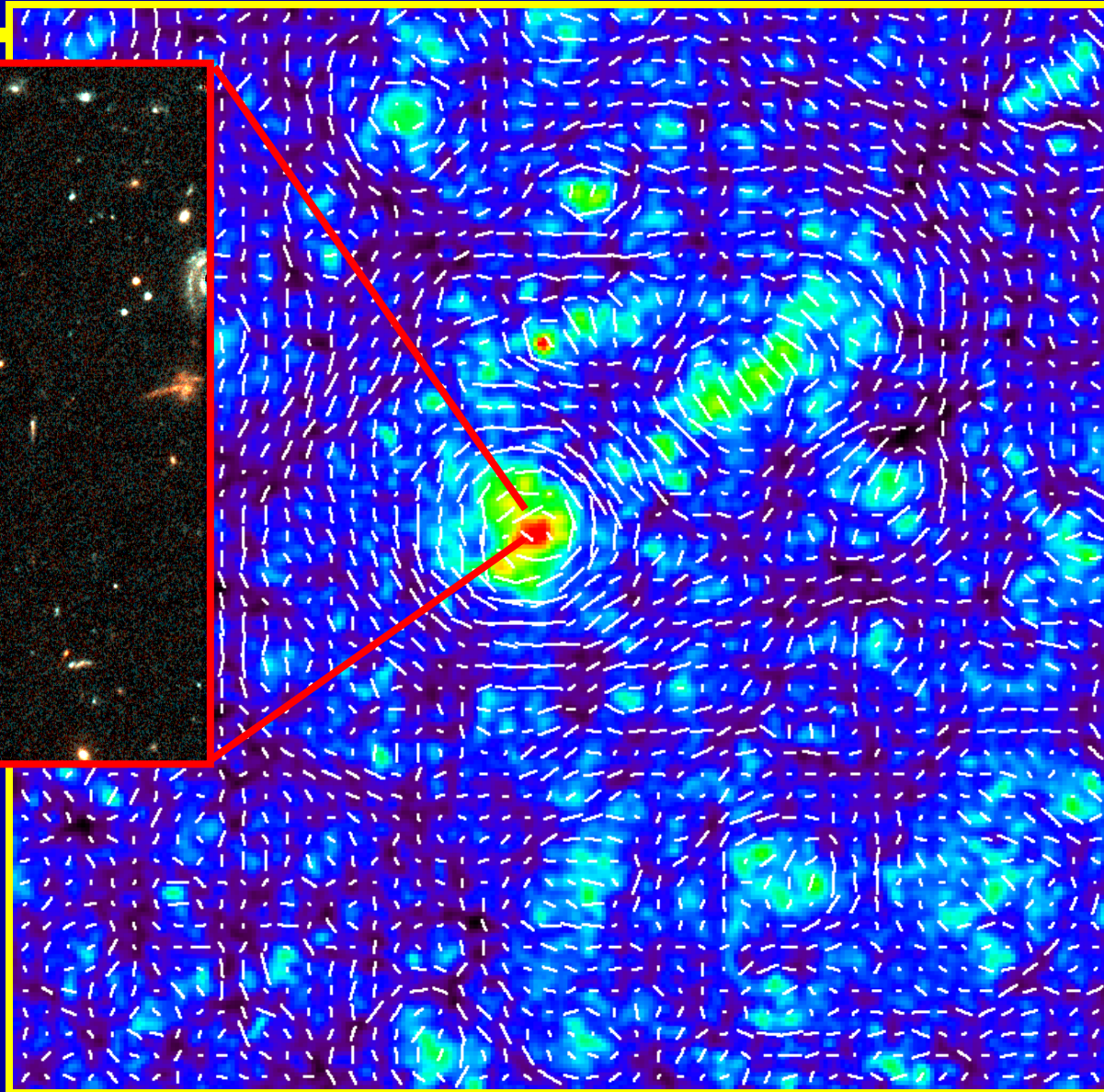
# Weak Lensing [1]: Tangential Shearing



Cluster  $z = 0.77$ ; Arc  $z = 4.89$ :  
Photo from H. Yee (HST/ACS)

**Shear to mass inversion**

$$\kappa = \Delta^{(2)^{-1}} \left( \partial^i \partial^j \Gamma_{ij} \right)$$



Simulated 3x3 degree field (Hamana 02)

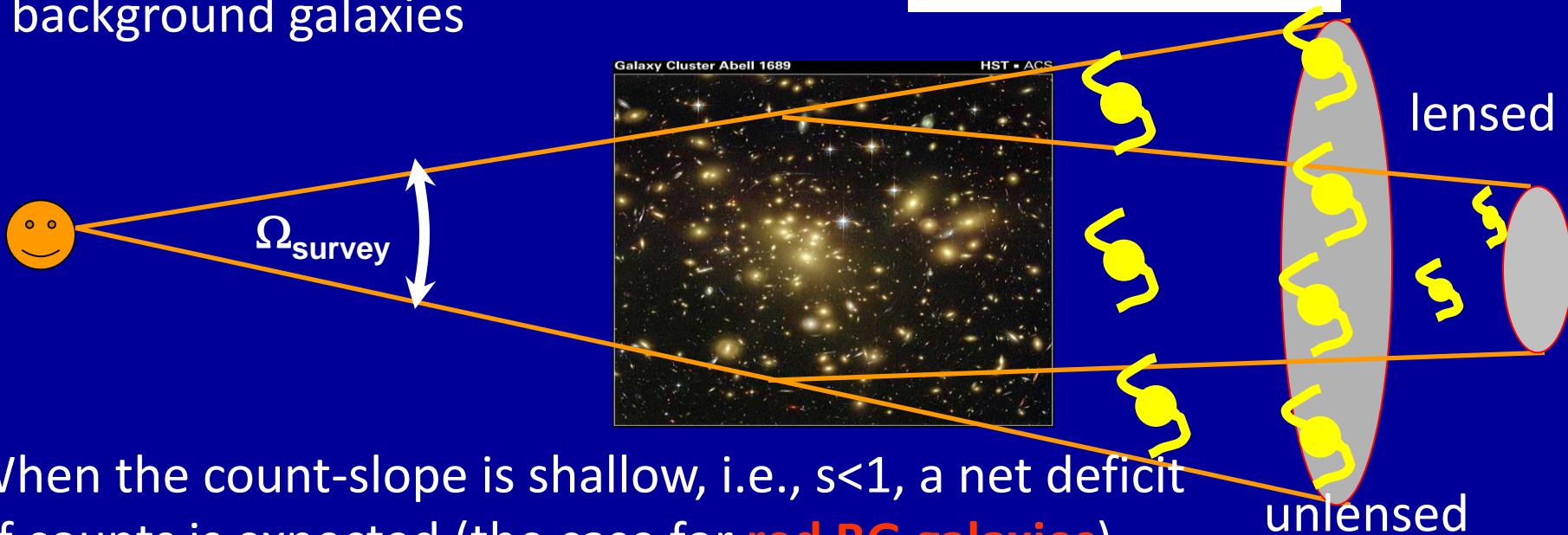
# Weak Lensing [2]: Magnification Bias

**Magnification bias:** Lensing-induced fluctuations in the background number density field (Broadhurst, Taylor, & Peacock 1995)

$$\frac{\delta n(\boldsymbol{\theta})}{n_0} = \mu^{s-1}(\boldsymbol{\theta}) - 1 \approx 2(s-1)\kappa(\boldsymbol{\theta})$$

with unlensed Luminosity Function of background galaxies

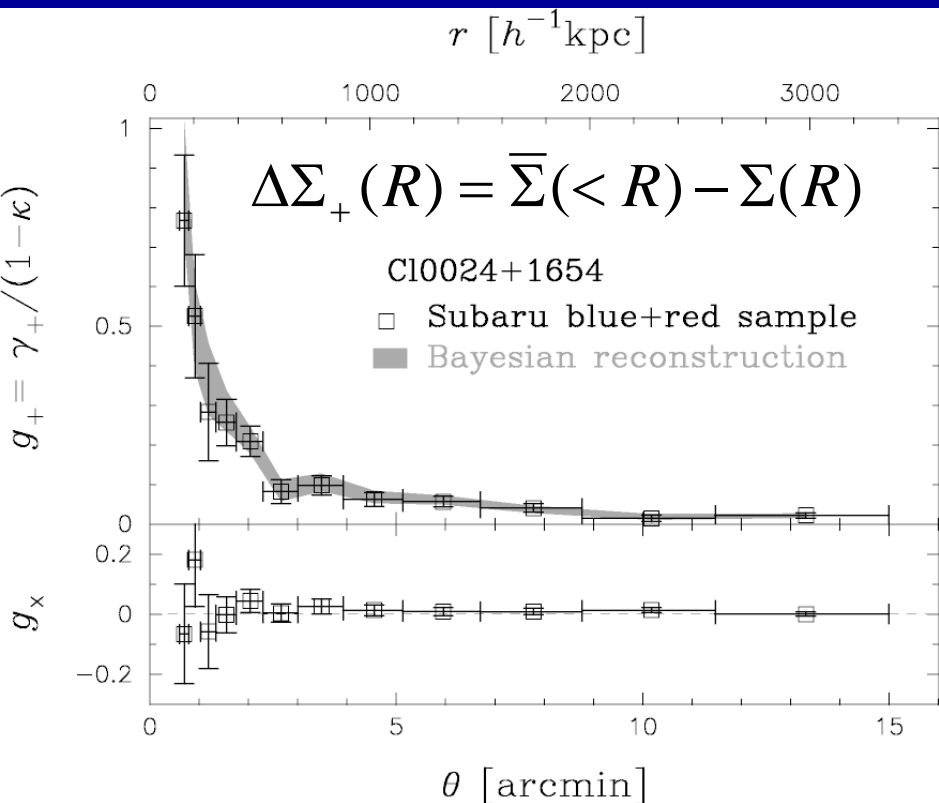
$$n_0(> F) \propto F^{-s}$$



When the count-slope is shallow, i.e.,  $s < 1$ , a net deficit of counts is expected (the case for **red BG galaxies**)

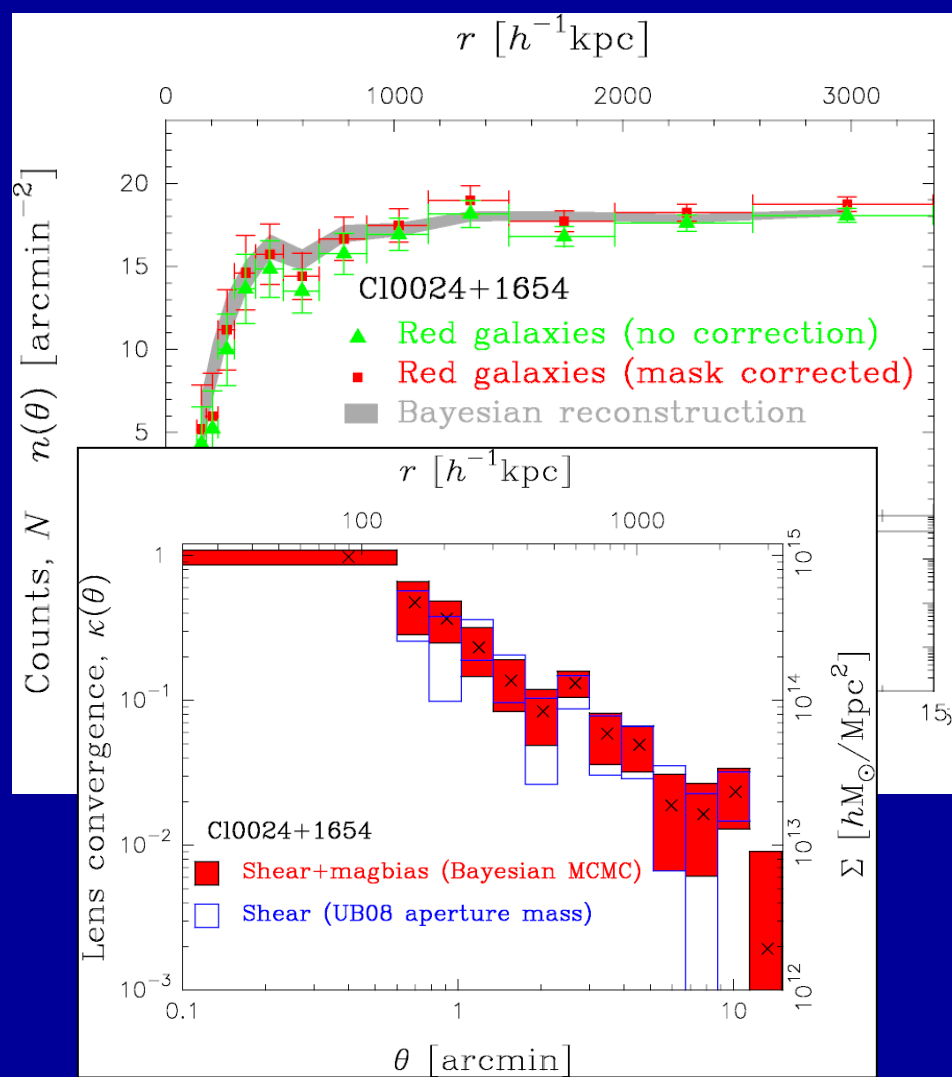
# Weak-Lensing Shear and Magnification

Tangential shear radial profile



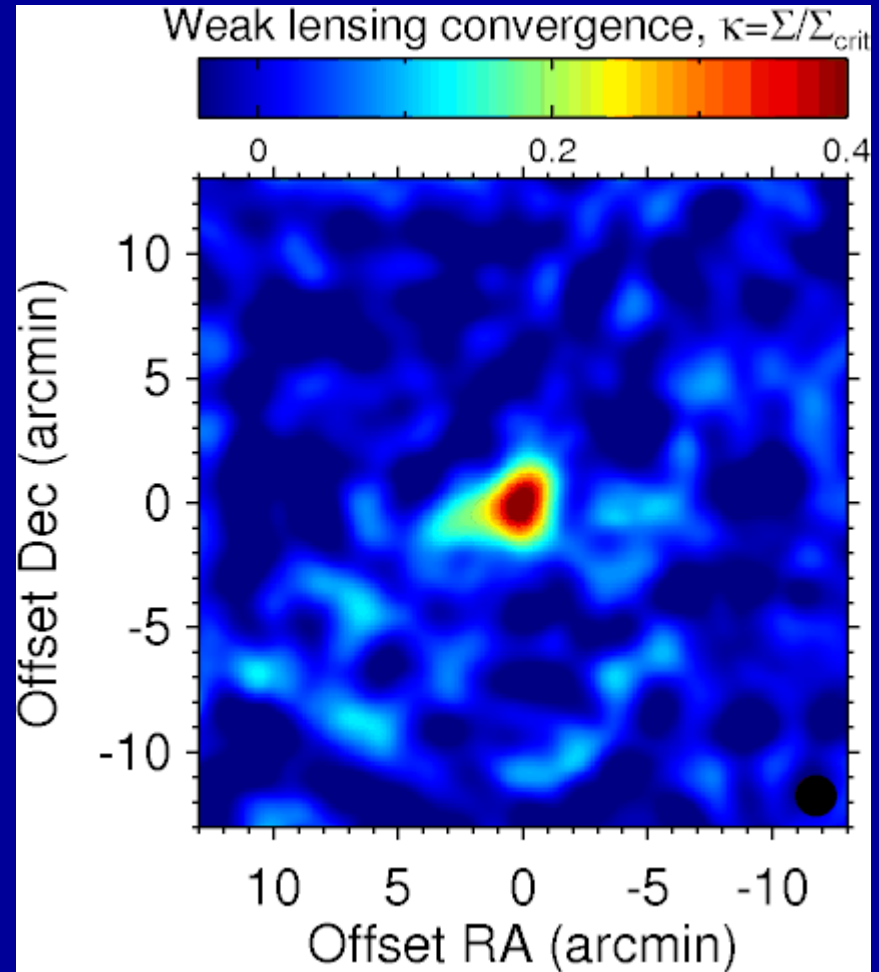
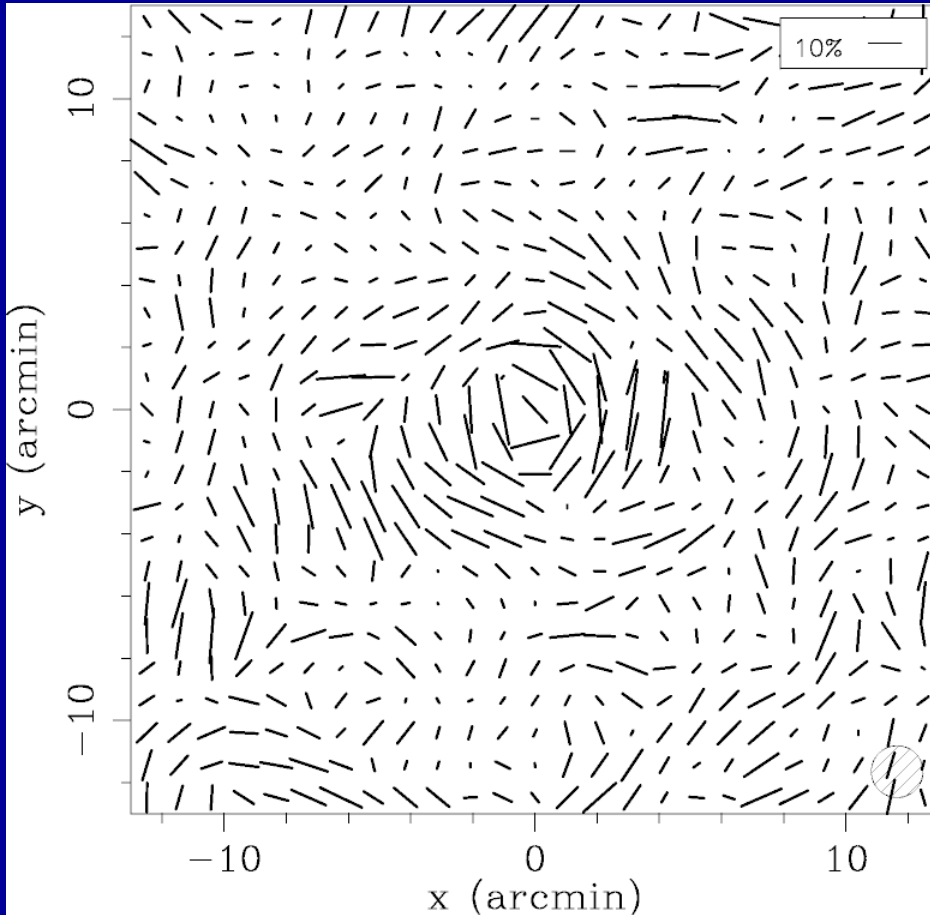
A unique mass profile solution ( $\Sigma$ ) can be obtained from joint WL shear + magnification profiles:  
Umetsu+2011a

Number counts (magnification bias)



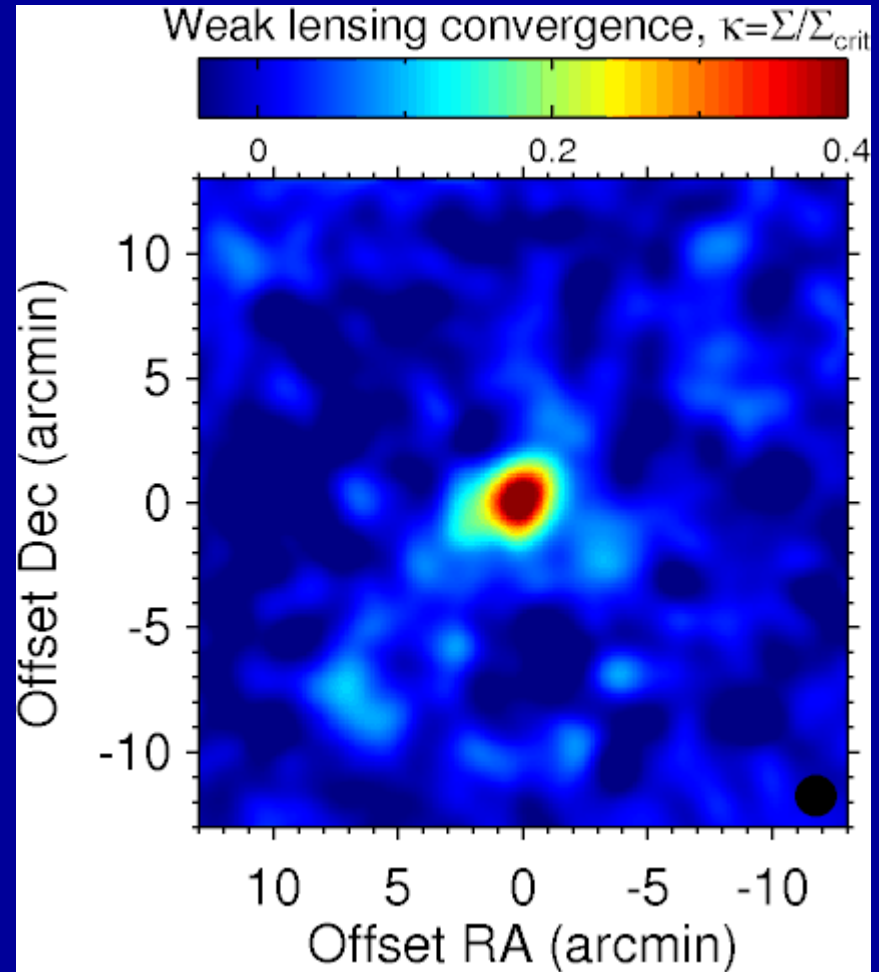
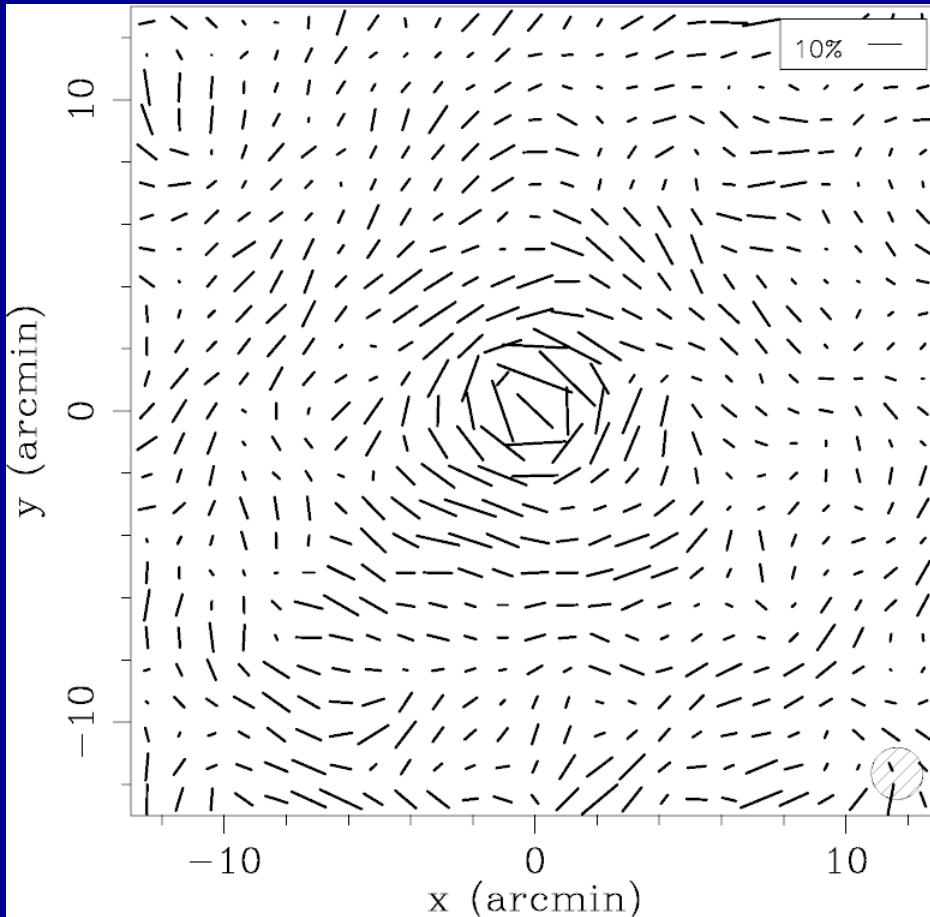
# Weak Lensing [3]: Power of Stacking Analysis

Subaru shear data: **N=1**



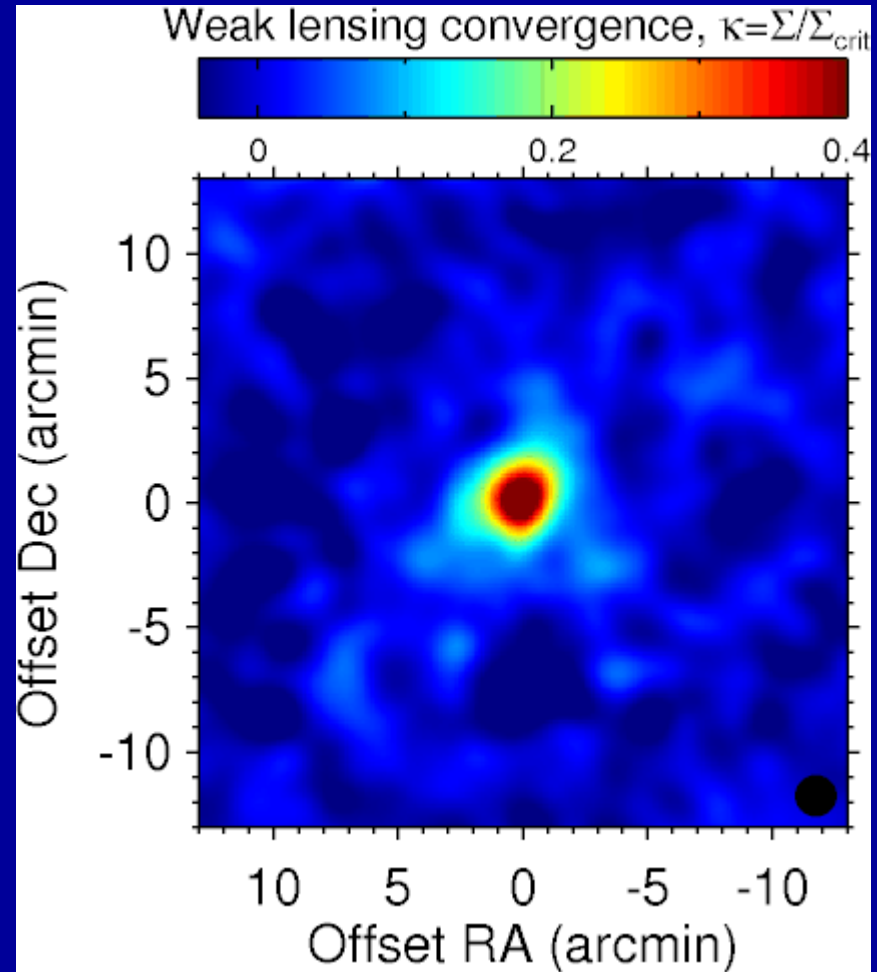
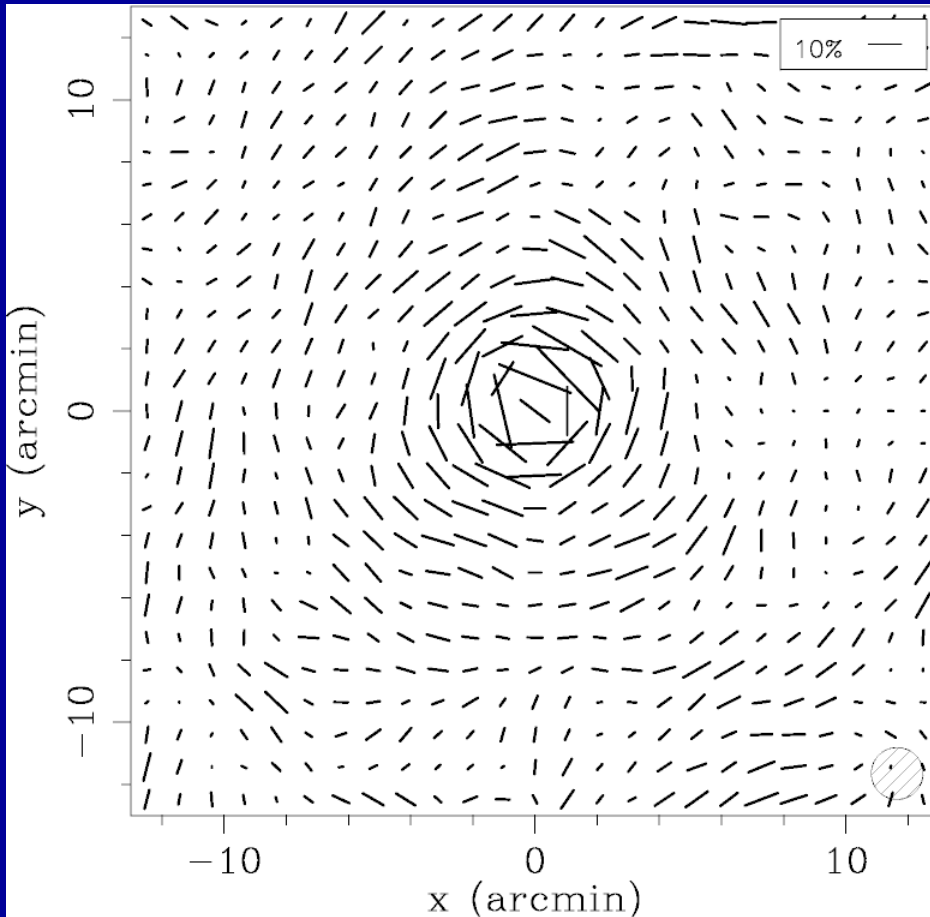
# Weak Lensing [3]: Power of Stacking Analysis

Subaru shear data: **N=2**



# Weak Lensing [3]: Power of Stacking Analysis

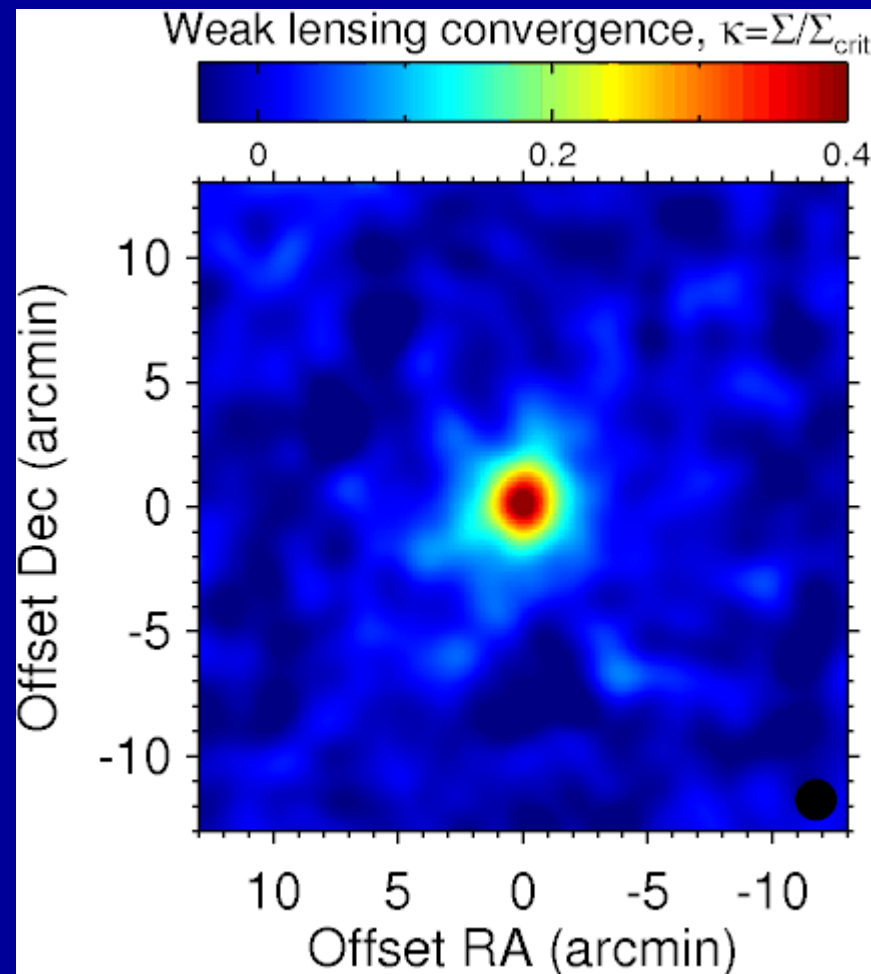
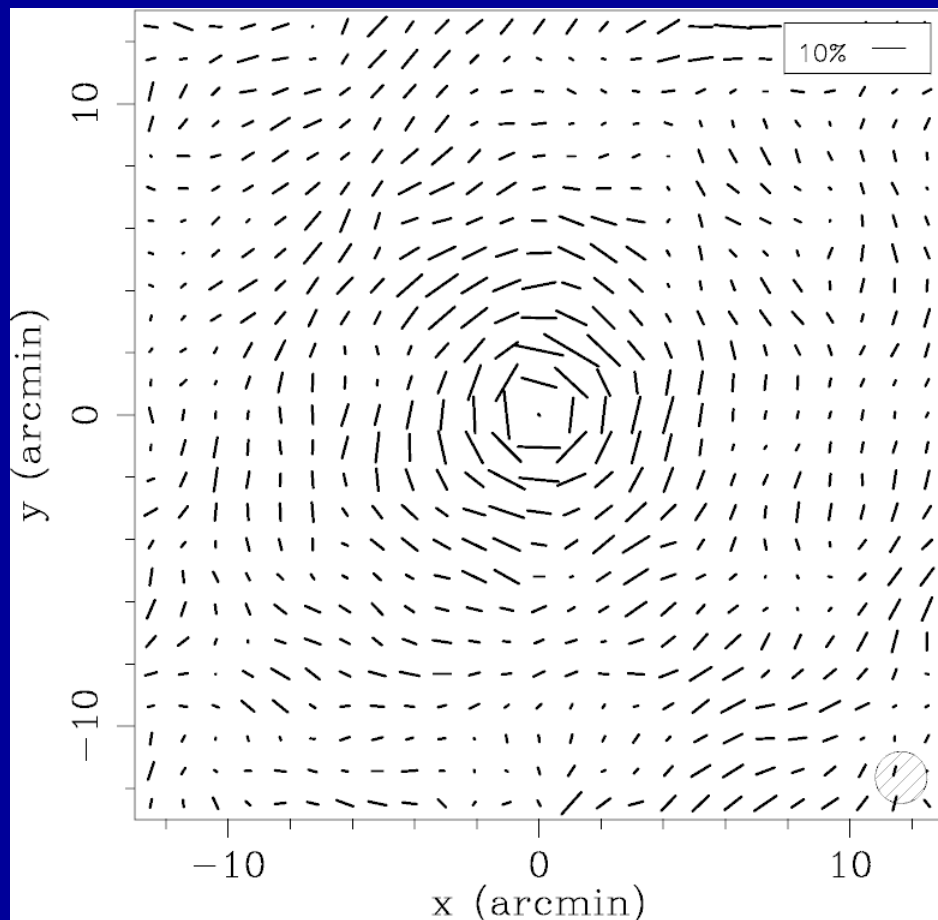
Subaru shear data: **N=3**





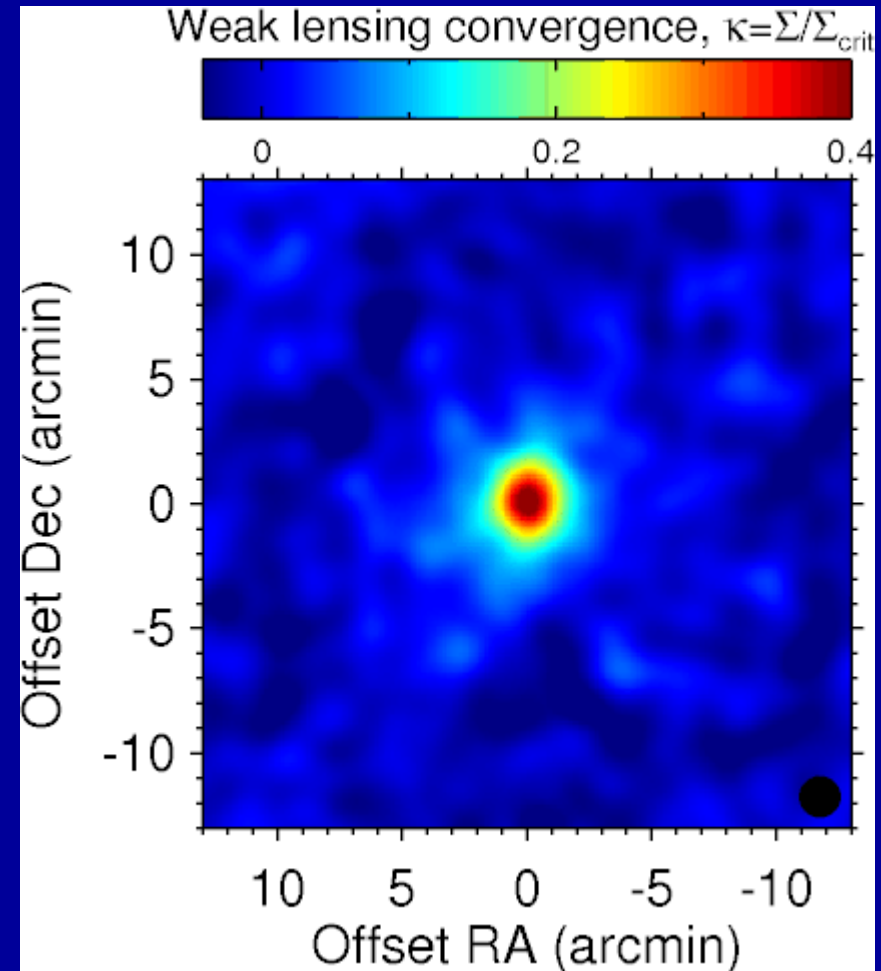
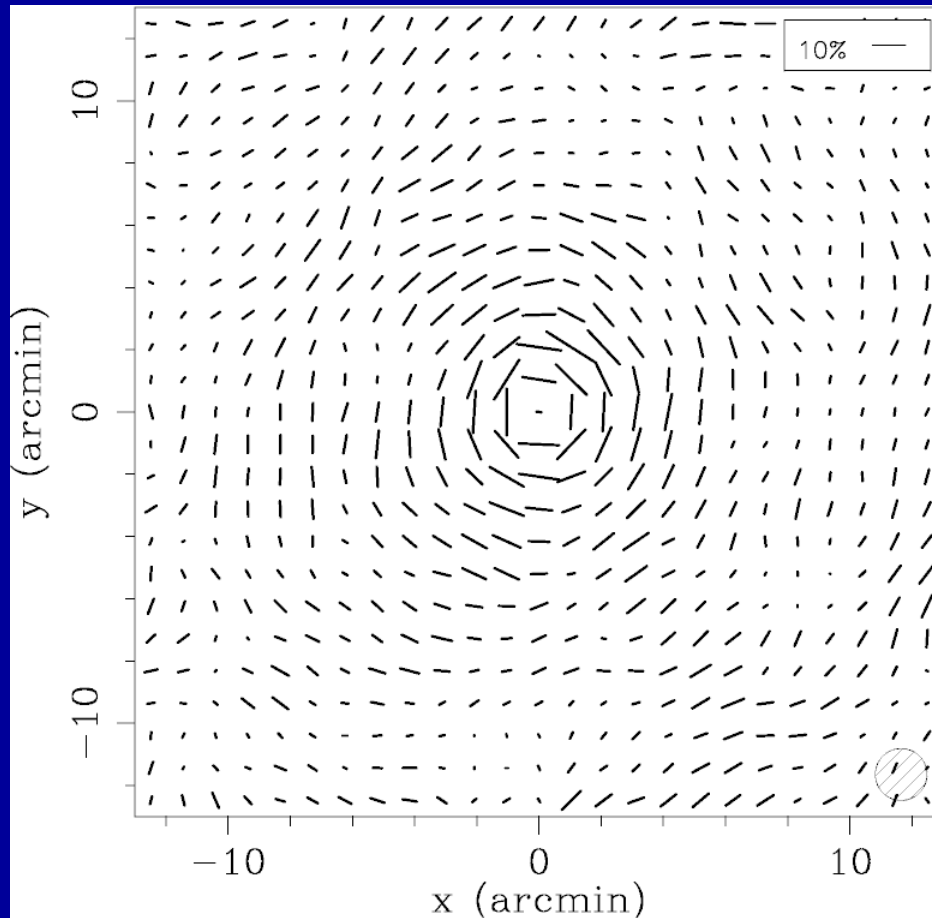
# Weak Lensing [3]: Power of Stacking Analysis

Subaru shear data: **N=4**



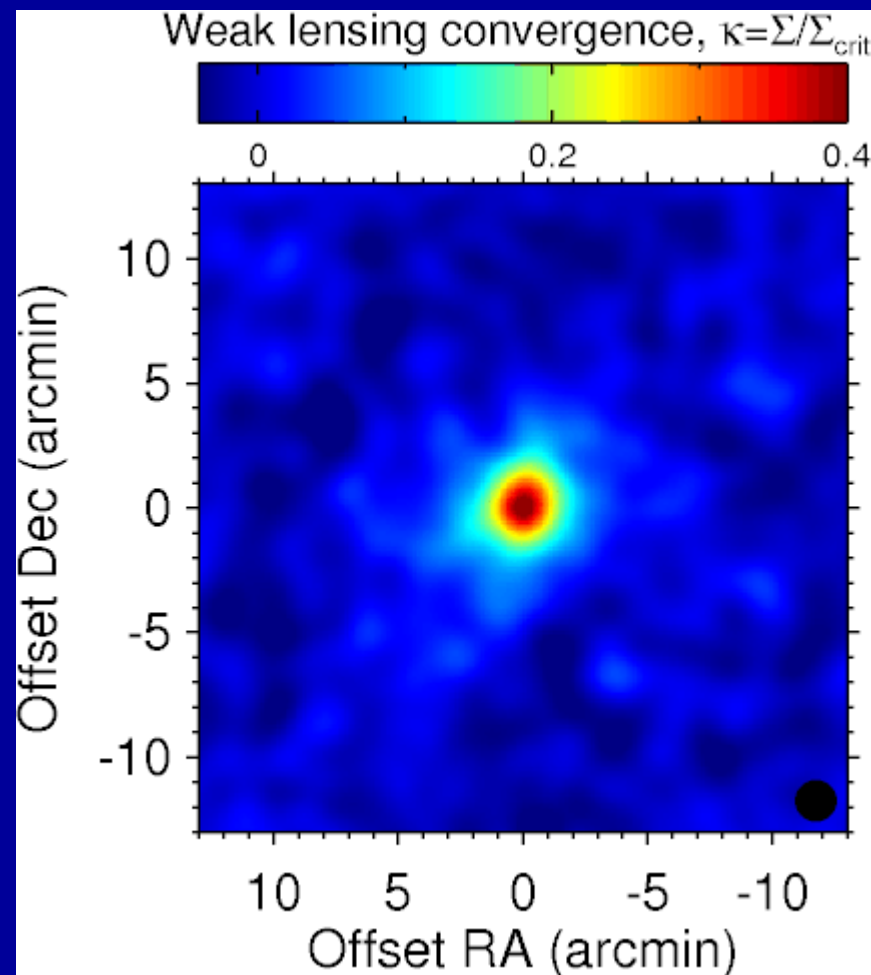
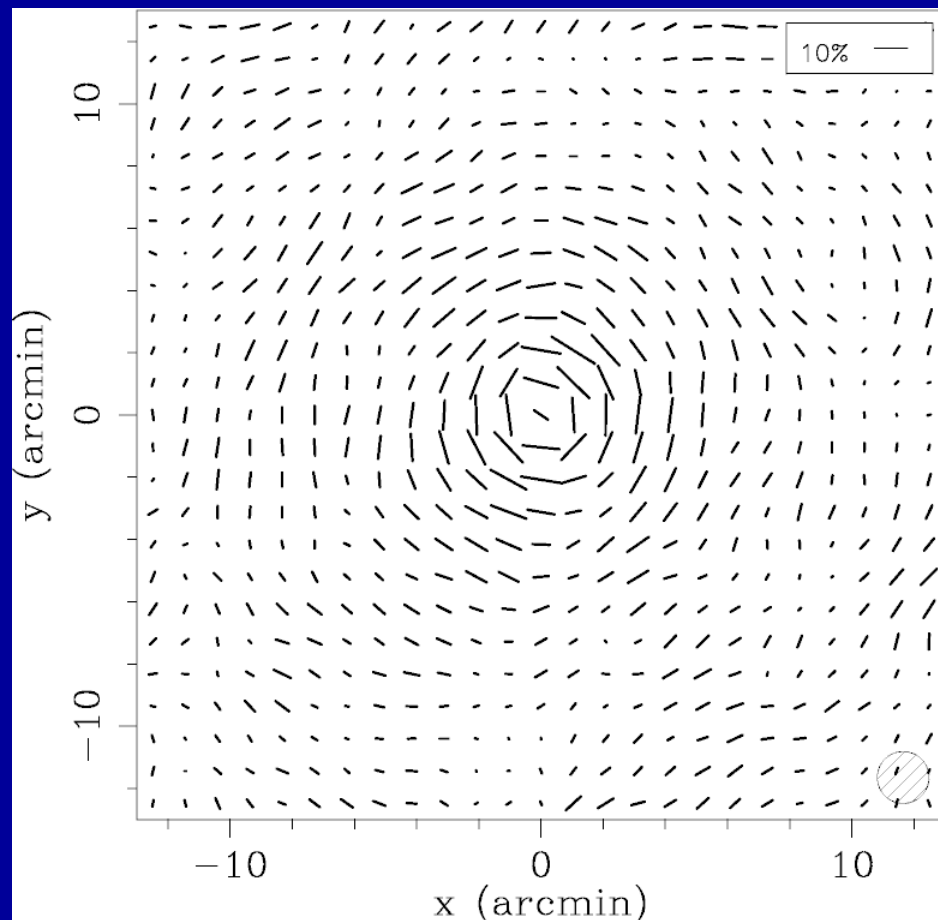
# Weak Lensing [3]: Power of Stacking Analysis

Subaru shear data: **N=5**



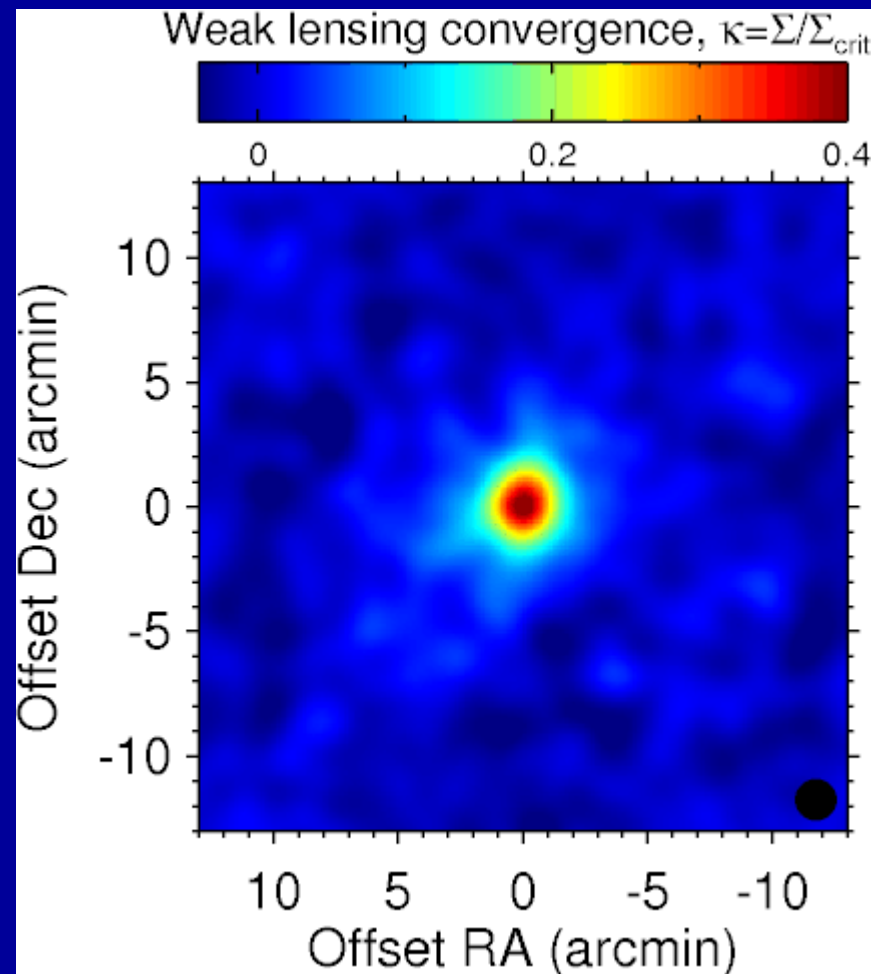
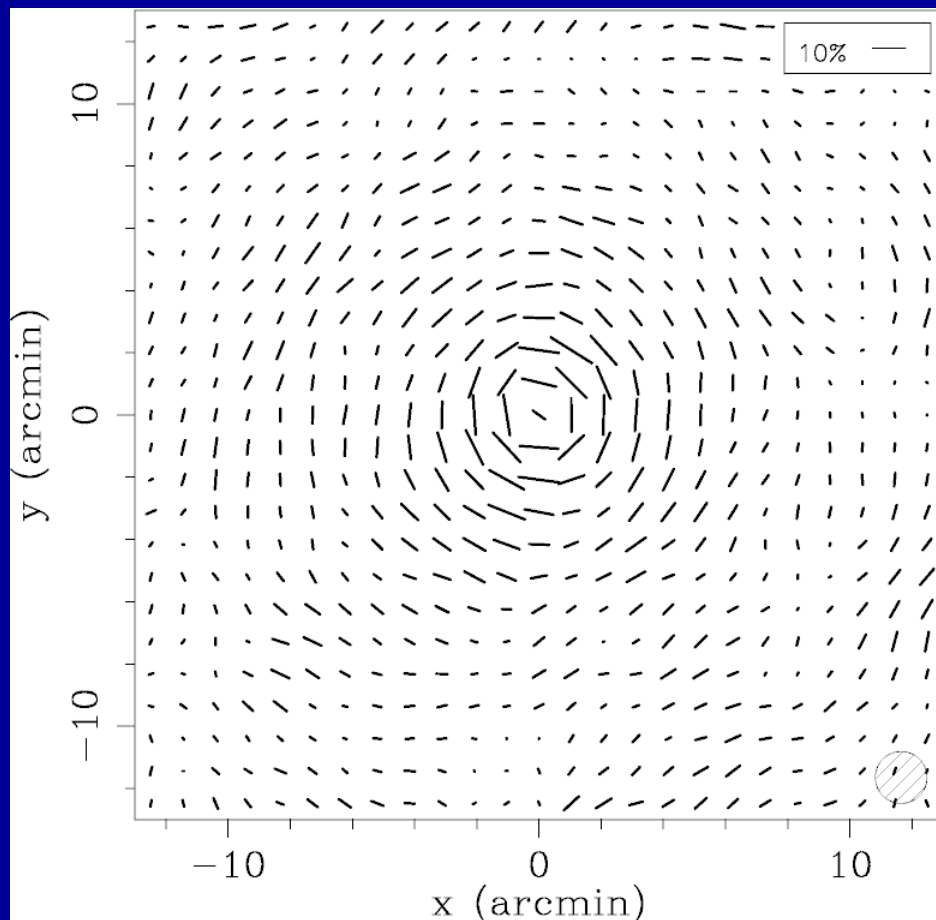
# Weak Lensing [3]: Power of Stacking Analysis

Subaru shear data: **N=6**



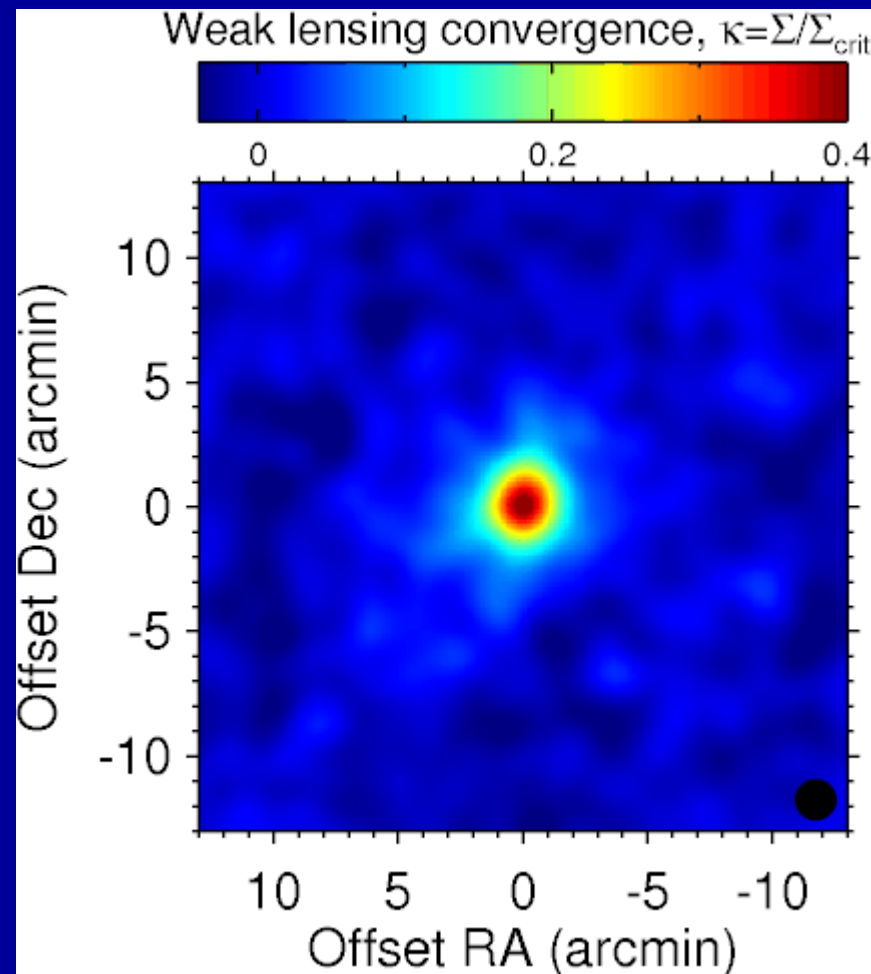
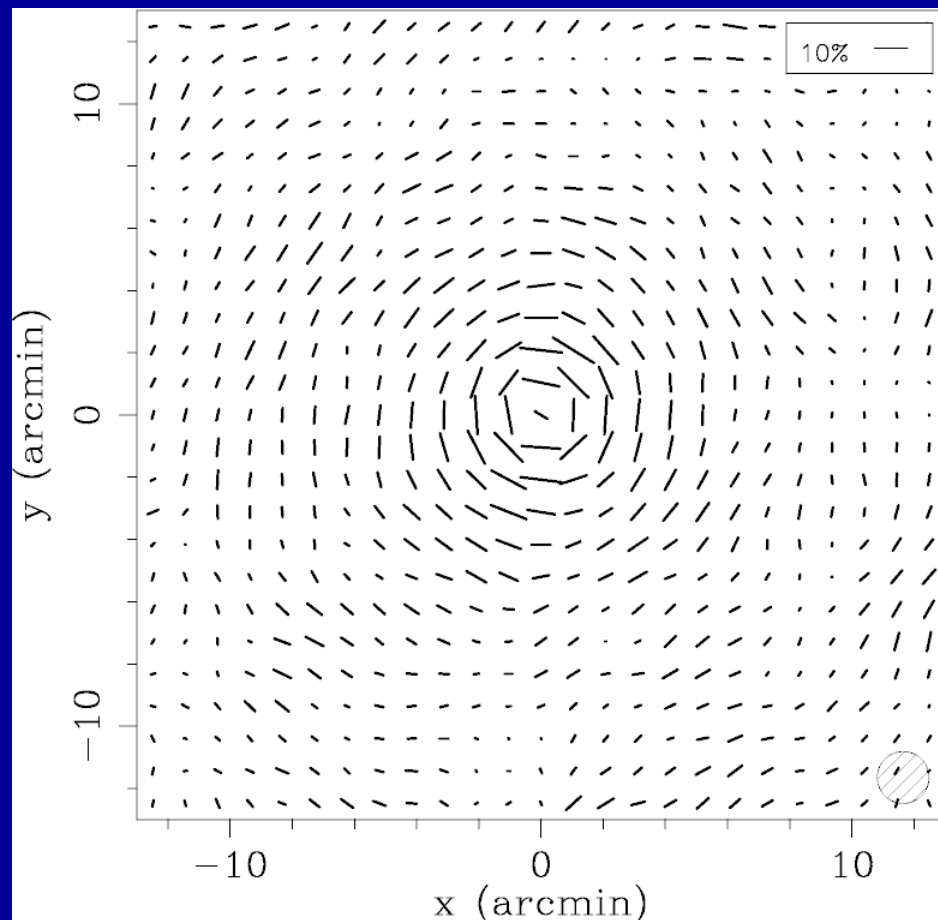
# Weak Lensing [3]: Power of Stacking Analysis

Subaru shear data: **N=7**



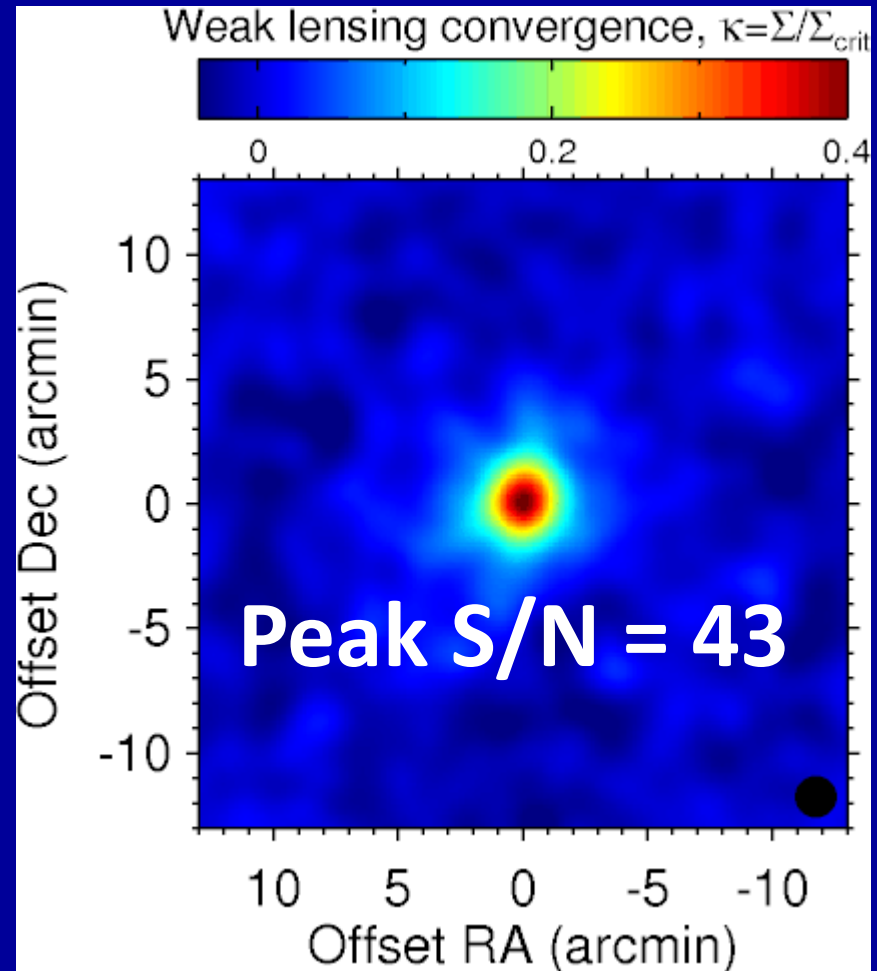
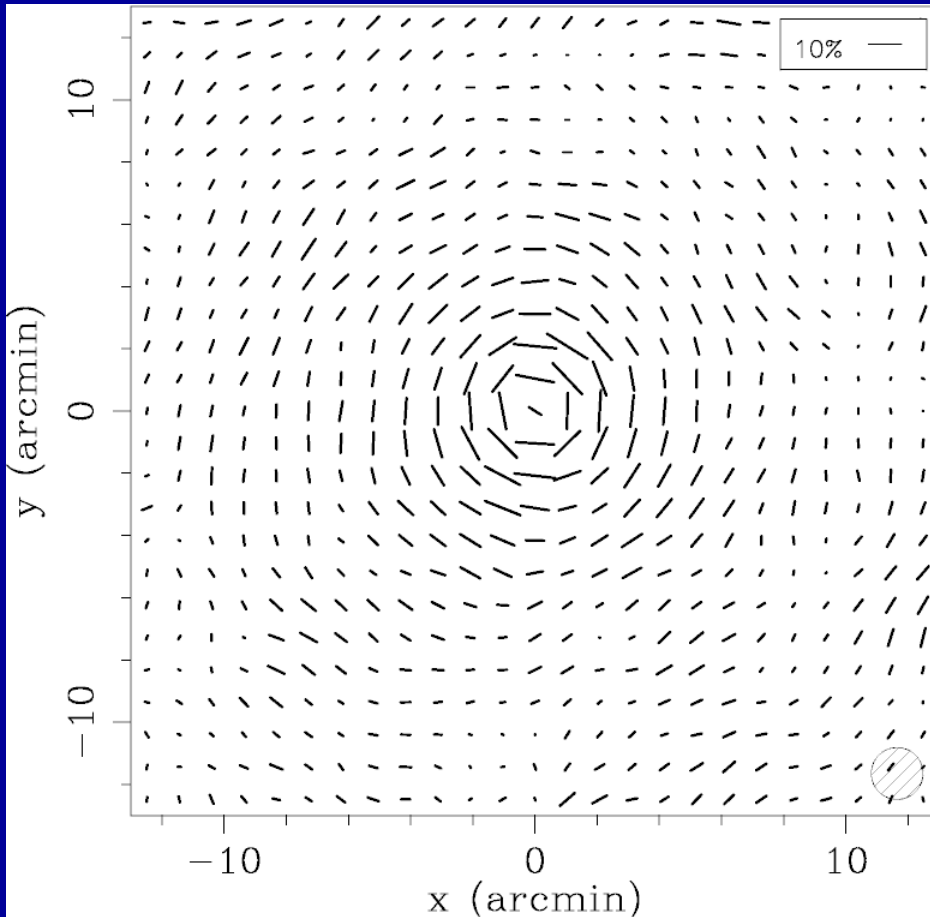
# Weak Lensing [3]: Power of Stacking Analysis

Subaru shear data: **N=8**



# Weak Lensing [3]: Power of Stacking Analysis

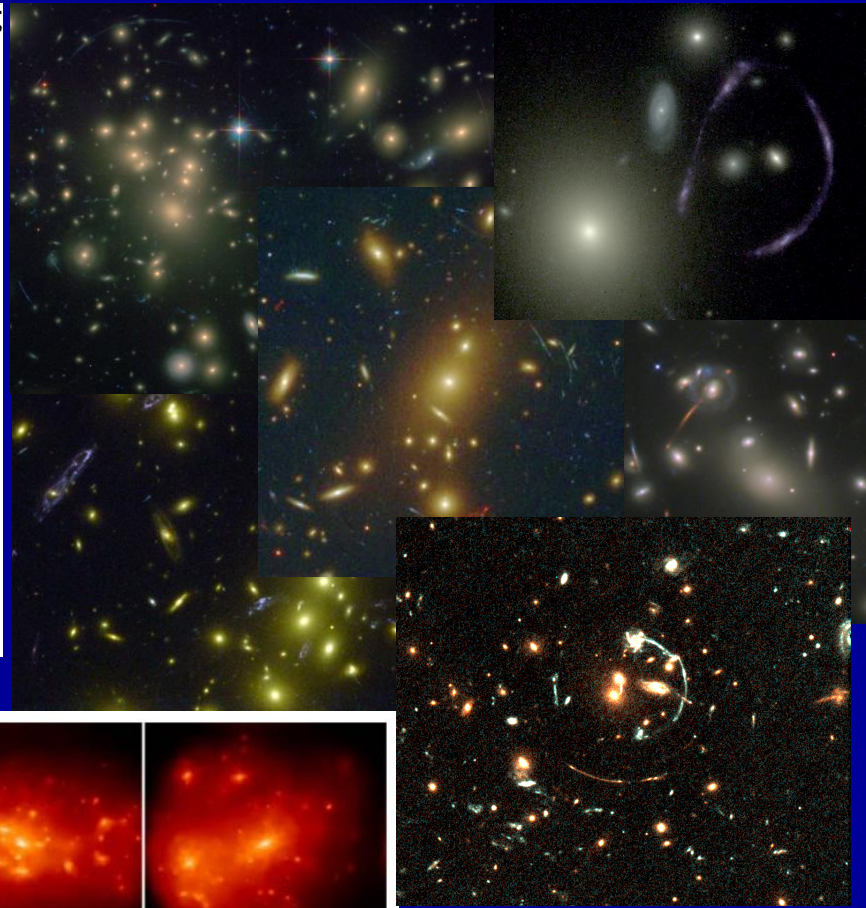
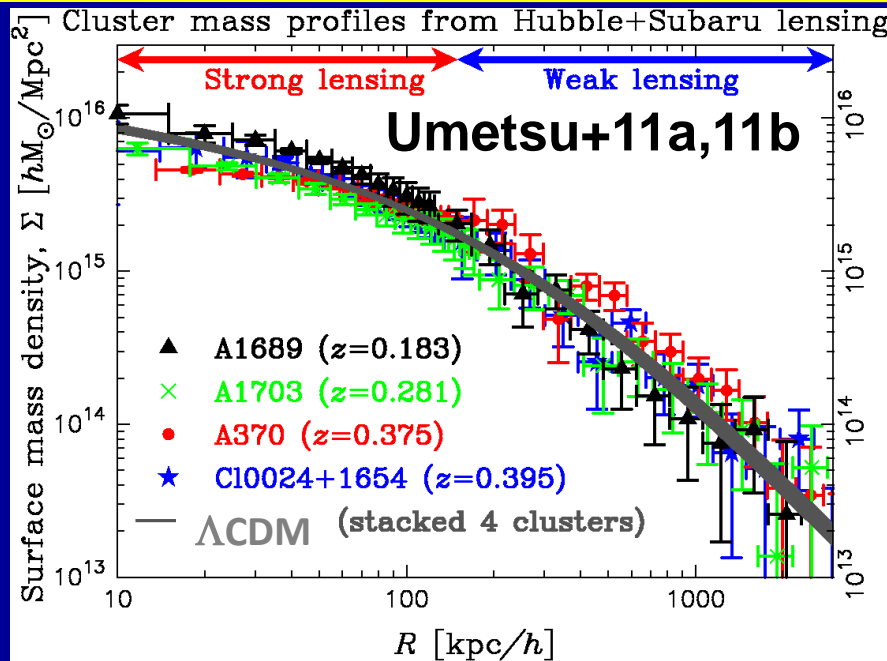
Subaru shear data: **N=9**



Incoherent contributions, such as asphericity, substructures, cosmic shear (uncorrelated LSS contributions), as well as intrinsic shape noise, being averaged out by stacking clusters, due to the isotropic nature of the universe

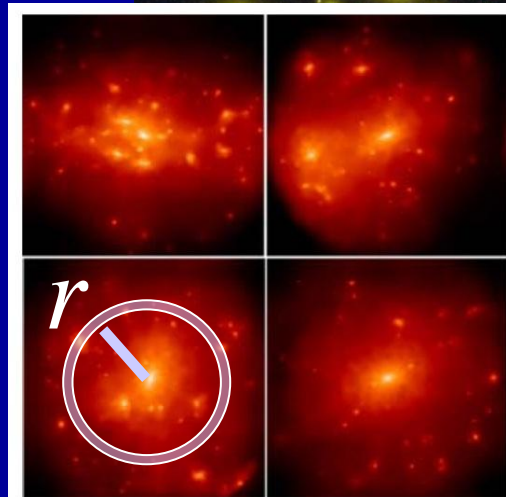
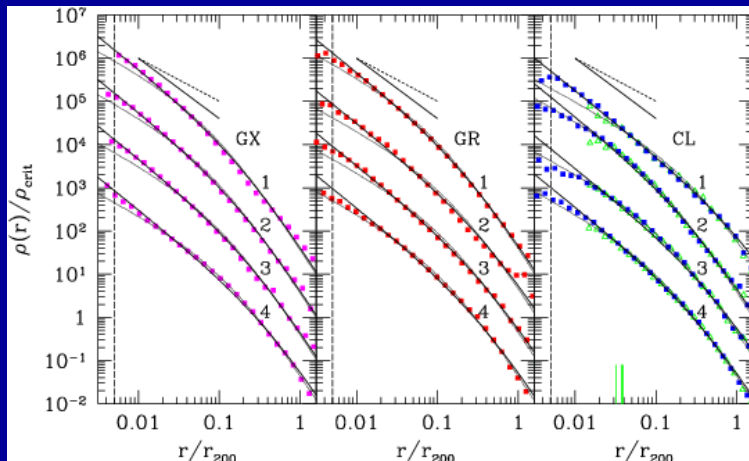
# 3. Radial Mass Profiles of Galaxy Clusters: LCDM Predictions vs. Lensing Observations

Data



$\Lambda$ CDM theory

CDM universal density profile (NFW)

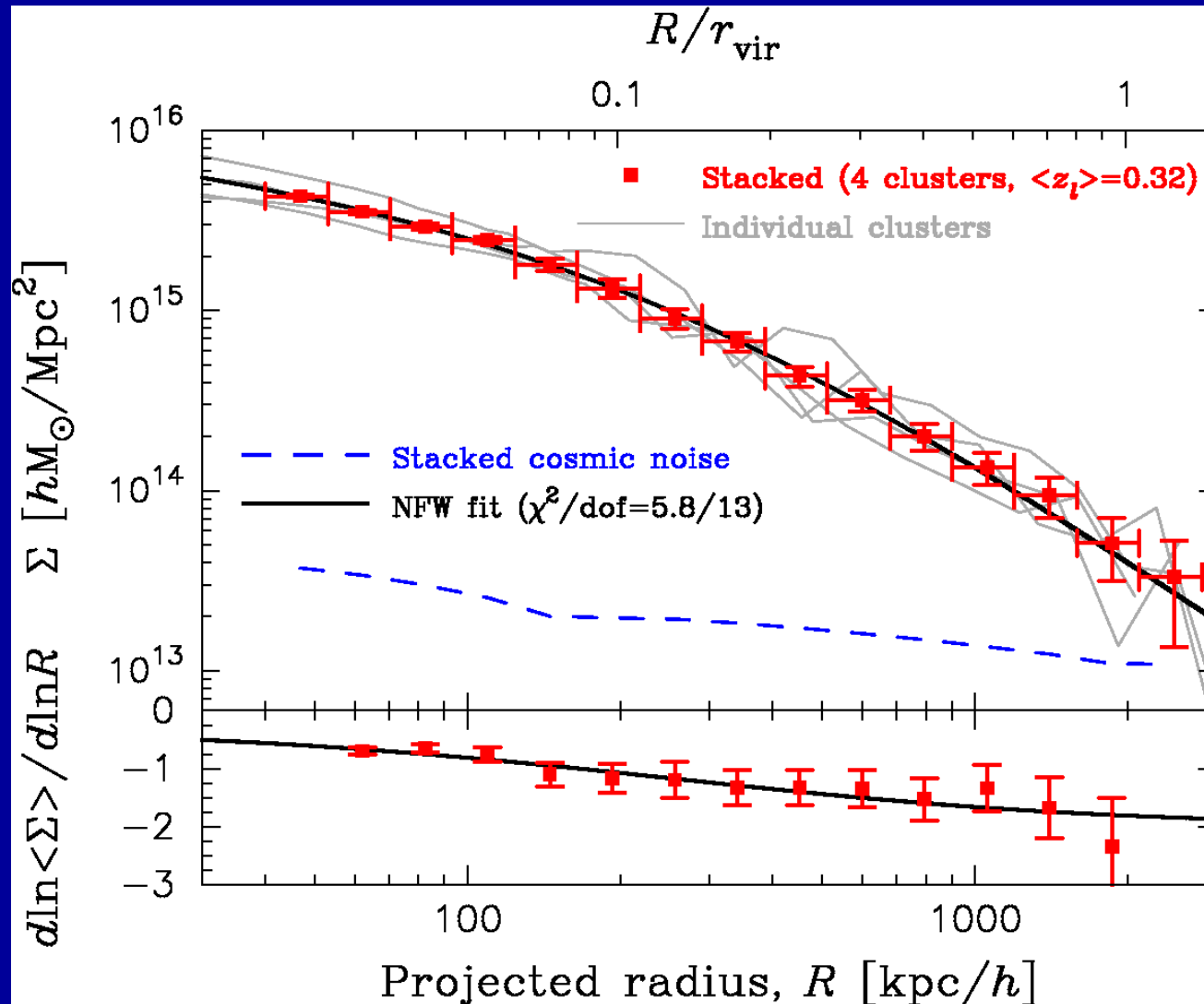


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(1) Testing the mass profile “shape”



# 58 $\sigma$ cluster mass profile averaged from the highest-quality SL+WL data



Stacking clusters by

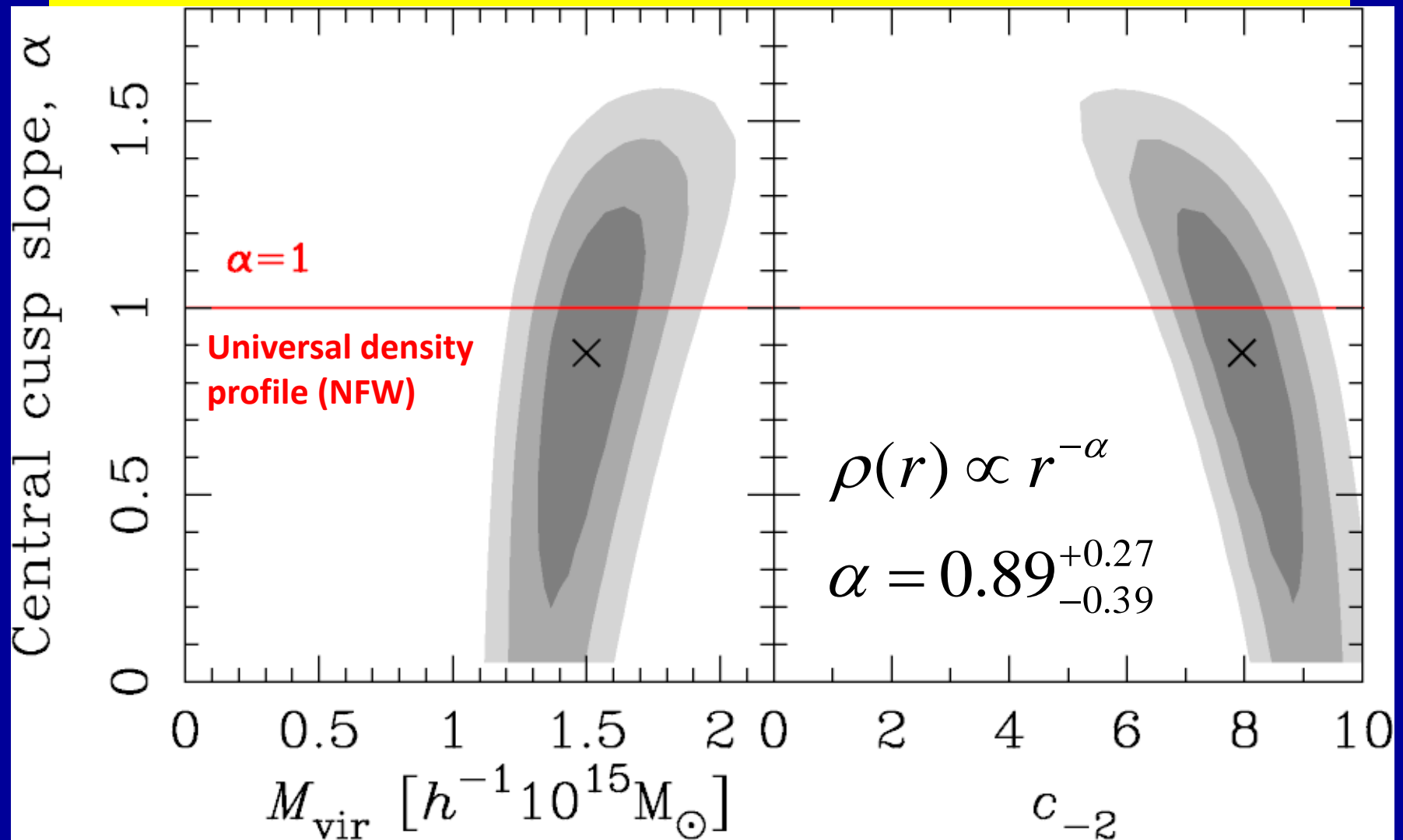
$$\langle \Sigma \rangle = \left( \sum_n C_n^{-1} \right)^{-1} \left( \sum_n C_n^{-1} \Sigma_n \right)$$

2-parameter universal profile gives an excellent fit over  $\sim 2$ -decades of radius

SIS model is rejected at  $>60\sigma$  significance

Lensing observations are consistent with that, DM is non-relativistic (cold) and effectively collisionless on the relevant scales.

# Constraint on Central Cusp Slope



Slightly shallower than, but consistent with, the CDM universal density profile (cf. Navarro et al. 2010)

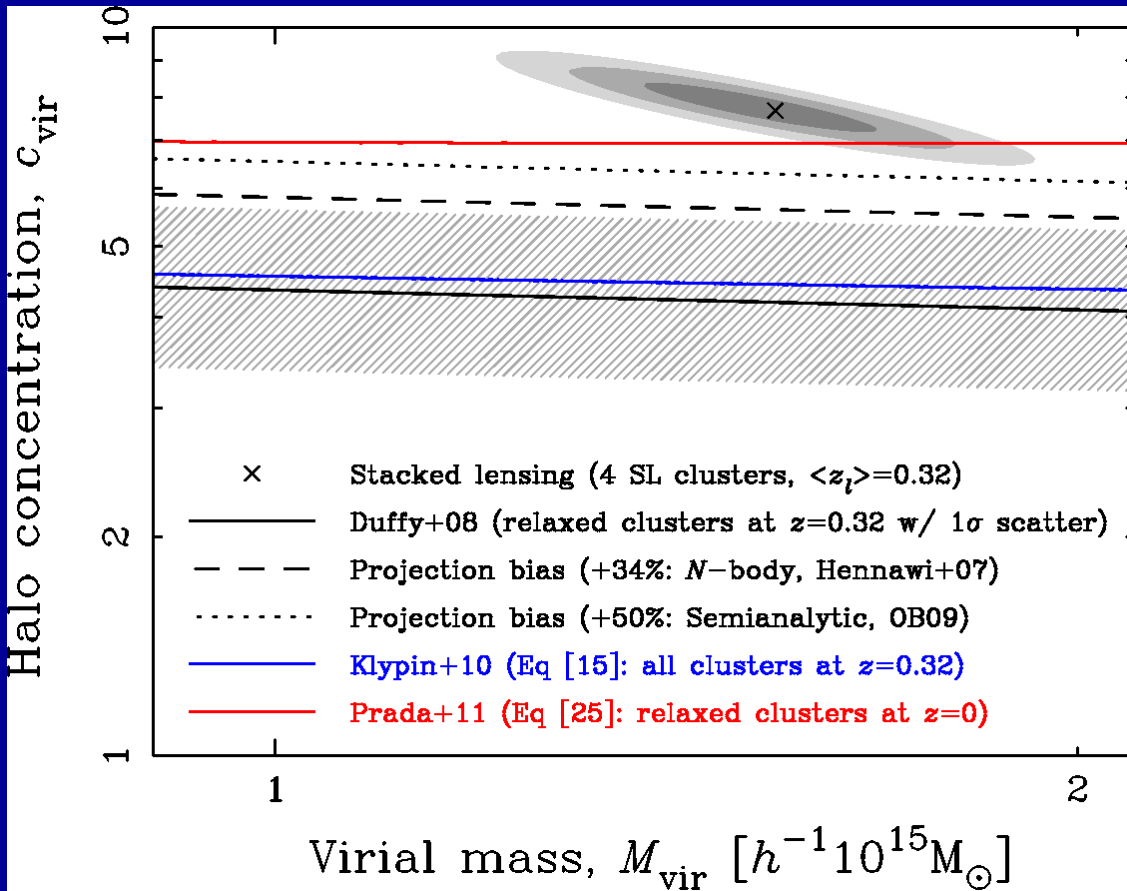
Umetsu et al. 2011b

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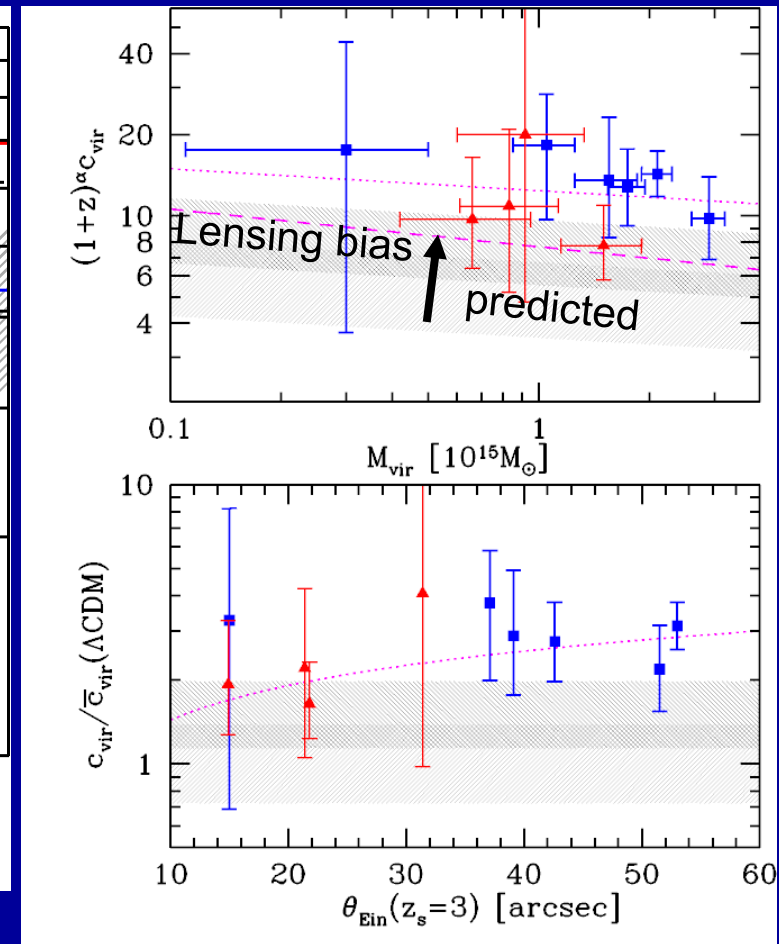
(2) Testing the mass profile “normalization”

# Halo central density somewhat higher than LCDM predictions??

Observed lensing clusters are more concentrated than LCDM?



Umetsu et al. 2011b

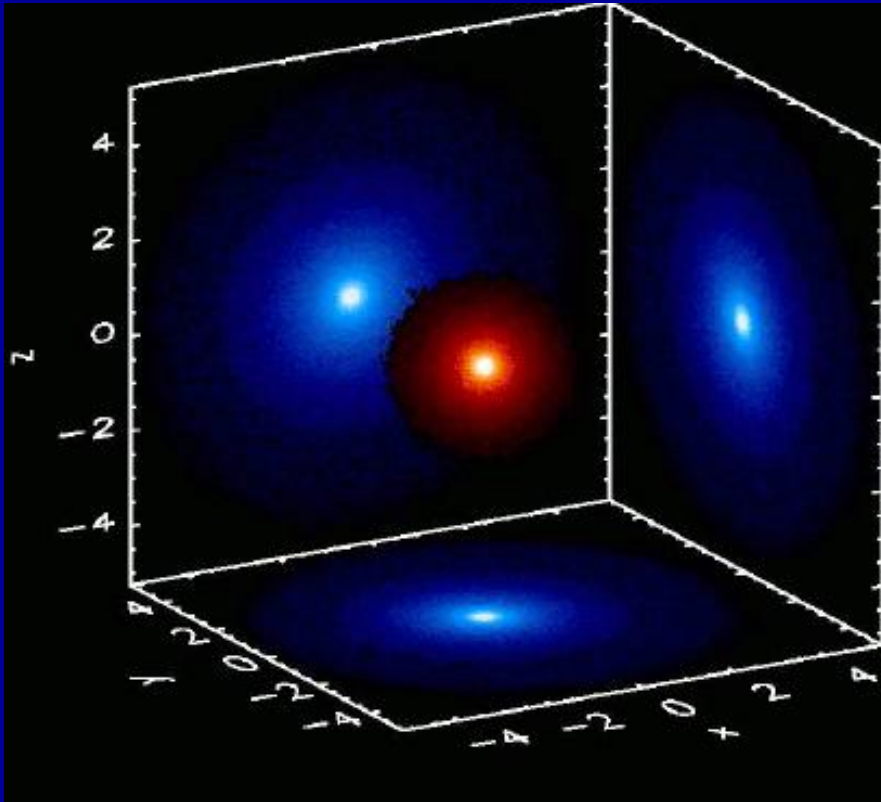


Oguri et al. 2010

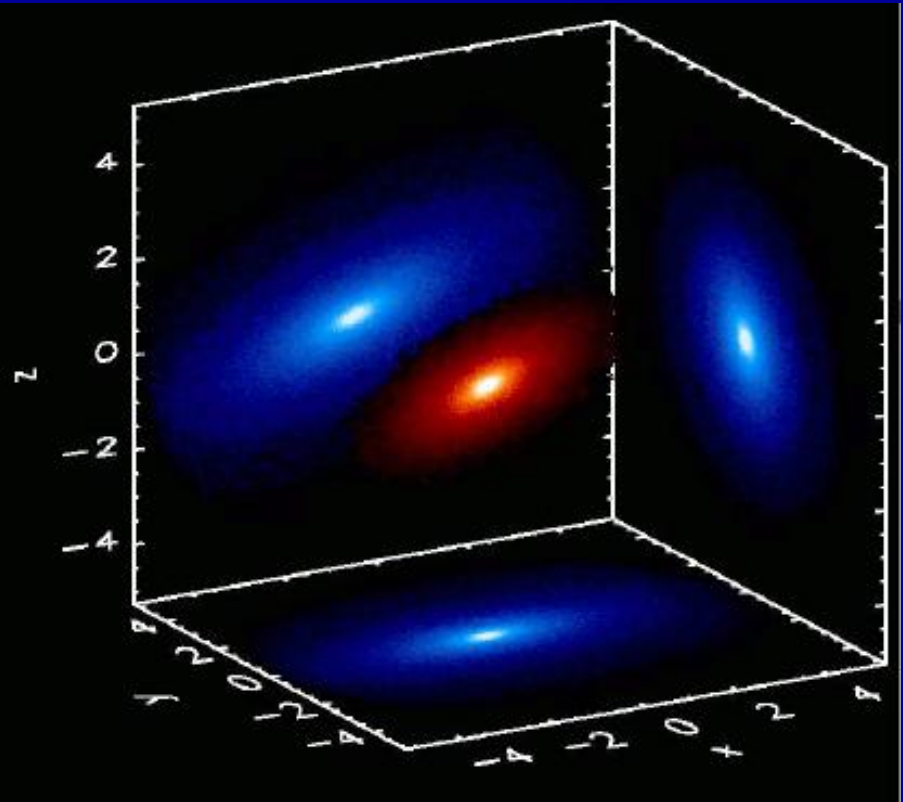
Broadhurst, Umetsu et al. 2008

# Projection Effect by Halo Triaxiality

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**Spherical**



**Triaxial (prolate)**

# Possible explanations for observed high concentrations

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- **Lensing projection and selection bias?**

- Selection bias towards intrinsically high- $c$  halos (Hennawi +07)
- Triaxial orientation bias (Oguri & Blandford 09)
- Significant (30-50%) but probably not sufficient

- **Clusters formed earlier than in LCDM?**

- Early Dark Energy (Sadeh & Rephaeli 08; Grossi & Springel 09) or primordial non-Gaussianity?

- **N-body simulations**

- High-mass clusters are very rare objects – only 8 relaxed halos with  $M > 10^{15} M_{\text{sun}}/h$  found in the Millennium simulation (500Mpc/h box), suffering from cosmic variance.
- The latest simulation predicts >50% higher concentrations than previous simulations for high-mass clusters (Prada+11, arXiv:1104.5130).

# Summary

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- Cluster mass profile shape reconstructed from WL+SL is fully consistent with the standard form predicted for the family of CDM models:
  - Lensing observations are consistent with that, DM is non-relativistic (negligible free-streaming scale) and effectively collisionless on astrophysical scales.
- The mass concentrations from WL+SL are high for high-mass clusters ( $M > 10^{15} M_{\text{sun}}$ ), but be consistent with LCDM if a sizable lensing-projection bias and intrinsic scatter is considered.
  - High-mass clusters formed earlier than in LCDM?
  - If the findings from the latest N-body simulation are confirmed, observations and LCDM models come closer.
- These issues will be definitively tested by the ongoing **“Cluster Lensing And Supernova survey with Hubble”** (CLASH: PI M. Postman, KU as Co-I) for a carefully-selected sample of 25 clusters with  $5\text{-}30e15M_{\text{sun}}$  ( $0.2 < z < 0.9$ ).

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**Thank you!**