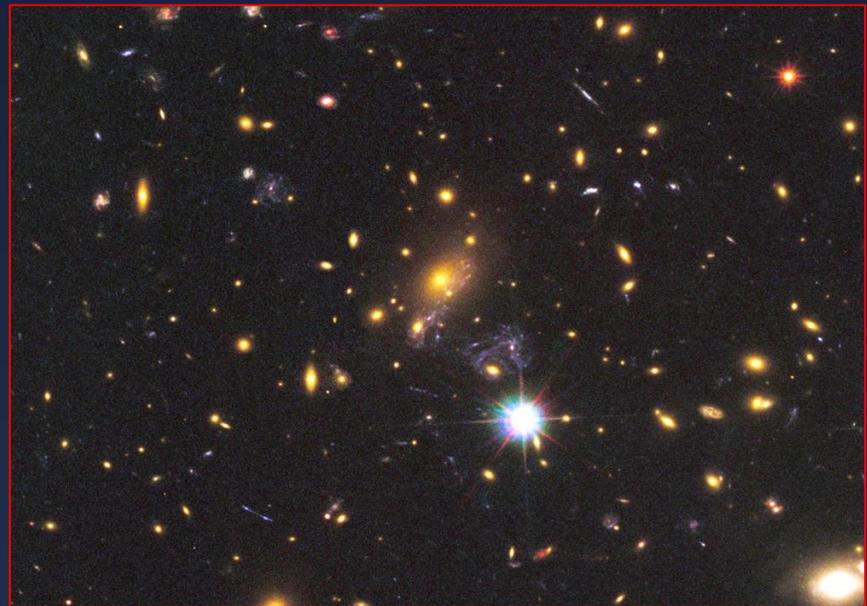
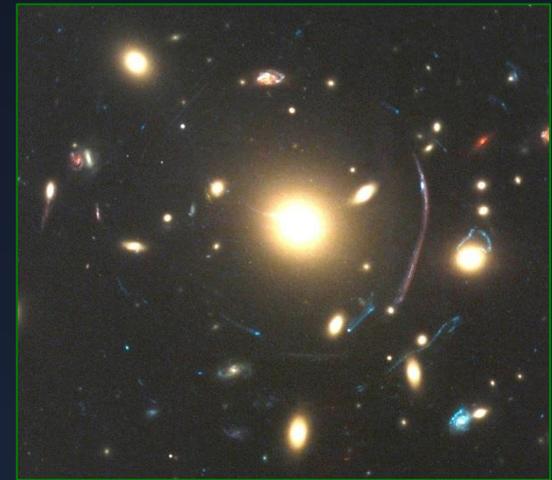


CLASH: Weak-Lensing Shear-and-Magnification Analysis of 20 Galaxy Clusters

Cluster Lensing And Supernova survey with Hubble

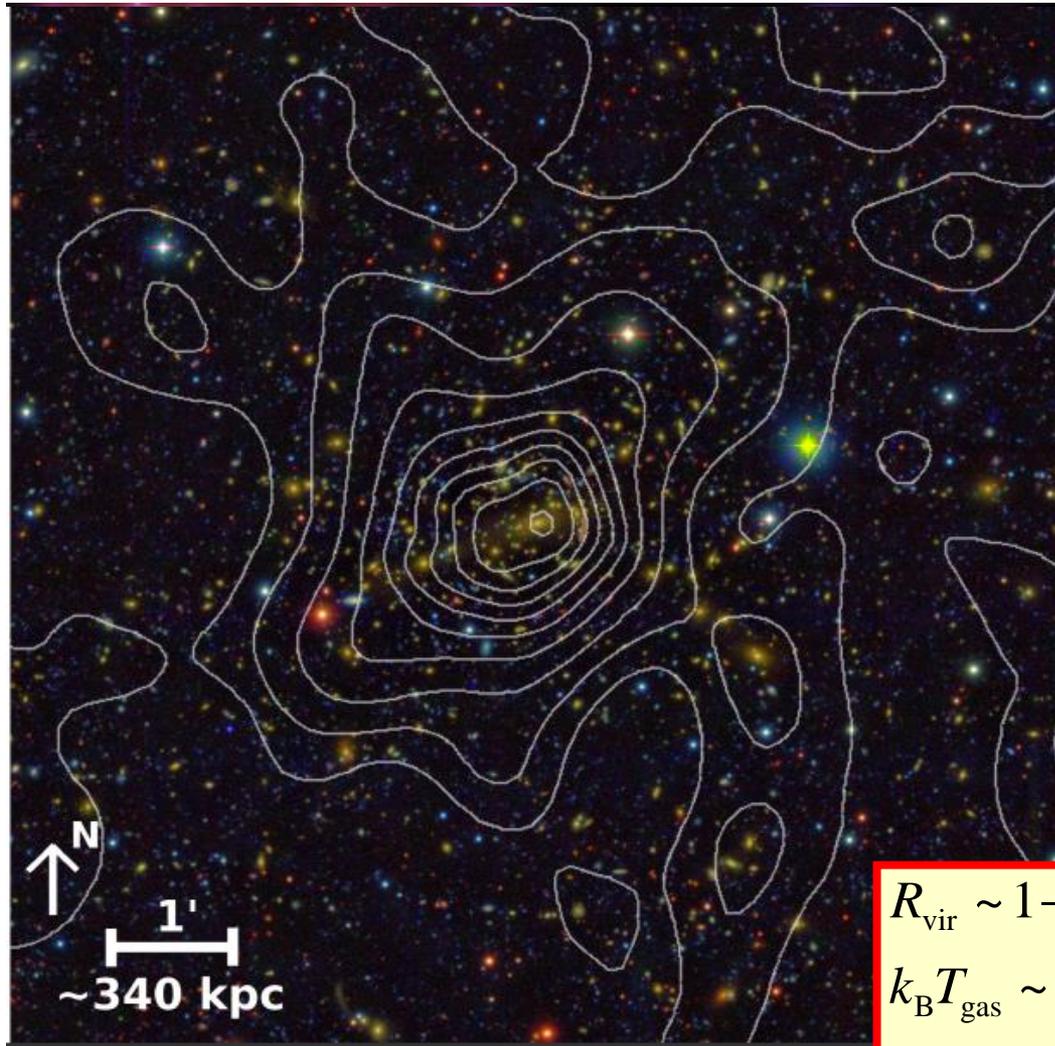


Keiichi Umetsu (ASIAA, Taiwan) with the CLASH team

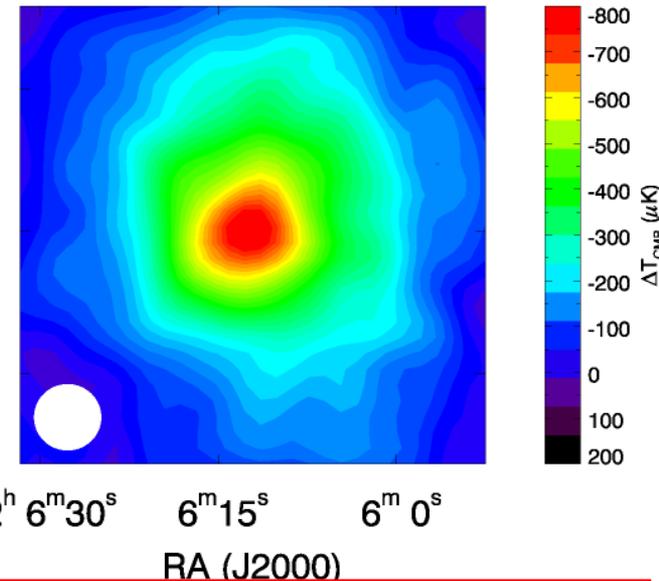
Introduction

Clusters of Galaxies

Clusters: the largest cosmic halos composed of 100-1000 galaxies.



tSZE by Bolocam

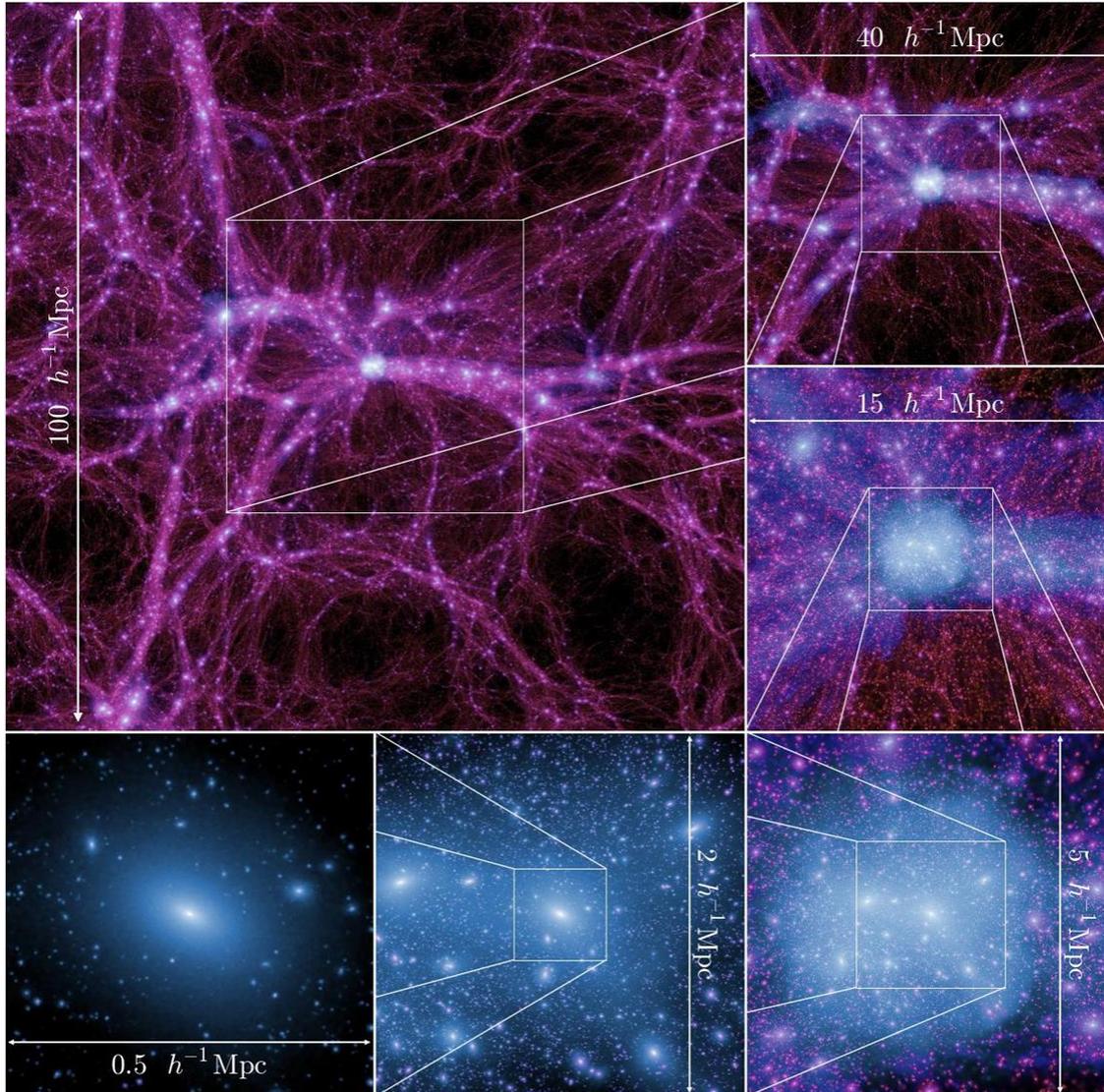


$$R_{\text{vir}} \sim 1-2 \text{ Mpc}$$
$$k_{\text{B}} T_{\text{gas}} \sim 3-10 \text{ keV}, \quad \sigma_v = 800-1300 \text{ km/s}$$
$$\Rightarrow M(R_{\text{vir}}) \sim 2 R_{\text{vir}} \sigma_v^2 / G \sim 10^{14-15} M_{\text{sun}}$$

MACS1206 at z=0.44 (Umetsu+CLASH 12)

Clusters as the largest DM halos:

halos = gravitationally-bound nonlinear objects



Clusters are formed at the intersection of filaments and sheets (LSS).

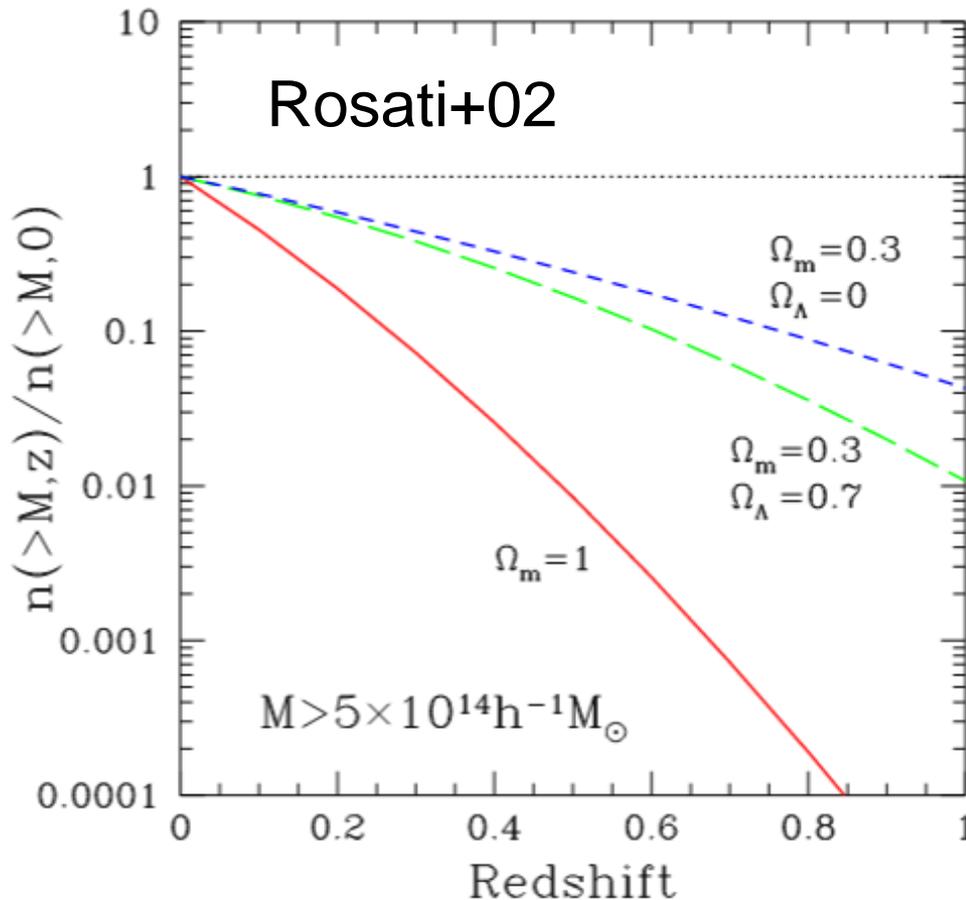
Inner halos are more triaxial (collisionless nature of DM)

Abundant substructures (CDM)

Boylan-Kolchin+09

Clusters as Cosmological Probe

Cluster # counts $\frac{dN(> M_{\text{lim}}, z)}{d\Omega dz} = \int_{M_{\text{lim}}}^{\infty} dM \frac{dV(z)}{d\Omega dz} \frac{d^2 n}{dV dM}(M, z)$



Volume element

$$\frac{d^2 V}{dz d\Omega} = \frac{cr^2[\chi(z)]}{H(z)}, \quad \chi(z) = \int_0^z \frac{dz'}{H(z')}$$

Halo mass function

$$\frac{d^2 n}{dV dM}(M, z) \propto \exp\left[-\frac{v^2}{2}\right]$$

$$v \equiv \frac{\delta_c}{D_+(z)\sigma(M)} \sim 3 \text{ for clusters}$$

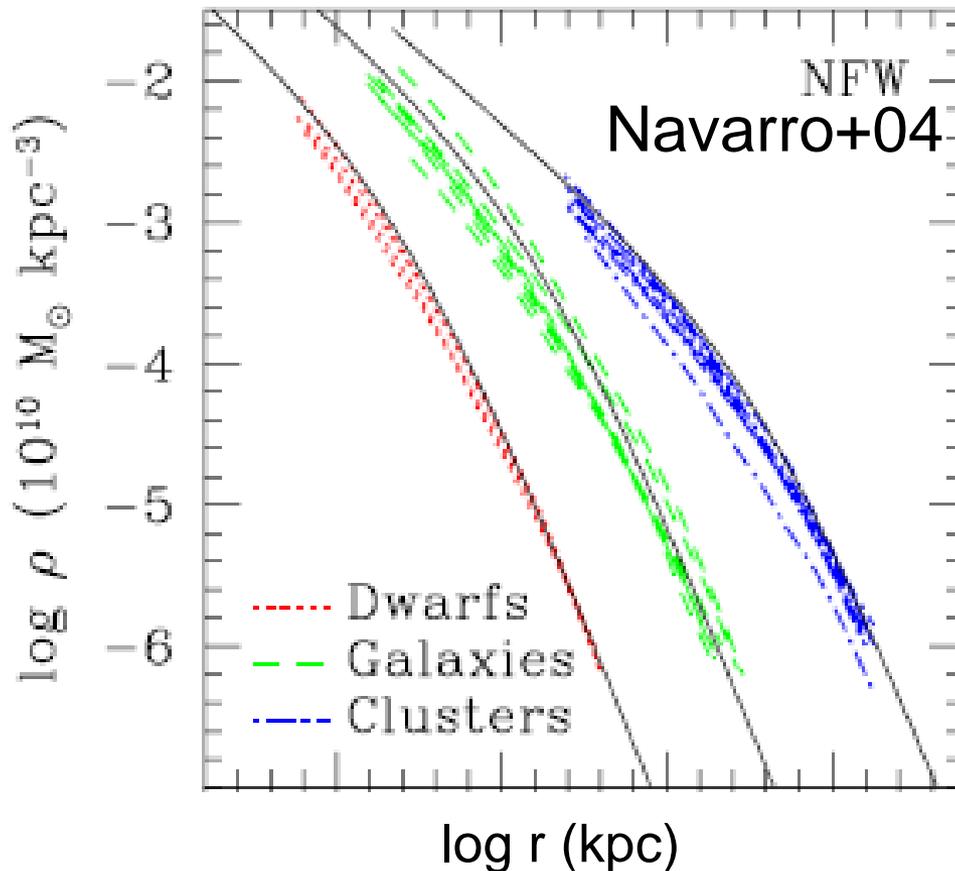
Cluster counts are exponentially sensitive to *cosmology* and ***cluster mass calibration!***

Key Predictions of nonlinear structure formation models

(1) Quasi self-similar DM-halo density profiles

Quasi-universal Halo Density Profile for collisionless CDM

Spherically-averaged DM density profiles $\langle\rho(r)\rangle$ from numerical simulations



Self-similarity

$$\rho(r) = Af(r/r_s)$$

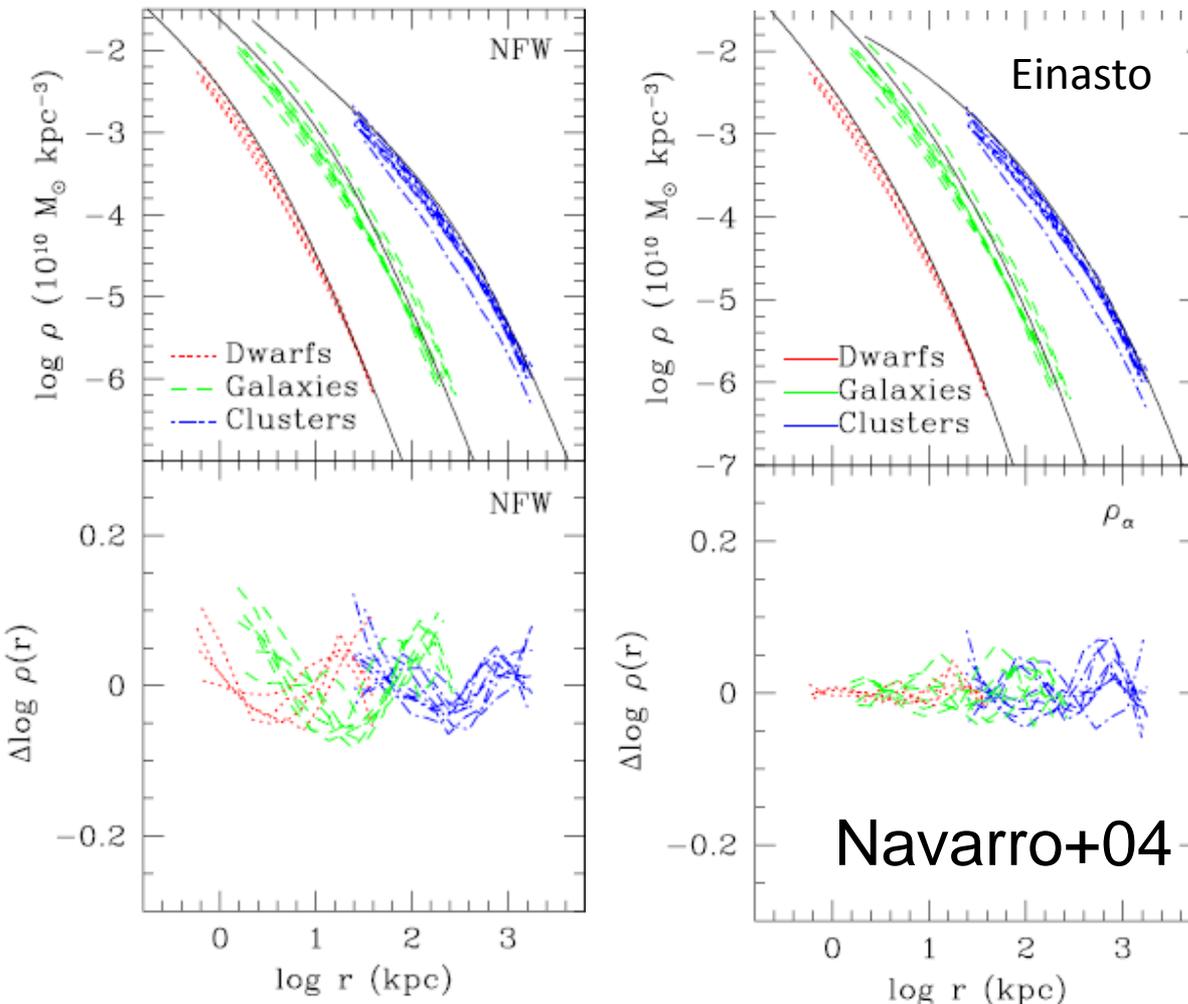
Empirical fitting formula by Navarro-Frenk-White (NFW)

$$\rho(r) = \frac{\rho_s}{(r/r_s)(1+r/r_s)^2}$$

Nearly independent of halo mass, redshift, initial conditions, and cosmology (NFW96, 97)

“Diversity” of halo density profiles

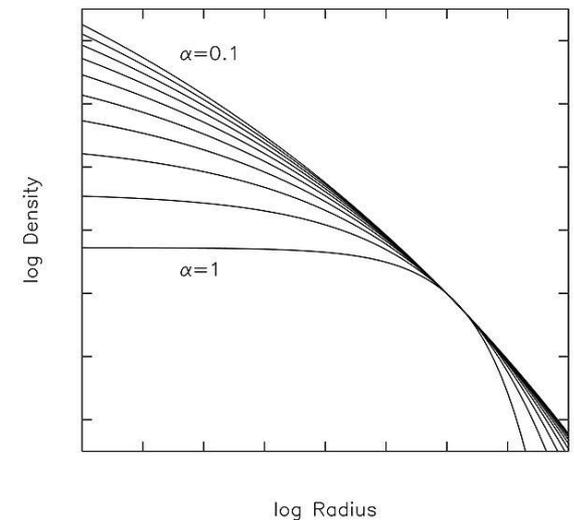
Mass profiles of DM halos are not strictly self-similar:



Einasto profile (ρ_s, r_s, α)

$$\frac{d \ln \rho(r)}{d \ln r} = -2 \left(\frac{r}{r_s} \right)^{\alpha}$$

α : degree of curvature

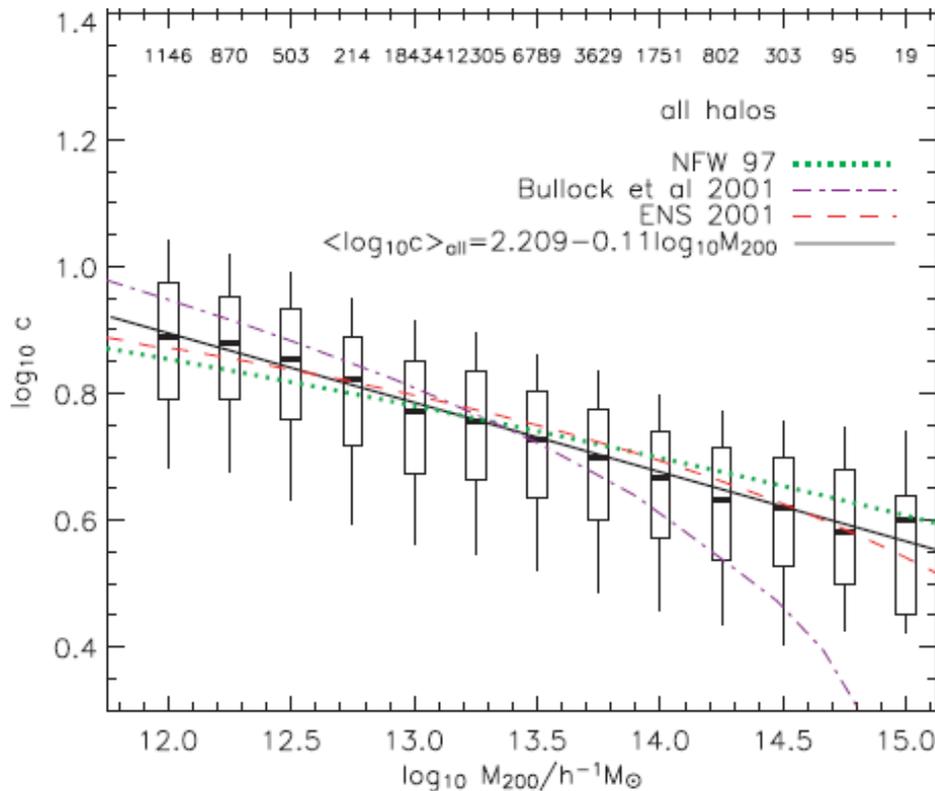


Key Predictions of nonlinear structure formation models

(2) Halo concentration-mass (c-M) relation

Degree of mass concentration

$$c_{200}(M_{200}) \equiv \frac{r_{200}}{r_s} \Rightarrow \frac{\text{Virial radius}}{\text{Isothermal (scale) radius}}$$

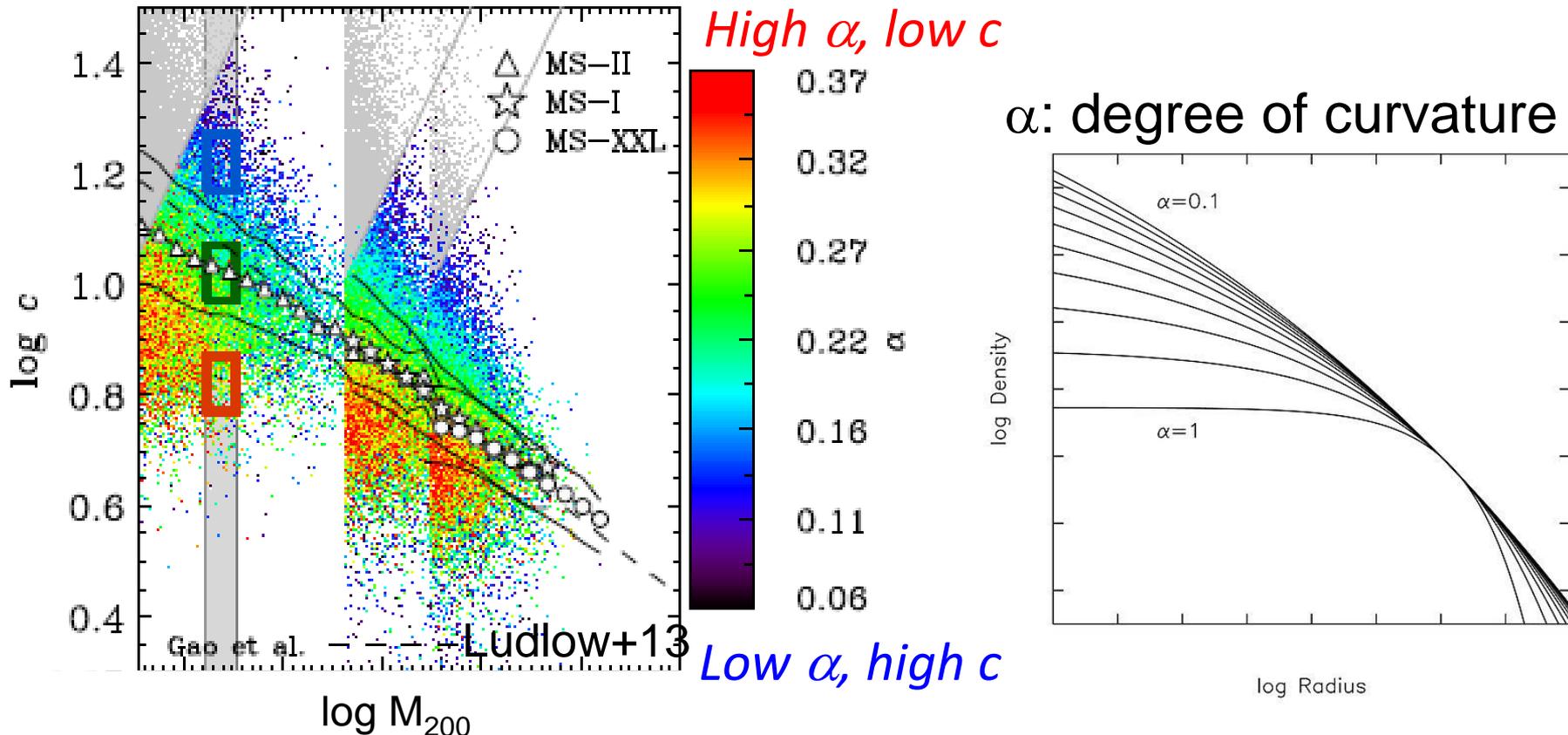


In hierarchical structure formation, $\langle c \rangle$ is predicted to decrease with increasing M

DM halos that are more massive collapse later on average, when the mean background density ρ_b of the universe is correspondingly lower (Bullock+01; Neto+07)

Clusters in a concordance LCDM cosmology are predicted to have $\langle c_{200} \rangle = 3-4$ (Gao+08; Duffy+08; Bhattacharya+13)

Intrinsic Scatter in $c(M)$: Mass Assembly Histories (MAH)



- Scatter is due to another DoF (α), related to MAH (Ludlow+13)
- Larger or smaller values of α correspond to halos that have been assembled more or less rapidly than the NFW curve
- Clusters with average c_{200} have the NFW-equivalent $\alpha \sim 0.18$

Key Predictions of nonlinear structure formation models

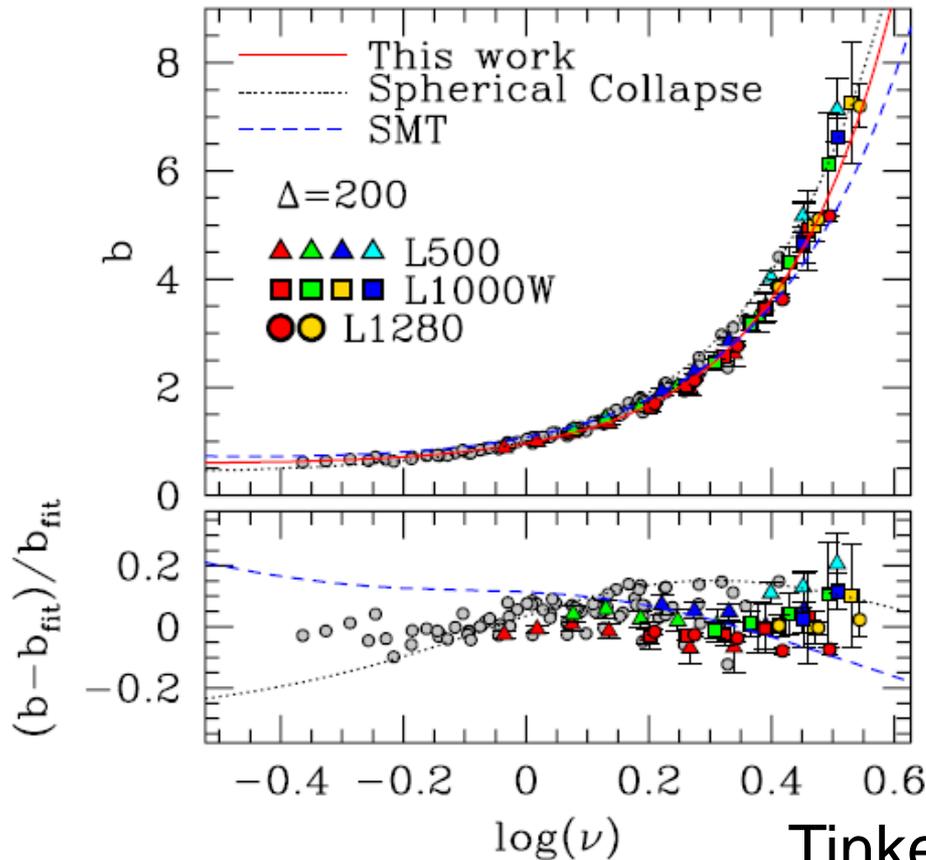
(3) Halo bias: surrounding large-scale structure

Halo bias: $b_h(M, z)$

2h term

Clustering of matter
around halos with M:

$$\xi_{\text{hm}}(r | M) = \frac{\langle \rho_{1h}(r | M) \rangle}{\bar{\rho}} + b_h(M) \xi_{\text{mm}}(r)$$



$$b_h(\nu) \approx 1 + \frac{\nu^2 - 1}{\delta_c}$$

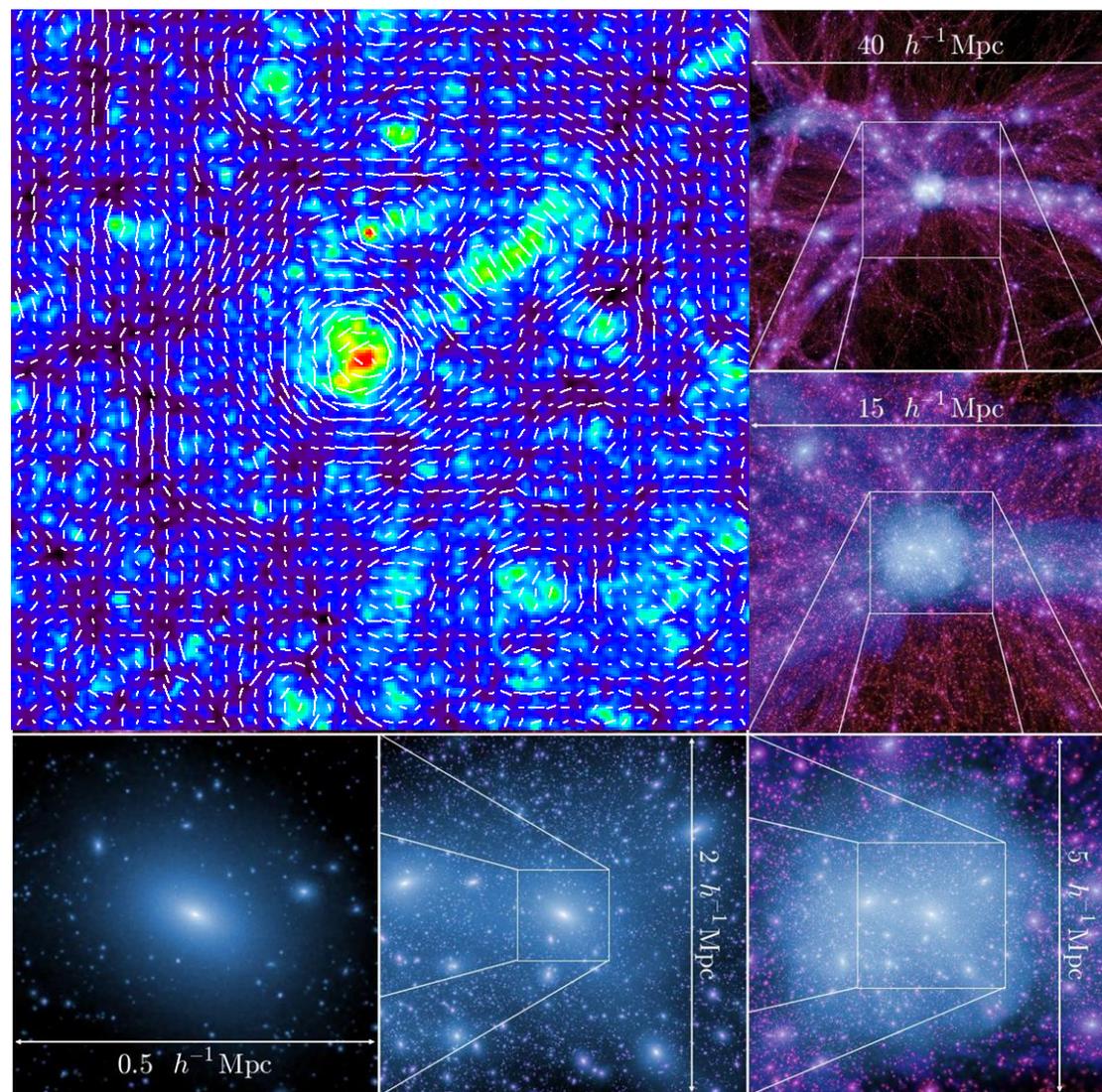
$$\nu \equiv \frac{\delta_c}{\sigma(M, z)} \sim 3 - 4 \text{ for clusters}$$

$$(\log_{10} \nu \sim 0.5 - 0.6)$$

Typical cluster formation epoch:
 $z_f = 0.7 - 0.5$ (Boylan-Kolchin 08)

Tinker+10 LCDM simulations

Weak Gravitational Lensing



Objectives

Halo structure (1h)

- ✓ *Virial mass, M_{200} :*
- ✓ *Halo density profile, $\langle \rho(r) \rangle$:*
- ✓ *Concentration, $c(M, z)$:*

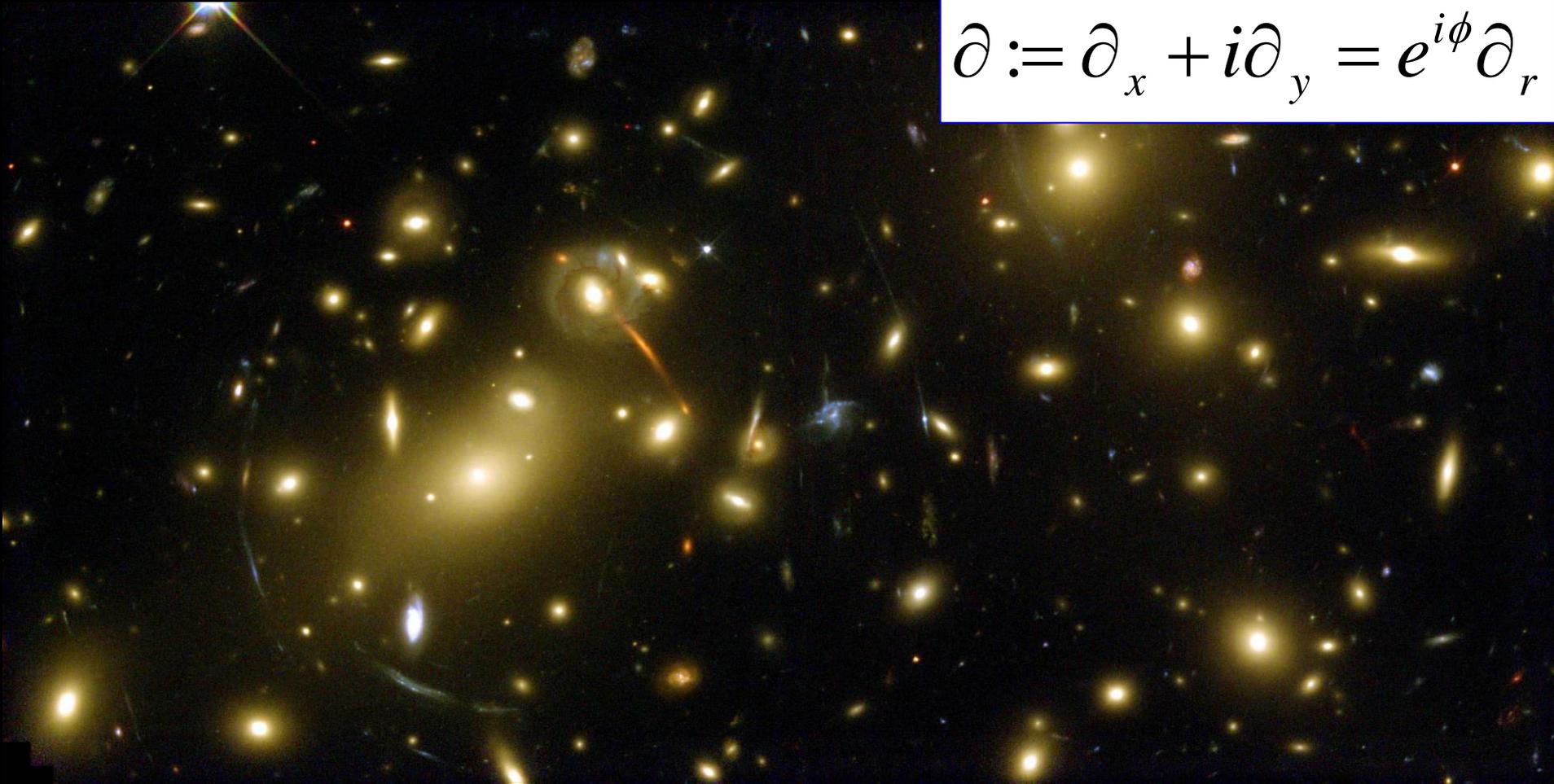
Surrounding LSS (2h)

- ✓ *Halo bias $b(M, z)$*
- ✓ *Primordial matter $P(k)$*

Gravitational Shear

$$\gamma = \partial\partial\Phi / 2$$

$$\partial := \partial_x + i\partial_y = e^{i\phi} \partial_r$$

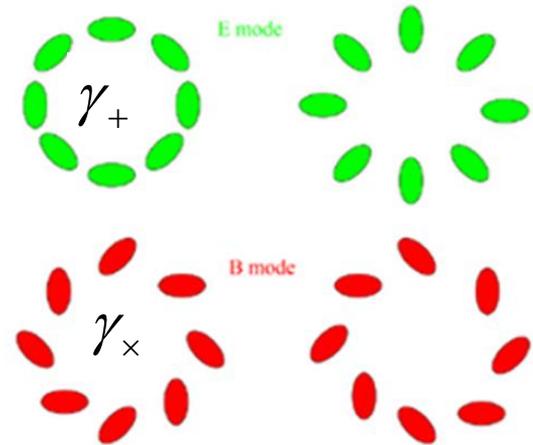


Tangential Shear

Measure of azimuthally-averaged tangential coherence of elliptical distortions around a given point (Kaiser 95):

$$\gamma_+(R) = \Delta\Sigma(R) / \Sigma_{\text{crit}}$$

$$\gamma_\times(R) = 0$$



$\Delta\Sigma(R)$ is the *radially-modulated surface mass density*:

$$\Delta\Sigma(R) = \Sigma(< R) - \Sigma(R)$$

Sensitive to interior mass

$$\Sigma = \int dl \delta\rho$$

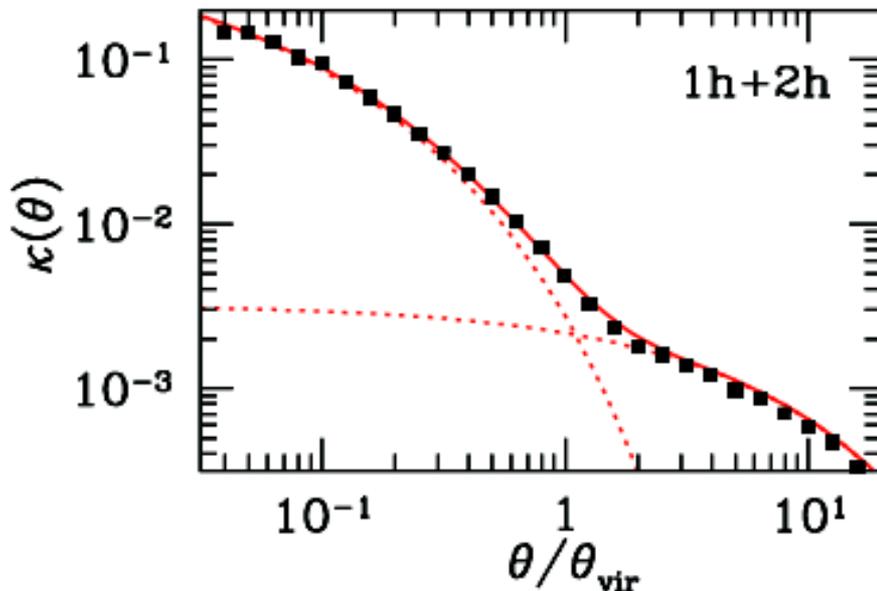
$\Sigma_{\text{crit}}(z_l, z_s)$ is the *critical surface mass density of lensing*

Shear doesn't see mass sheet

Averaged lensing profiles in/around LCDM halos (Oguri+Hamana 11)

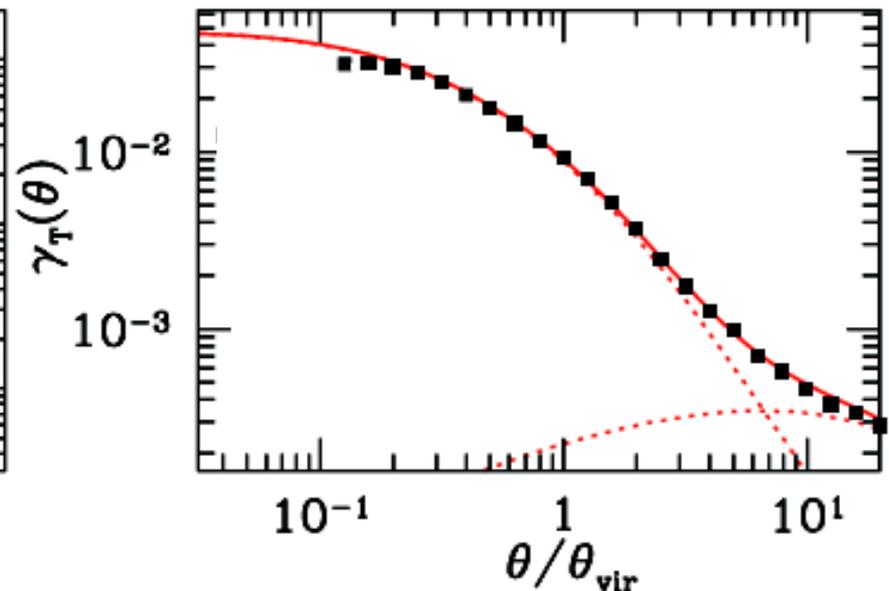
Total

$$\kappa = \Sigma(R) / \Sigma_{\text{crit}}$$



Modulated

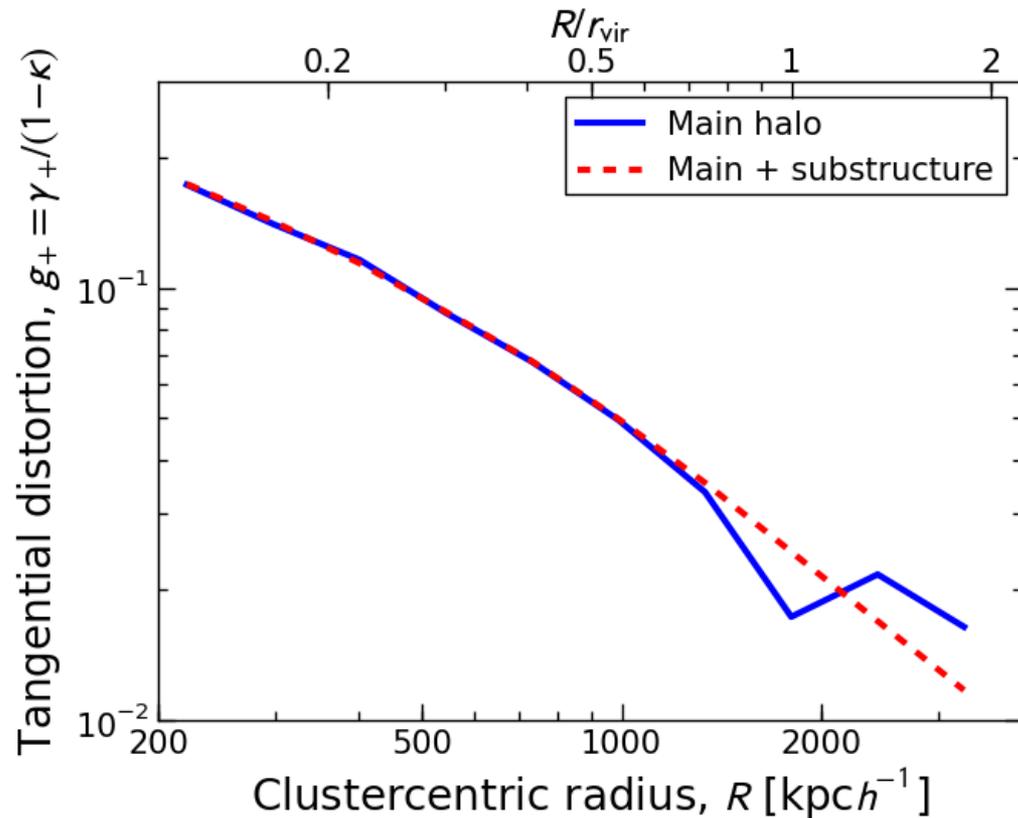
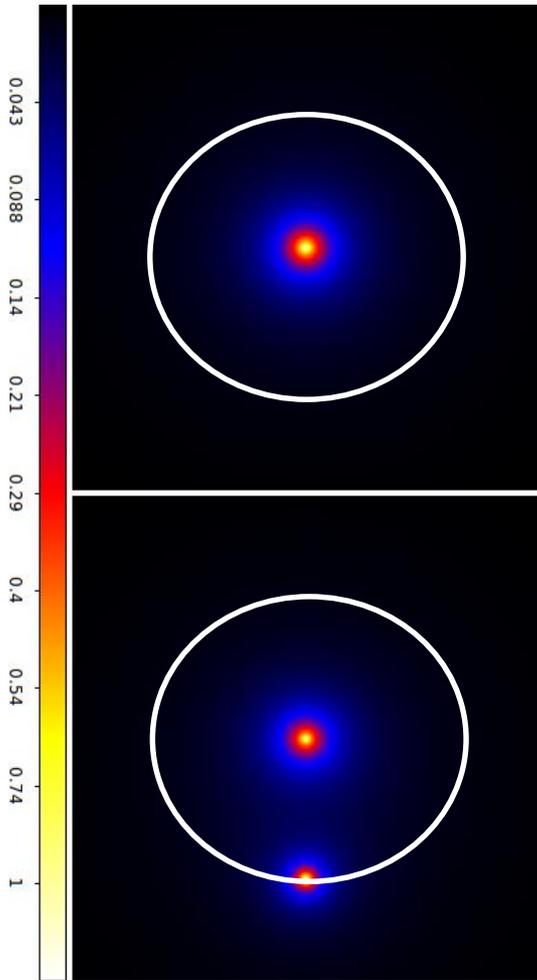
$$\gamma_+ = \Delta\Sigma(R) / \Sigma_{\text{crit}}$$



- Tangential shear is a powerful probe of **1-halo term**, or **internal halo structure**.
- Shear alone cannot recover absolute mass, known as **mass-sheet degeneracy**

Non-local substructure effect

A substructure at $R \sim r_{\text{vir}}$ of the main halo, modulating $\Delta\Sigma(R) = \Sigma(< R) - \Sigma(R)$



Known $\sim 10\%$ negative bias in mass estimates from tangential-shear fitting, inherent to clusters sitting in substructured field (Rasia+12)

Gravitational Magnification

$$\kappa = \partial\bar{\partial}^*\Phi / 2 = \Delta\Phi / 2$$

$$\partial := \partial_x + i\partial_y = e^{i\phi}\partial_r$$

MACSJ1149 (z=0.54)

Zheng+CLASH. 2012, *Nature*, 489, 406

Magnification Effects

Source plane

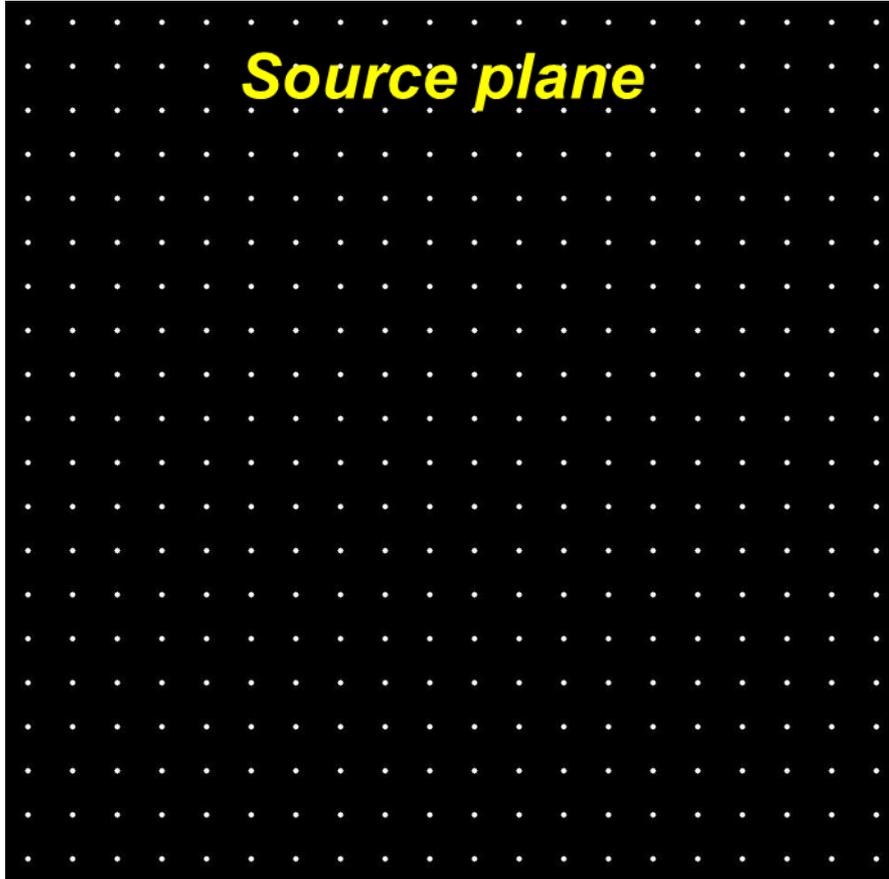
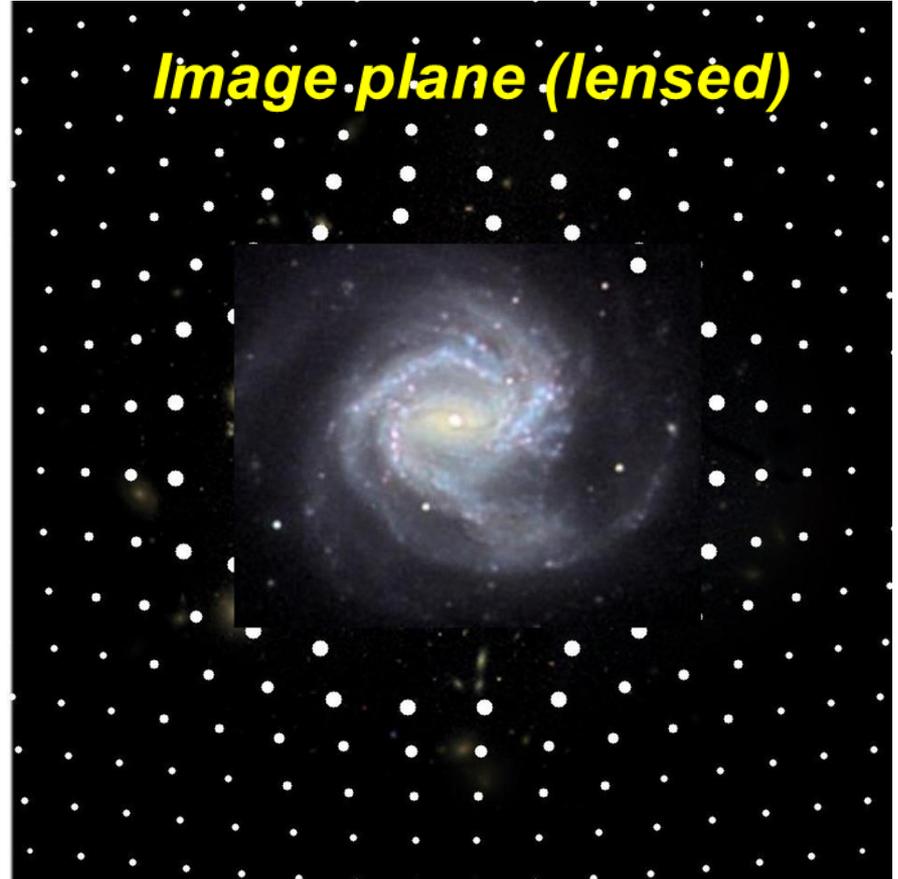


Image plane (lensed)



- Image flux, F : $\mu \sim 1+2\kappa$
- Image size, r : $\mu^{1/2} \sim 1+\kappa$
- Sky area, $\Delta\Omega$: $\mu \sim 1+2\kappa$

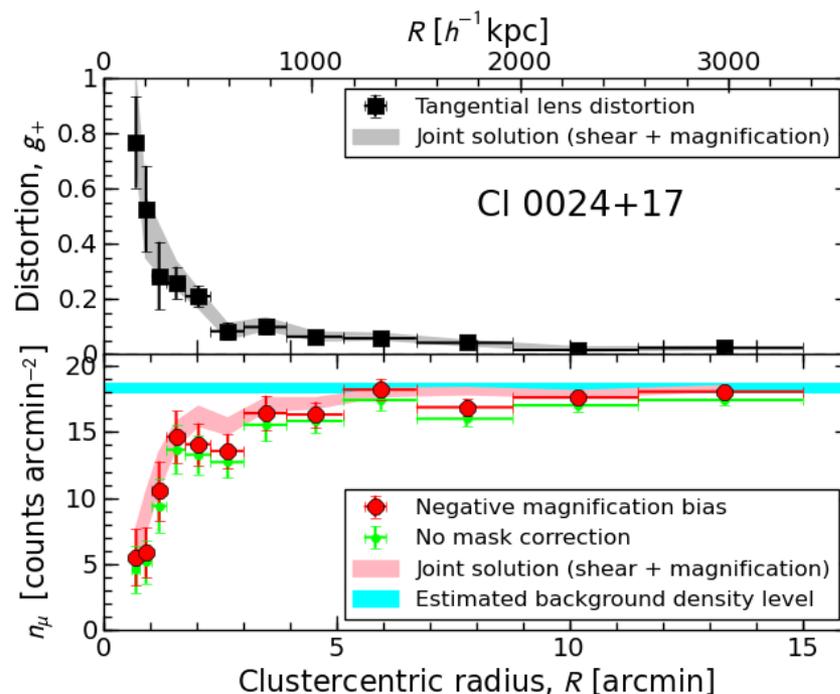
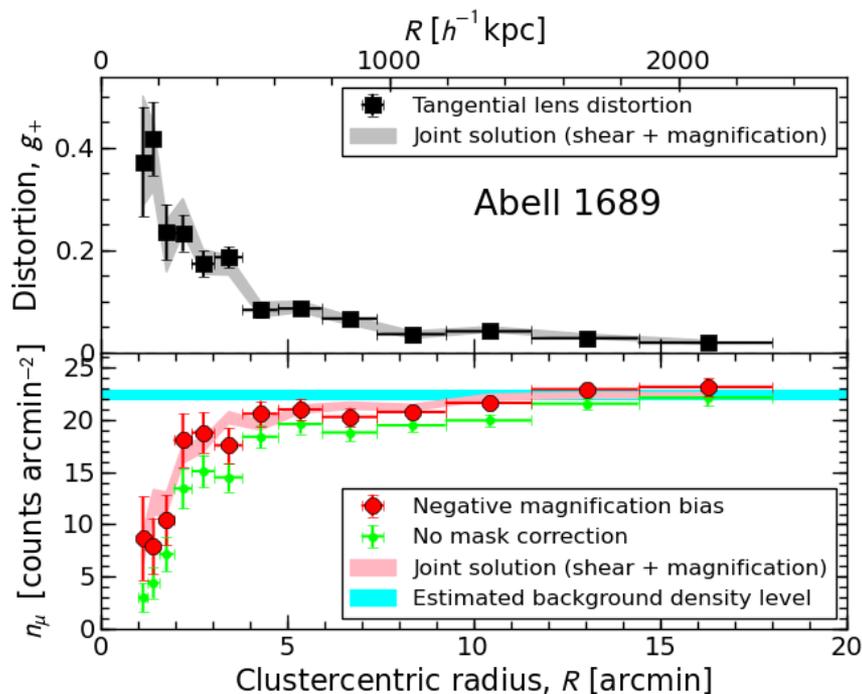
Sensitive to “local” matter density

$$\kappa = \Sigma / \Sigma_{\text{crit}}$$

Negative Magnification Bias: Count Depletion

Geometric shear-magnification consistency

Number counts of red galaxies at $\langle z \rangle \sim 1$ highly depleted



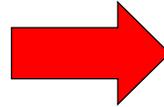
Umetsu+11a, ApJ, 729, 127

Subaru telescope data

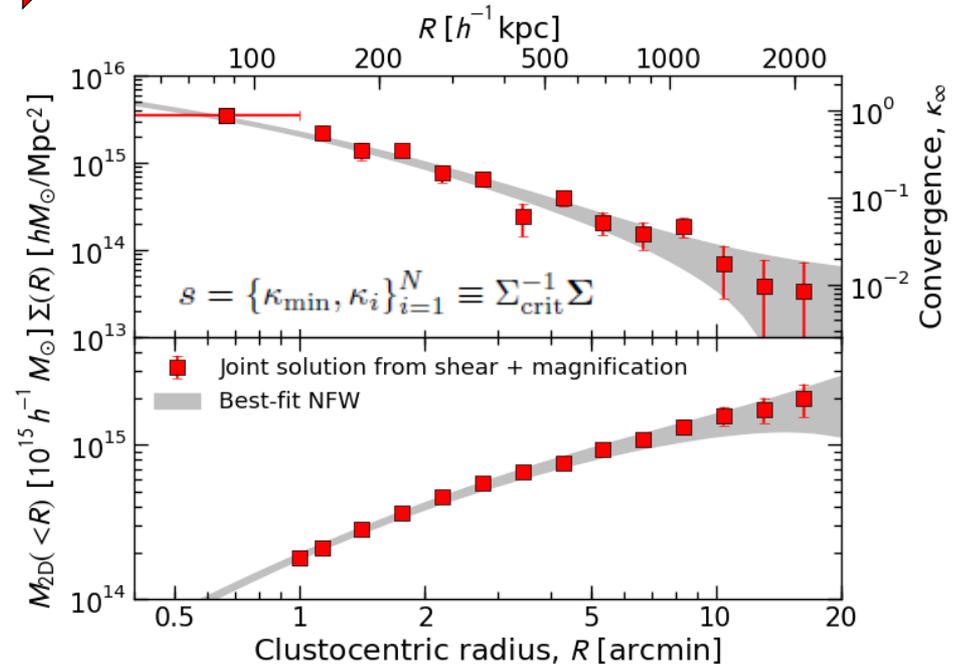
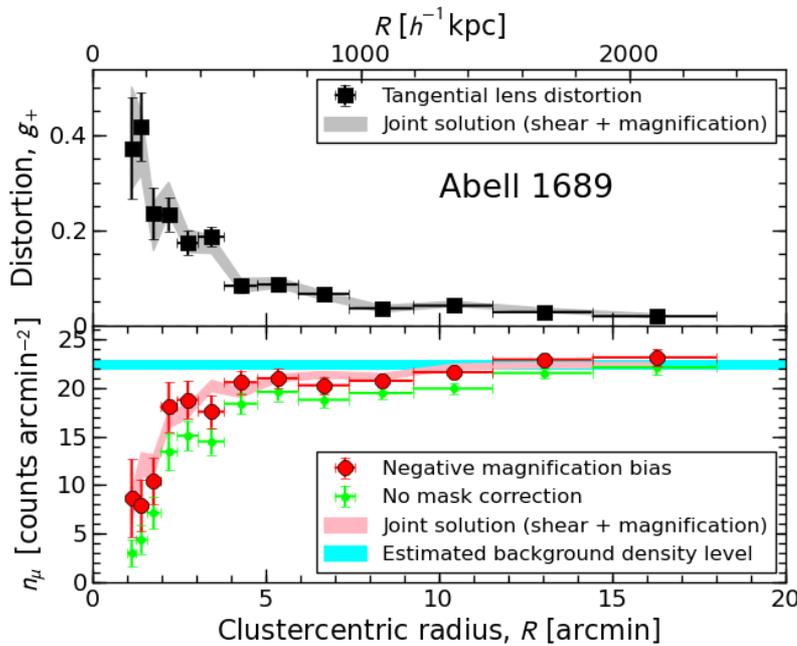
Combining Shear and Magnification

Bayesian joint-likelihood analysis (Umetsu+11a; Umetsu 13)

Shear + magnification



Non-parametric $\Sigma(R)$ solution



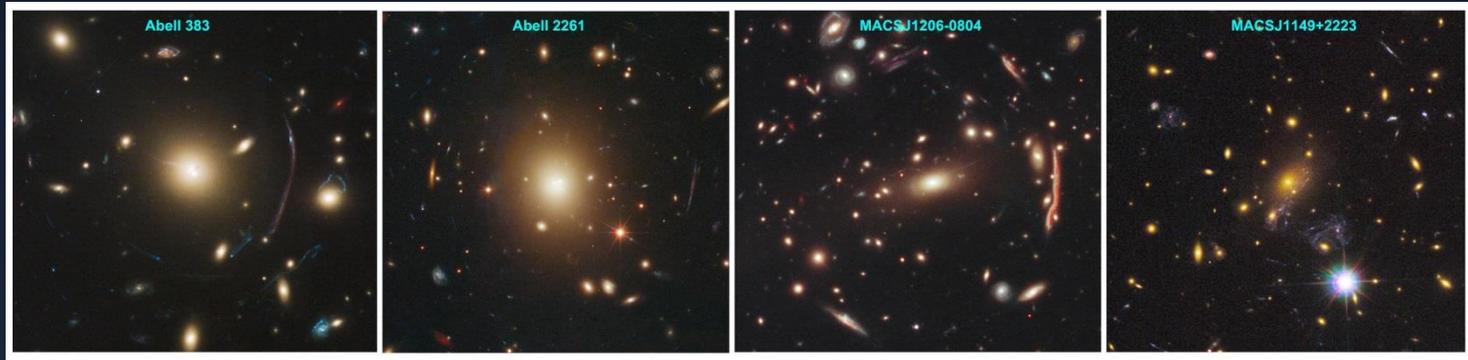
- Mass-sheet degeneracy broken
- Total statistical precision improved by $\sim 20\text{-}30\%$
- Calibration uncertainties marginalized over: $c = \{\langle W \rangle_s, f_{W,s}, \langle W \rangle_\mu, \bar{n}_\mu, s_{\text{eff}}\}$.



CLASH:

Cluster Lensing And Supernova survey with Hubble

A 524-orbit HST Multi-Cycle Treasury Program designed to place new constraints on the fundamental components of the cosmos: dark matter, dark energy, and baryons (PI: Marc Postman, STScI)

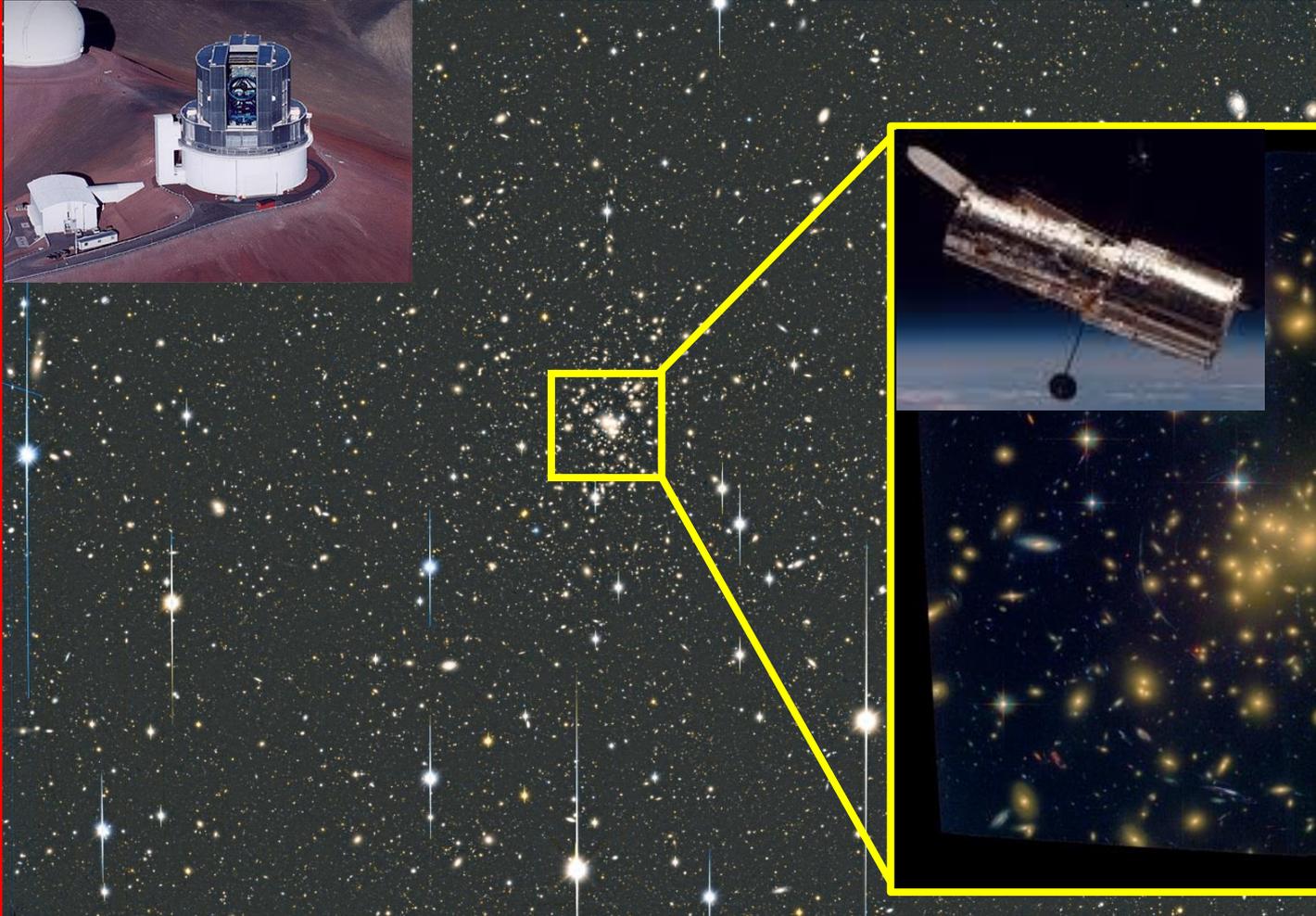


Wide-field Subaru imaging ($0.4 - 0.9 \mu\text{m}$) plays a unique role in complementing deep HST imaging of cluster cores.

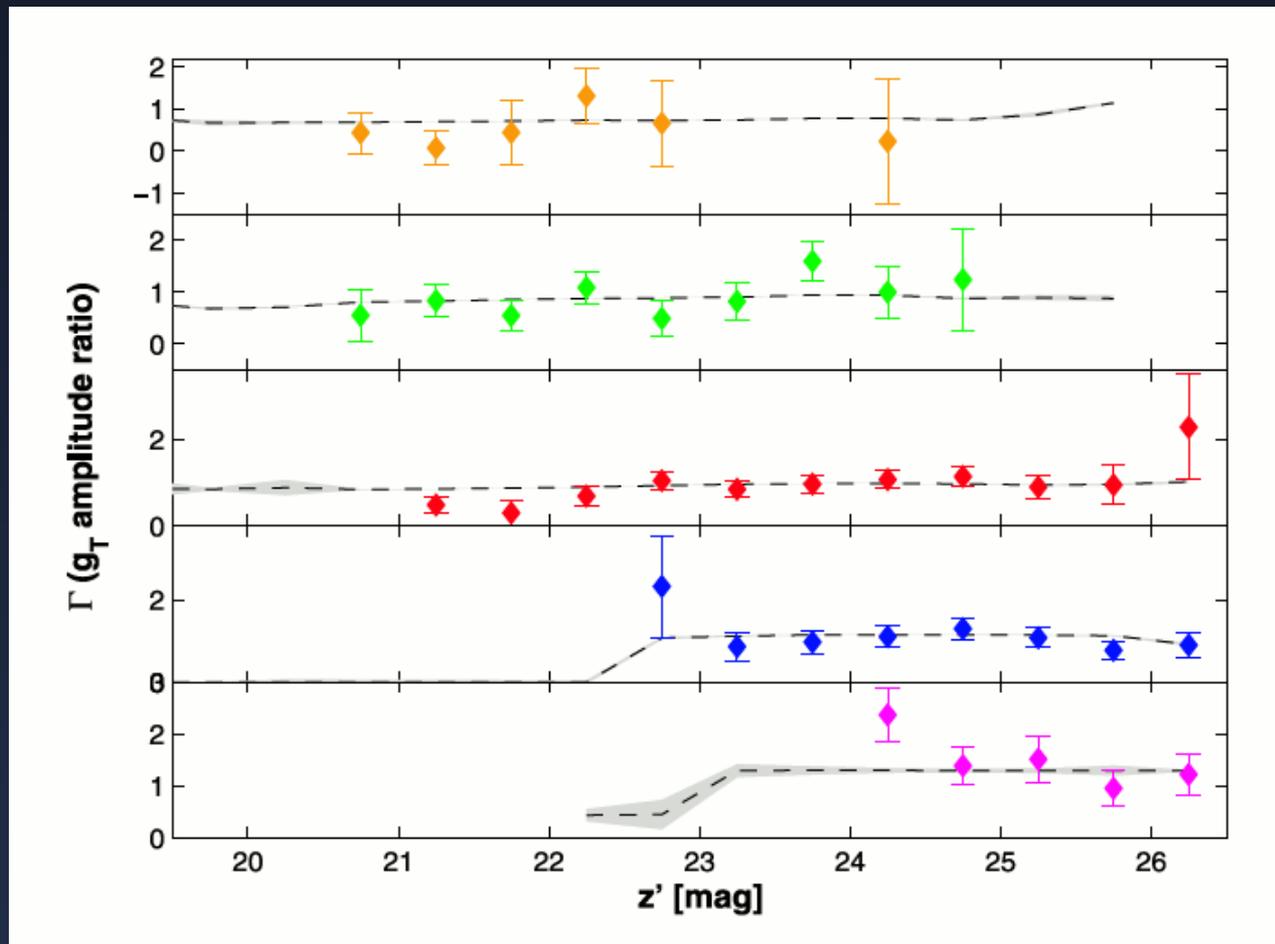
My talk will focus on CLASH-WL results based primarily on Subaru data (Umetsu+CLASH 14, arXiv:1404.1375)

***SUBARU* multi-color maging for wide-field weak lensing**

High-resolution space imaging with *Hubble* for strong lensing

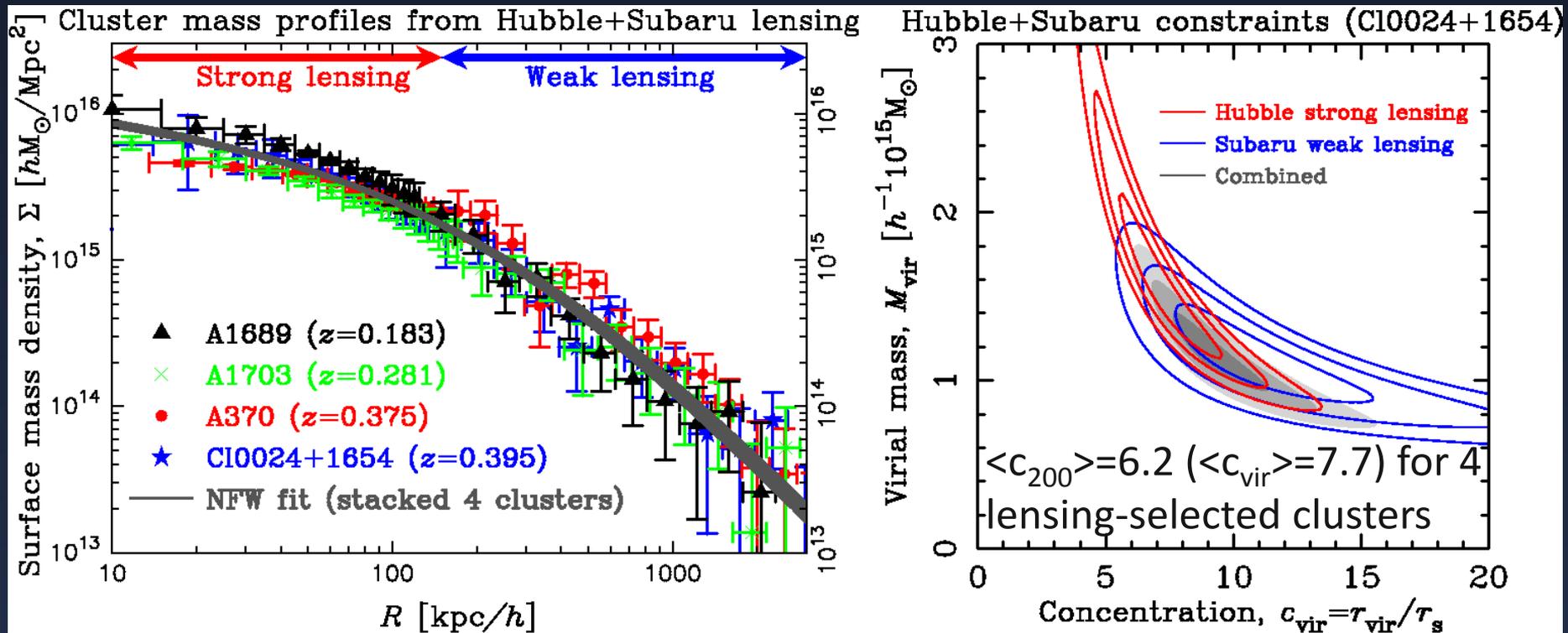


SUBARU shear strength as a function of magnitude



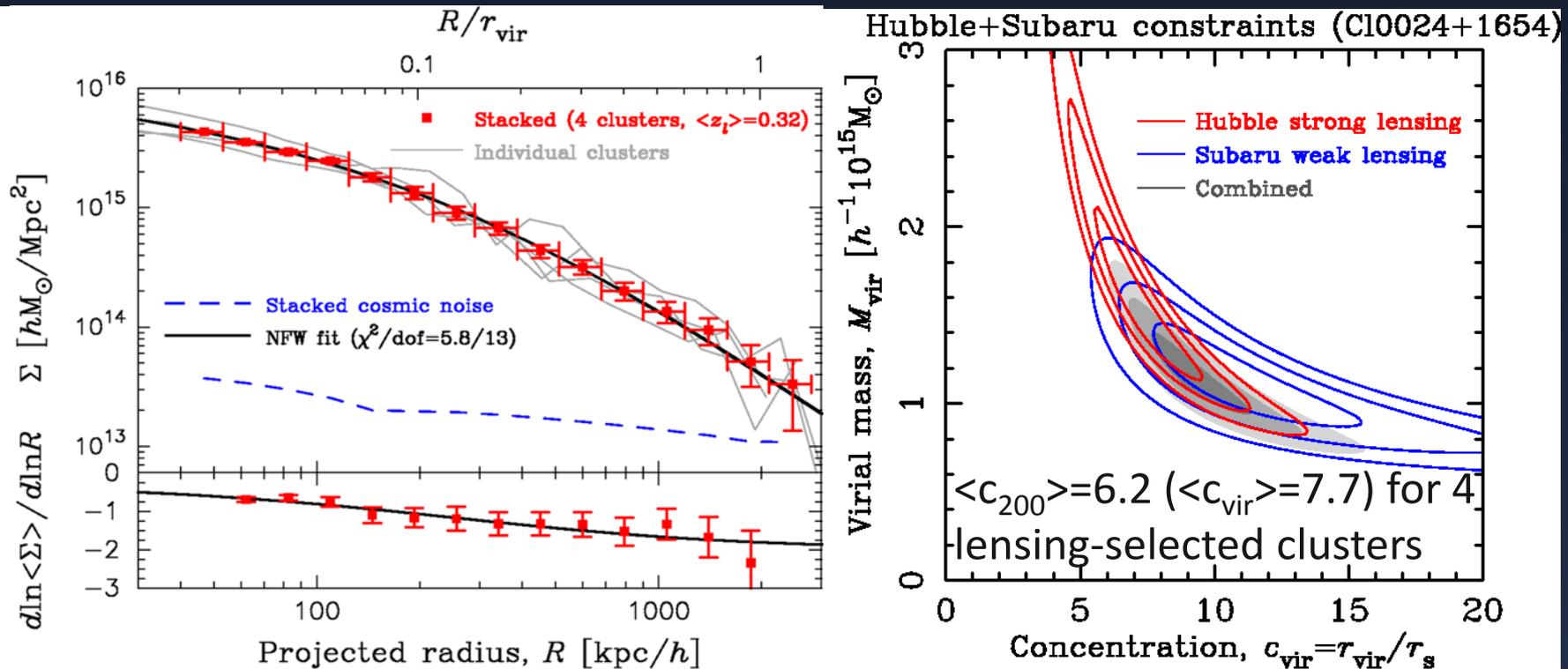
Pre-CLASH Lensing Results

Strong-lensing (*HST*) + shear + magnification (Subaru) available only for a handful of **strong-lensing-selected** high-mass clusters ($\theta_E > 30$ arcsec, $z_s=2$)



Pre-CLASH Lensing Results

Strong-lensing (*HST*) + shear + magnification (Subaru) available only for a handful of **strong-lensing-selected** high-mass clusters ($\theta_E > 30$ arcsec, $z_s=2$)



Pre-CLASH Lensing Summary

1. Cluster mass profile “shape”

- NFW is an excellent fit out to $\sim R_{\text{vir}}$ (cf. Okabe, Smith, Umetsu+13; Newman+13)
- Consistent with collisionless, non-relativistic DM

2. Degree of halo concentration

- $c_{200} \sim 6$ at $M_{200} = 1.2e15 M_{\text{sun}}/h$ ($z=0.32$) assuming spherical NFW
- Higher than LCDM predictions, $\langle c_{200} \rangle \sim 3$ for high-mass clusters
- Expected lensing-selection/projection bias $\sim +50\%$:
 $\langle c_{200} \rangle \sim 4.5$ *not enough??*



CLASH Targets & Objectives

1. 20 X-ray hot/regular clusters

- Individual and ensemble-averaged DM density profiles $\langle\rho(r)\rangle$ in equilibrium clusters
- Cluster c - M relation, $c(M)$

2. 5 high-magnification clusters

- Search for high- z magnified galaxies

Postman+CLASH 2012, ApJS

The CLASH Gallery (HST)

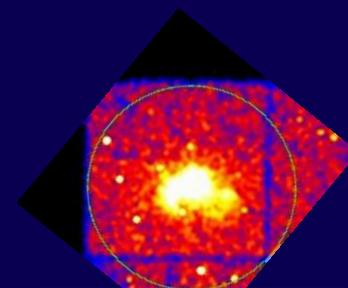
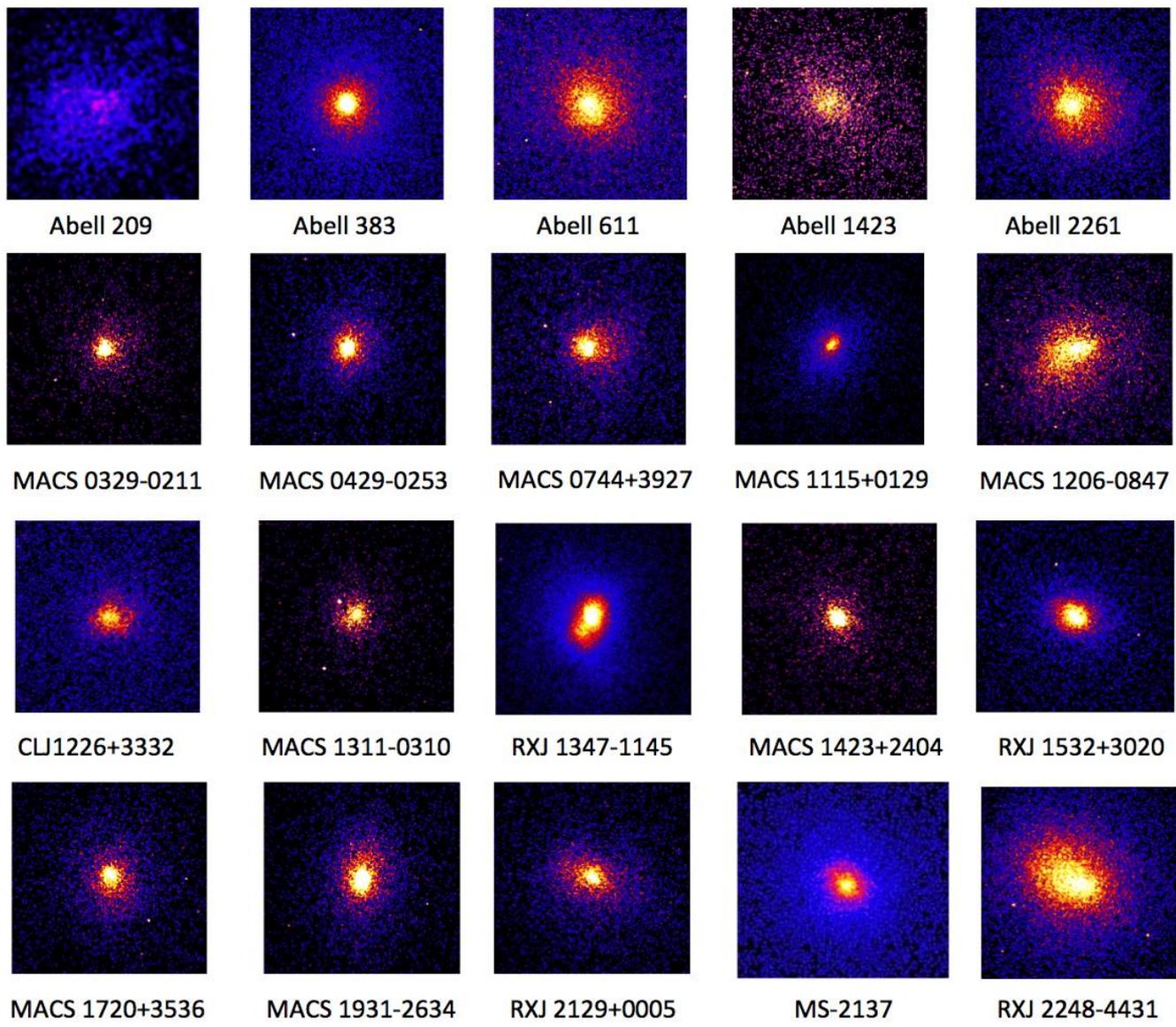


The final HST observation for CLASH was on 9-July-2013 ... 963 days, 15 hrs, 31 min after first obs.

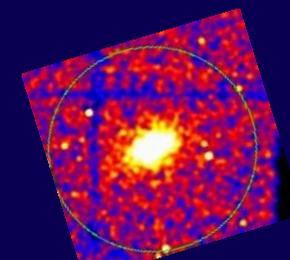


CLASH X-ray-selected subsample

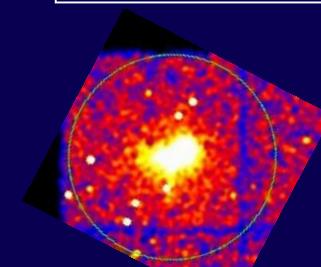
- Redshift coverage
 - $0.18 < z < 0.90$
 - No lensing selection bias
 - X-ray hot ($T_x > 5\text{keV}$)
 - $M_{200} = [5-20] 1e14 M_{\text{sun}}/h$
 - Small BCG to X-ray-peak offset
 - Offset dispersion: $\sigma_{\text{off}} \sim 10\text{kpc}/h$
 - Smooth, regular X-ray morphology
- Optimized for radial profile measurements



MACS 0717+3745



RXJ 0647+7015



MACS 1149+2223

All have
 $T_x > 5$ keV

X-ray images of 23 of the 25 CLASH clusters. 20 are selected to be “relaxed” clusters (based on their x-ray properties only). 5 are selected specifically because they are strongly lensing $\theta_E > 30''$



CLASH Characterization

Theoretical predictions from 1,400 clusters re-simulated at high spatial and mass resolution by Meneghetti+CLASH 14 (MUSIC-2: DM + adiabatic gas)

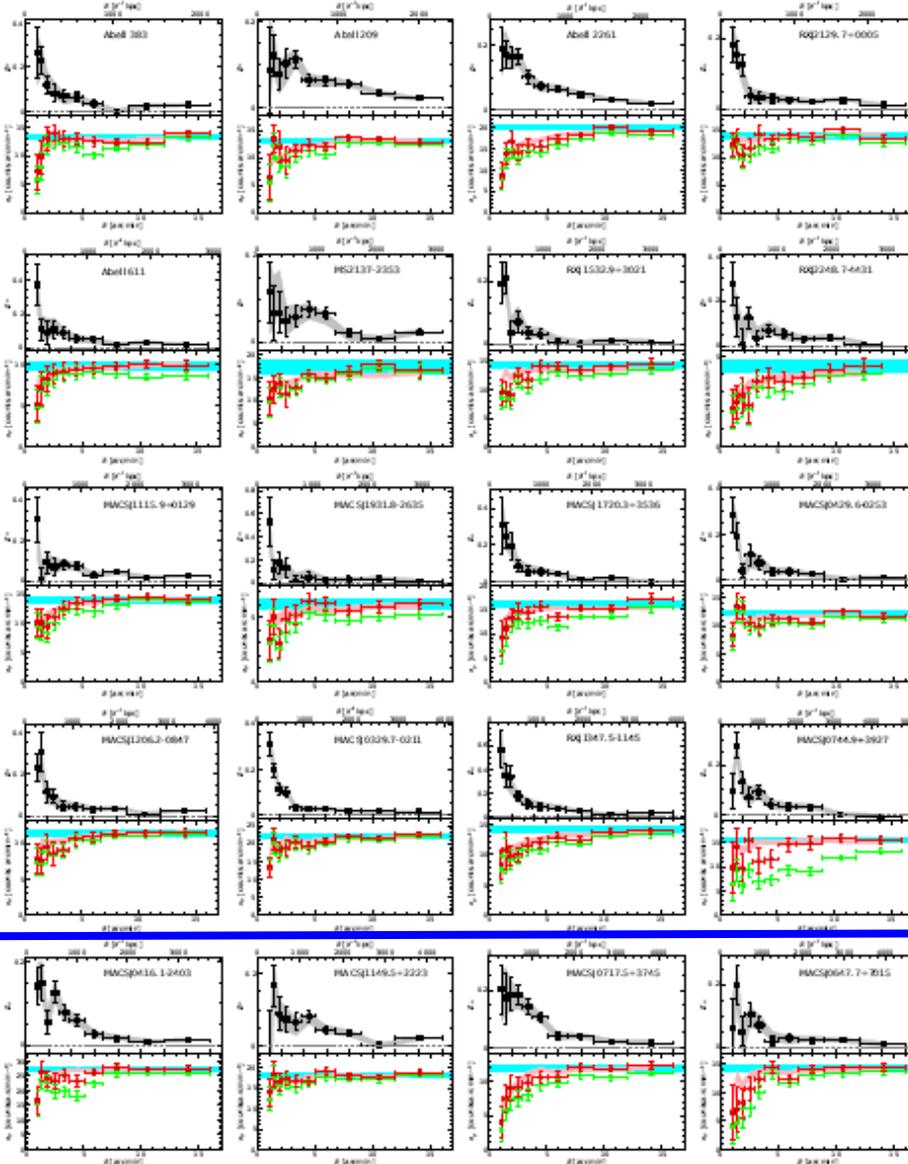
- CLASH X-ray selection function taken into account using Chandra X-ray image simulator (X-MAS).
- (M_{200}, c_{200}) measured both in 3D and 2D, taking into account projection effects \rightarrow modest orientation bias for CLASH.
- The CLASH selection function gives a heterogeneous sample of relaxed (70%) and unrelaxed (30%) clusters.
- c_{200} recovered from the lensing analysis of the CLASH clusters are $c=[3-6]$, with an average value of 3.9 and a standard deviation of 0.6.

Objective (1)

- Non-parametric mass profile reconstruction from joint shear-and-magnification analysis of 20 CLASH clusters
- Cluster mass measurements



20 CLASH clusters in Umetsu+14



16 X-ray-selected clusters

- 15 clusters from 8.3m Subaru Telescope
- 1 southernmost cluster (RXJ2248) from 2.2m ESO/MPG
- $0.18 < z < 0.69$

$\langle \chi^2/\text{dof} \rangle = 0.92$ for 20 CLASH clusters

4 high-magnification clusters

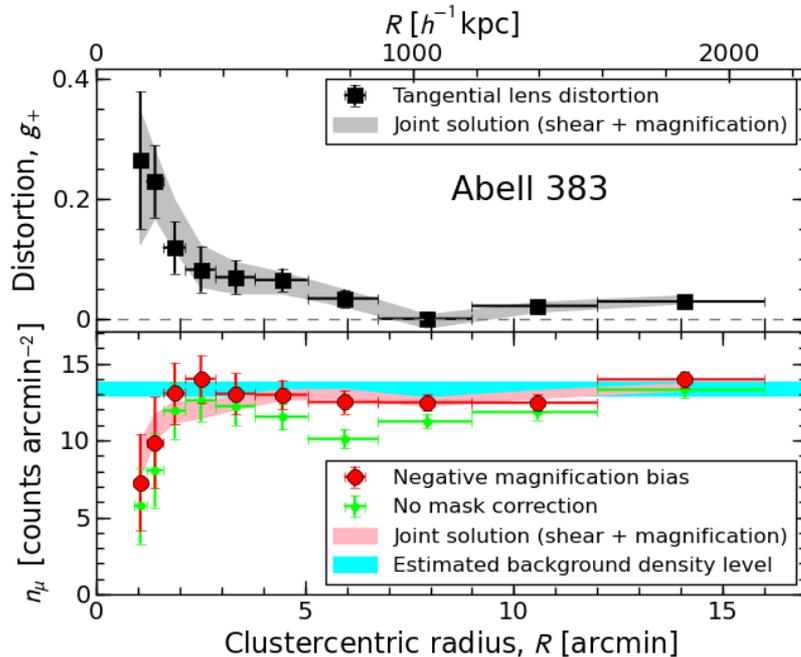
- All 4 clusters from 8.3m Subaru Telescope



Joint Shear+Magnification Analysis

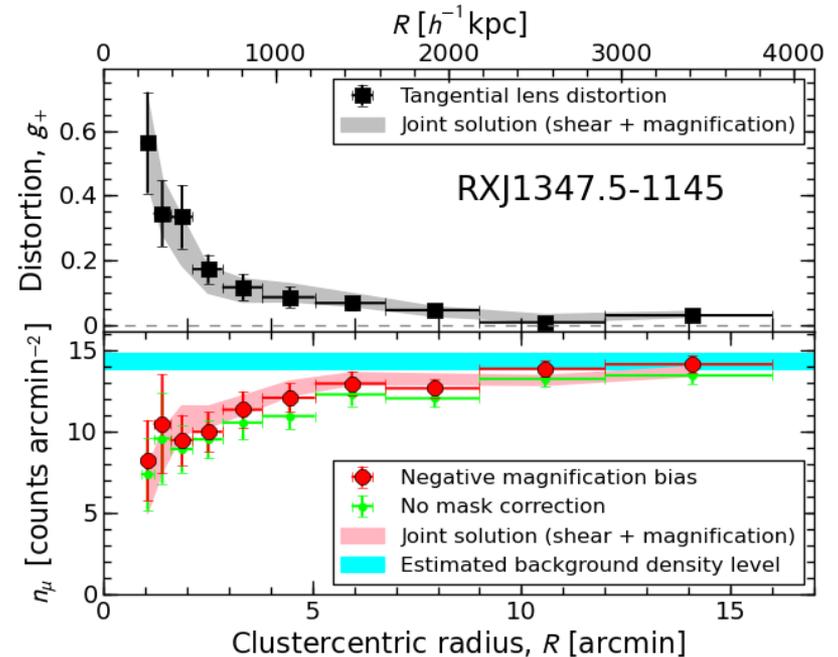
CLASH low mass

$M_{\text{vir}}=6e14M_{\text{sun}}/h$ ($z=0.19$)



CLASH high mass

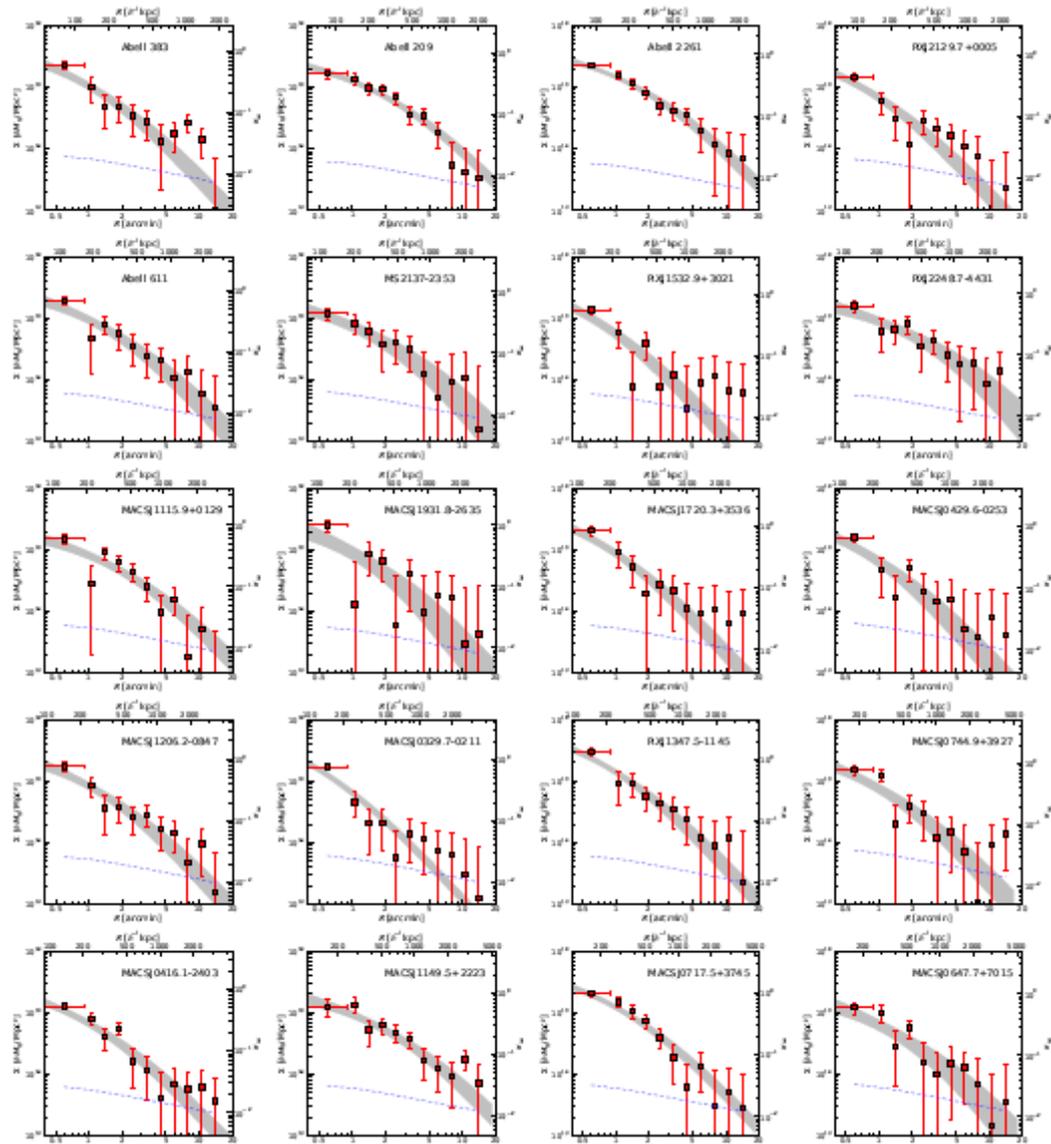
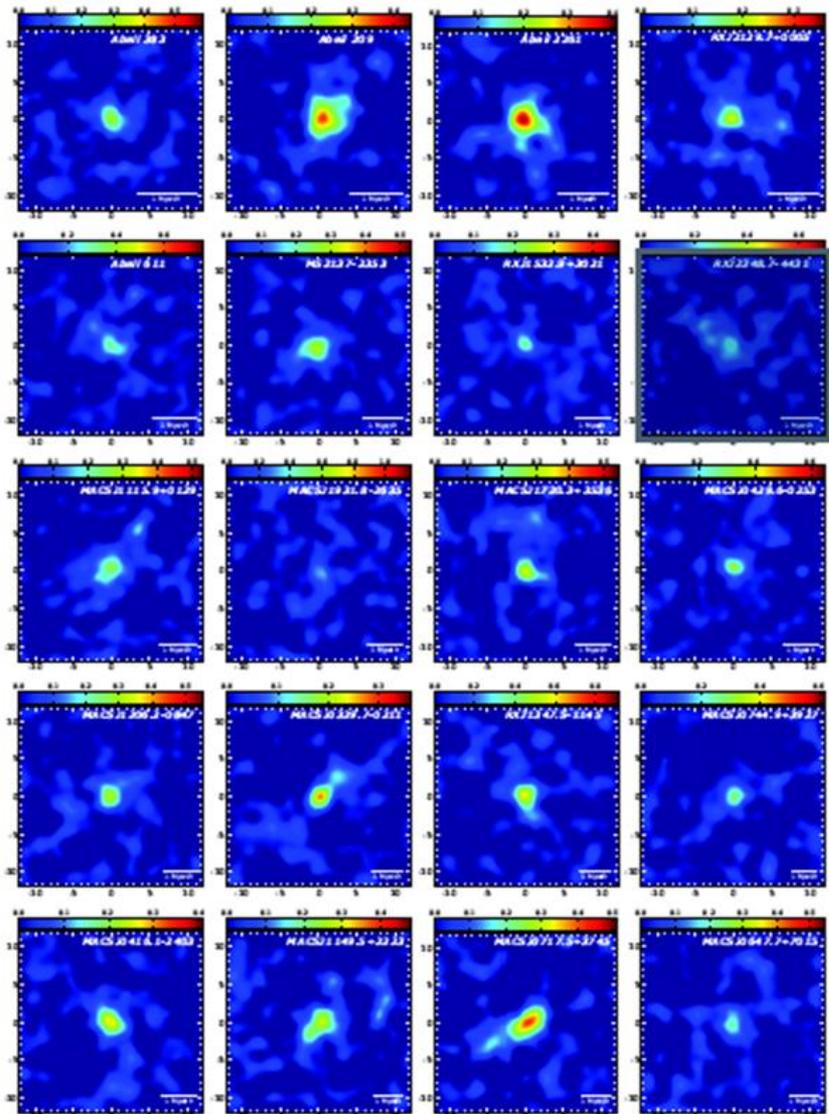
$M_{\text{vir}}=23e14M_{\text{sun}}/h$ ($z=0.45$)



For all clusters, $2N=20$ measurements, $N+1=11$ binned $\Sigma(R)$ parameters

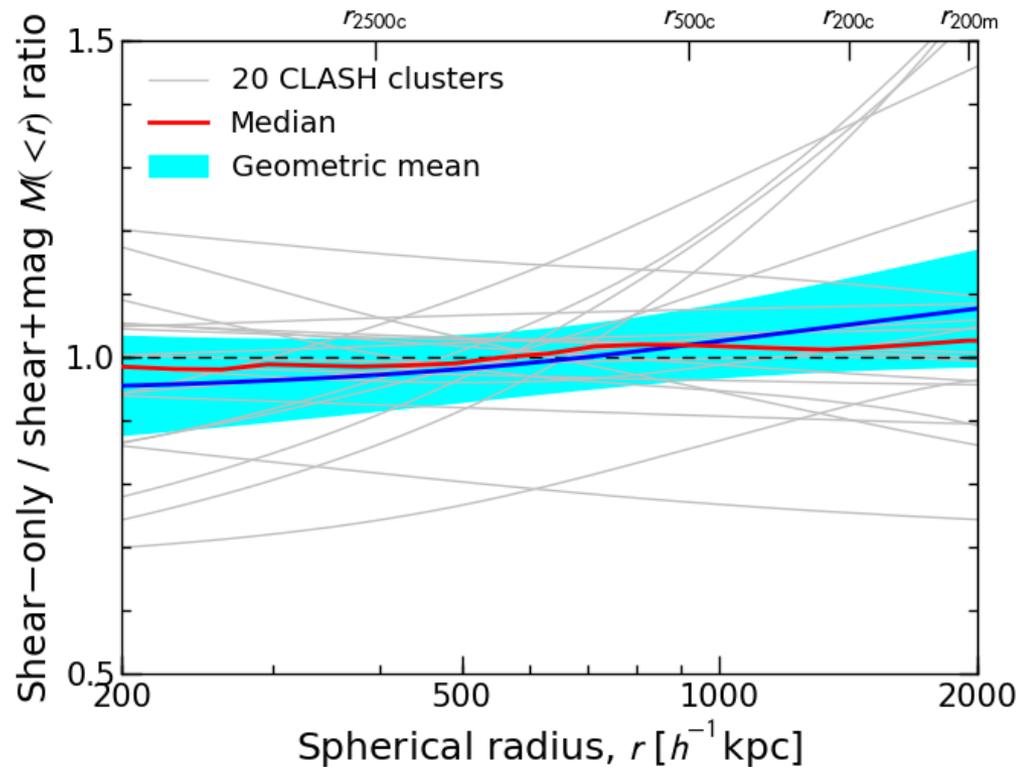
Umetsu+CLASH 14, arXiv:1404.1375

Mass Density Profile Dataset



Shear-Magnification Consistency

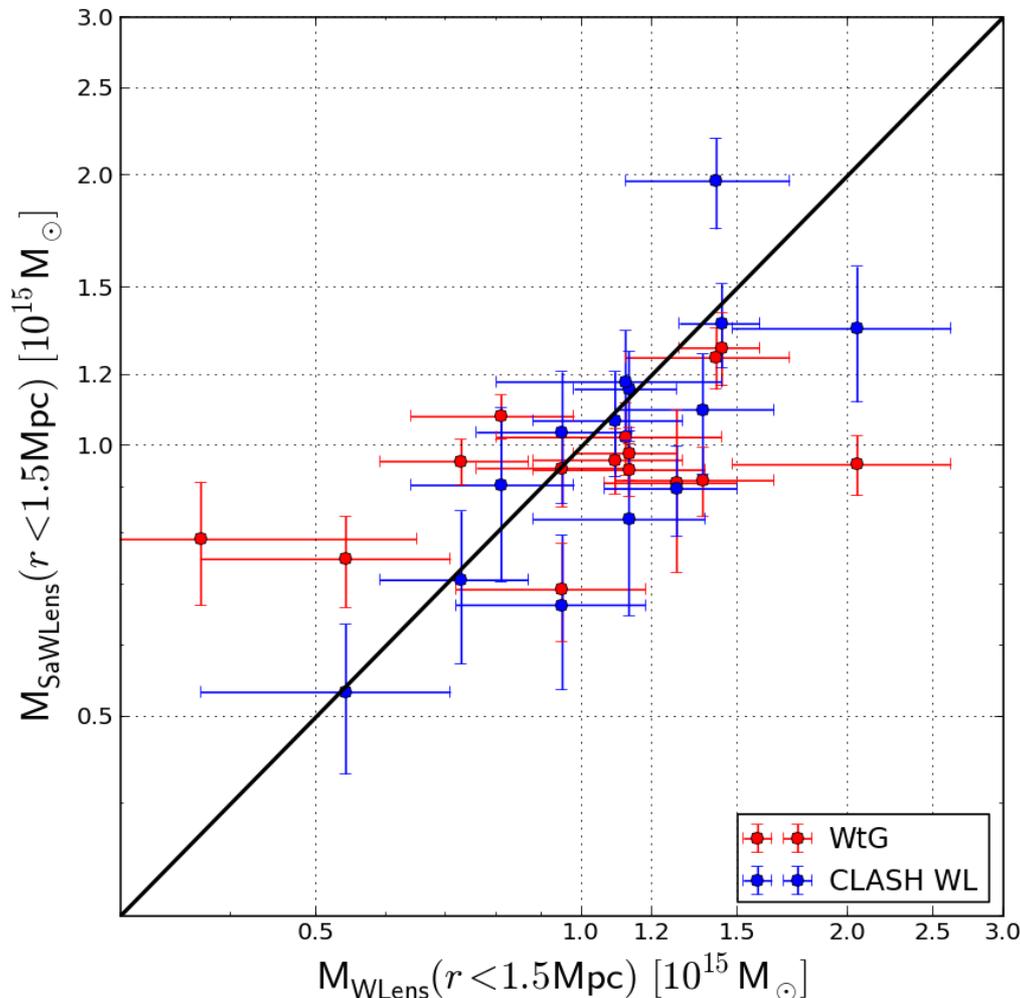
Spherical NFW $M_{3D}(r)$ profiles for 20 CLASH clusters



Systematic uncertainty in the overall mass calibration of about +/- 8 percent

Mass Comparisons @ R=1.5Mpc

Merten+CLASH 14



Un-weighted geometric mean mass ratios ($\langle Y/X \rangle = 1/\langle X/Y \rangle$)

- $\langle \text{SaWLenS} / \text{WL} \rangle = 0.96$
- $\langle \text{WL} / \text{WtG} \rangle = 0.91$
- $\langle \text{SaWLenS} / \text{WtG} \rangle = 0.88$

WL (Umetsu+14)

→ shear+mag (Subaru)

SaWLenS (Merten+14)

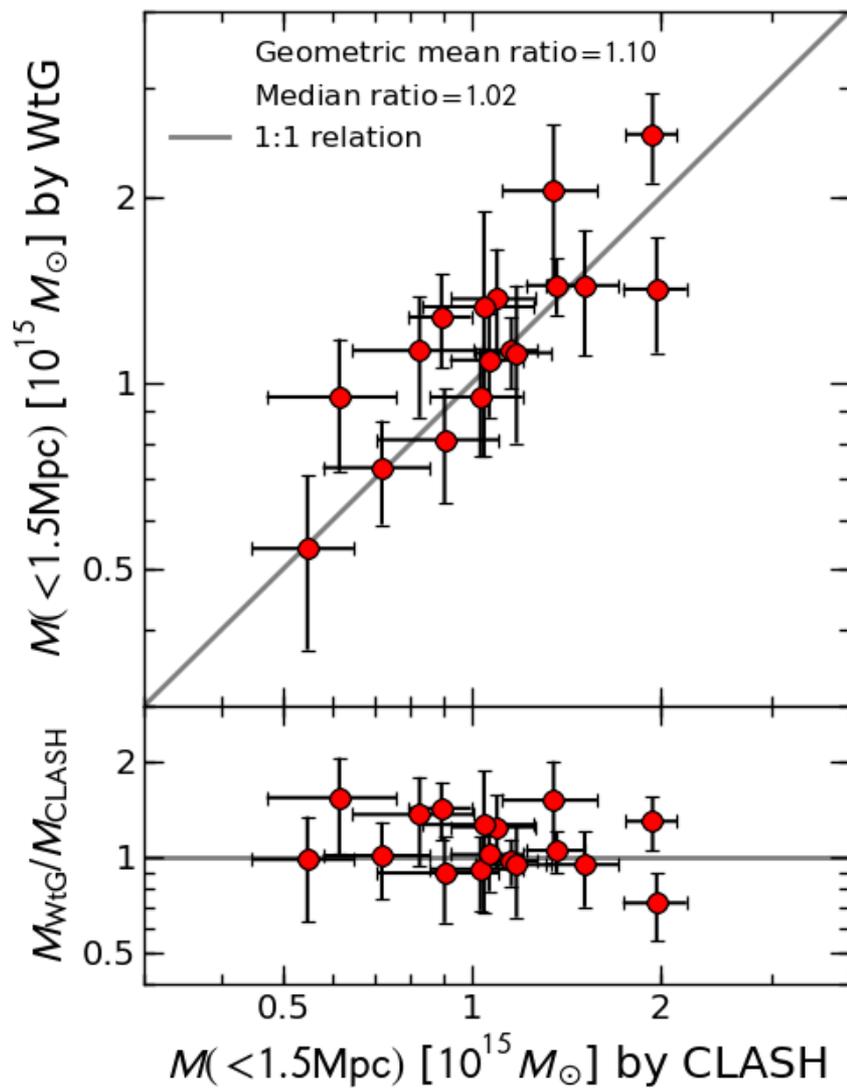
→ SL + shear (HST+Subaru)

WtG (Applegate+14)

→ shear (Subaru)

Note: WL mass calibration uncertainty of 8 percent

(contd.)

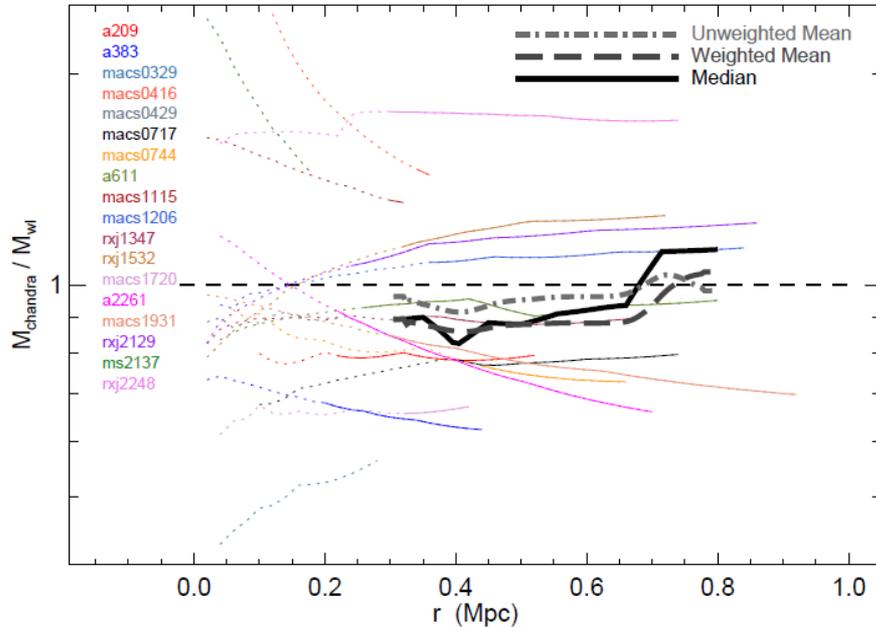


No obvious mass dependence

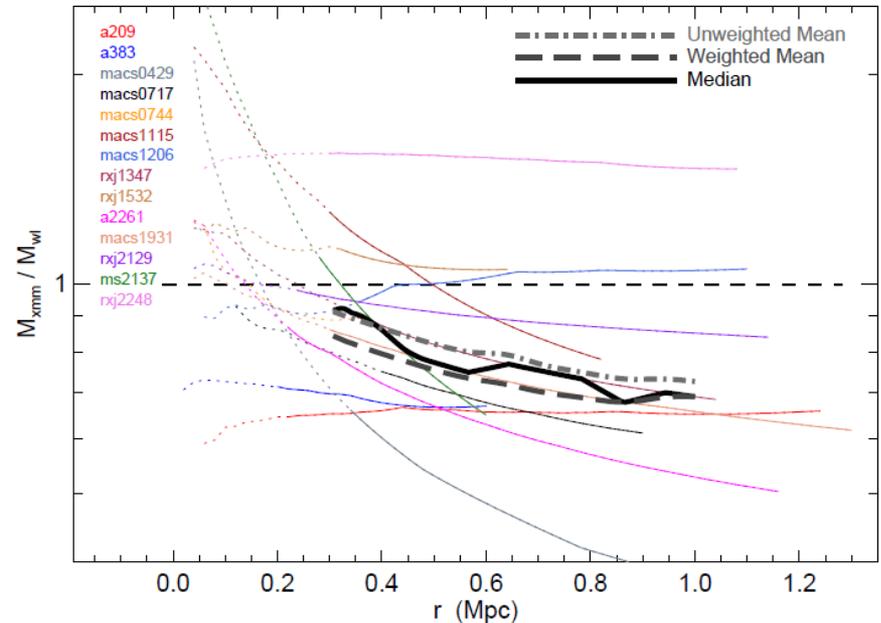
Umetsu+CLASH 14,
arXiv:1404.1375

Comparisons with X-ray masses

Chandra HSE / CLASH-WL



XMM HSE / CLASH-WL



$$M_{\text{chan}}/M_{\text{wl}} = 0.95 \pm 0.07 \pm 0.08 @0.5\text{Mpc}$$

$$M_{\text{xmm}}/M_{\text{wl}} = 0.83 \pm 0.05 \pm 0.08 @0.5\text{Mpc}$$

$$M_{\text{xmm}}/M_{\text{wl}} = 0.73 \pm 0.10 \pm 0.08 @1.0\text{Mpc}$$



Objective (2)

- Ensemble-averaged halo mass profile $\Delta\Sigma(R)$
 - Ensemble-averaged halo concentration
- from stacked *shear-only* analysis of the CLASH X-ray-selected sample (16 clusters)



Ensemble-averaged DM halo (1h) density profile

Stacking of weak-lensing signals by weighting individual clusters according to the sensitivity kernel matrix:

$$\langle\langle \widehat{\Delta\Sigma}_+ \rangle\rangle = \left(\sum_n \mathcal{W}_{+n} \right)^{-1} \left(\sum_n \mathcal{W}_{+n} \widehat{\Delta\Sigma}_{+n} \right),$$

with the individual sensitivity matrix

$$(\mathcal{W}_{+n})_{ij} \equiv \Sigma_{c,n}^{-2} (C_{+n}^{-1})_{ij}$$

defined with the total covariance matrix

$$C_+ = C_+^{\text{stat}} + C_+^{\text{sys}} + C_+^{\text{lss}}.$$

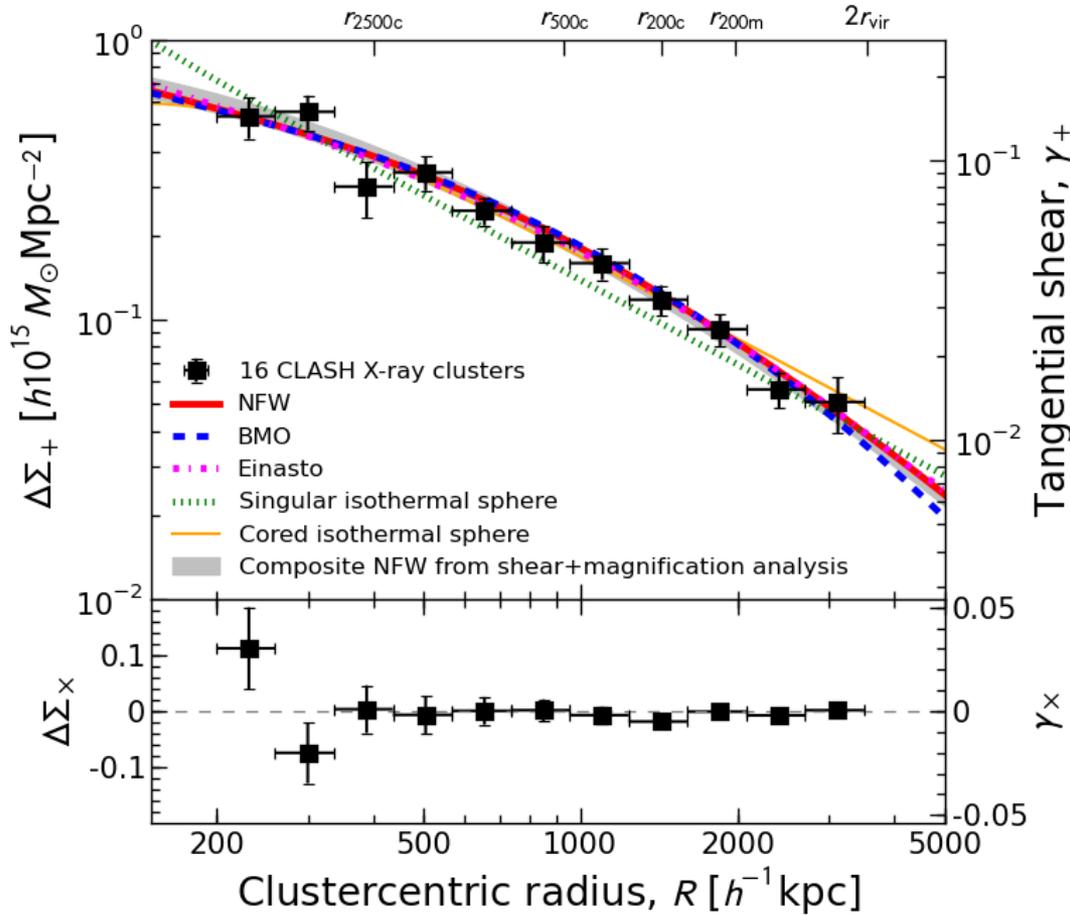
With “trace-approximation”, averaging is interpreted as

$$\langle\langle \Sigma_c^{-1} \rangle\rangle = \frac{\sum_n \text{tr}(\mathcal{W}_{+n}) \Sigma_{c,n}^{-1}}{\sum_n \text{tr}(\mathcal{W}_{+n})},$$

Umetsu+CLASH 14,
arXiv:1404.1375



Stacked halo profile shape



2-halo contribution ($v \sim 3.8$, $b_h \sim 9$) is estimated to be $\gamma_+ < 1e-3$ within $2R_{vir}$

Stacked shear-only analysis provides a net 1-halo-only constraint.

Einasto shape parameter $\alpha = 0.19 \pm 0.07$, consistent with the NFW equivalent value of $\alpha \sim 0.18$

Consistent with a family of density profiles for collisionless, cold DM halos (NFW, variants of NFW, Einasto)

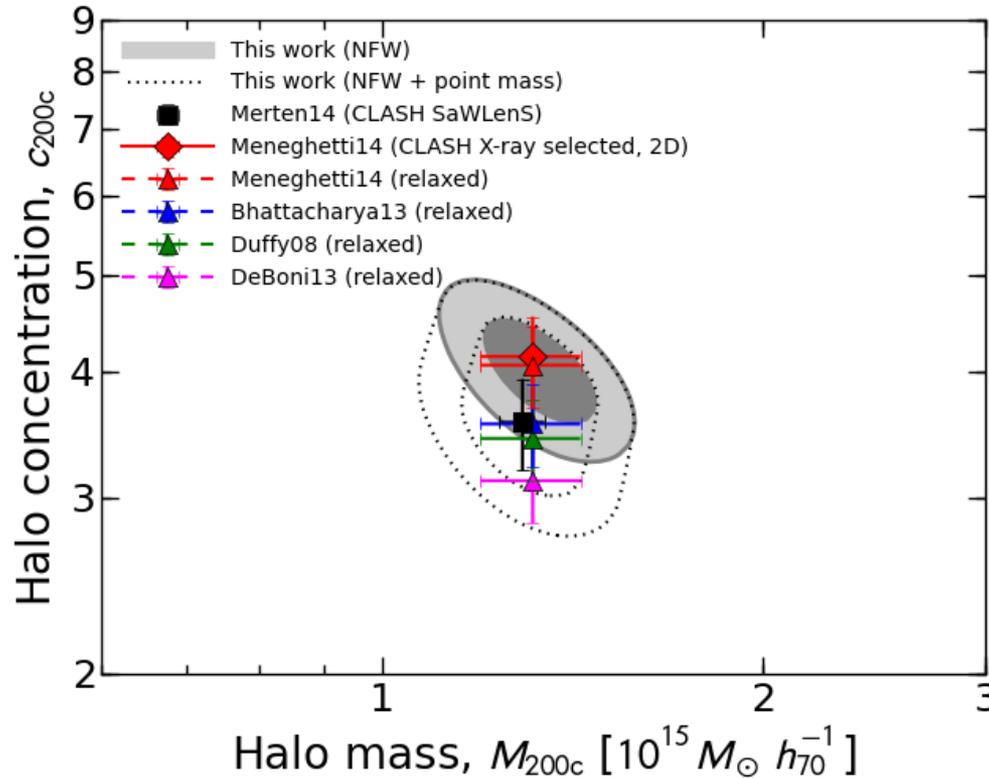
Umetsu+CLASH14



Integrated constraints on $c(M, z)$

**Theoretical predictions
for stacked c-M-z**

$$\langle\langle c \rangle\rangle = \frac{\int dM \int dz N(M, z) \hat{c}(M, z)}{\int dM \int dz N(M, z)} \approx \frac{\sum_n \text{tr}(W_n) \hat{c}(M_n, z_n)}{\sum_n \text{tr}(W_n)}$$



**Variance in theory due
to different cosmology
and spatial resolution**

M14: $\sigma_8=0.82$

Bhat13: $\sigma_8=0.8$

Duffy08: $\sigma_8=0.8$

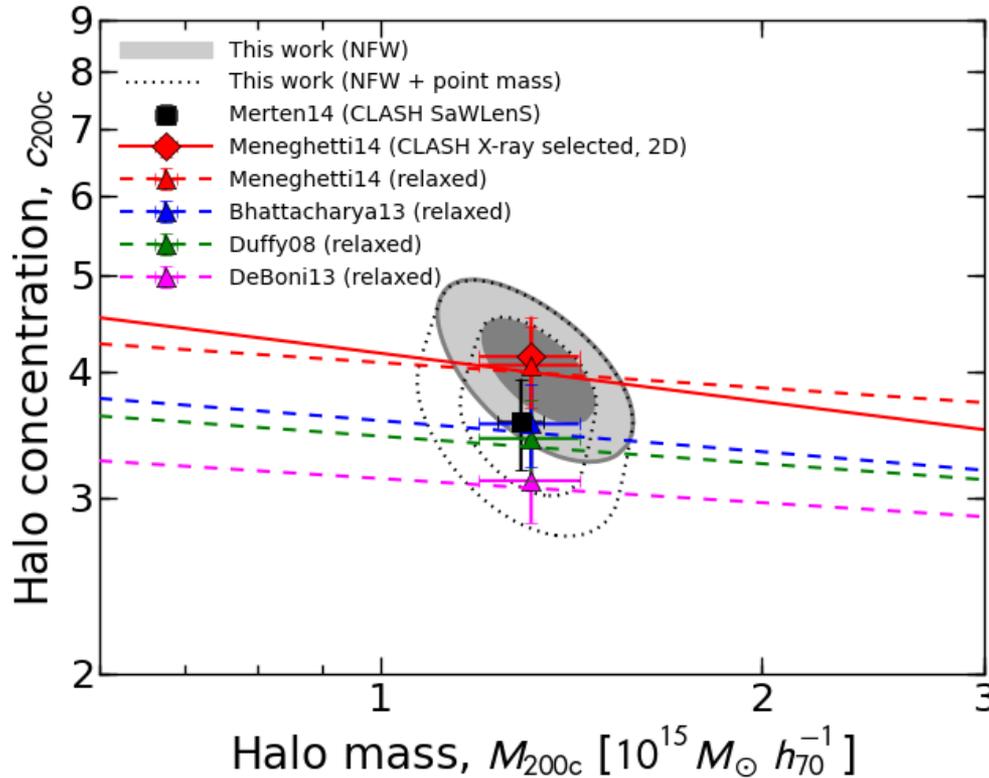
DeBoni13: $\sigma_8=0.78$



Integrated constraints on $c(M, z)$

**Theoretical predictions
for stacked c-M-z**

$$\langle\langle c \rangle\rangle = \frac{\int dM \int dz N(M, z) \hat{c}(M, z)}{\int dM \int dz N(M, z)} \approx \frac{\sum_n \text{tr}(W_n) \hat{c}(M_n, z_n)}{\sum_n \text{tr}(W_n)}$$



c-M curves

$$c = \hat{c}(M, \langle\langle z \rangle\rangle)$$

$$\langle\langle z \rangle\rangle = 0.35$$



Objective (3)

- Ensemble-averaged total mass profile

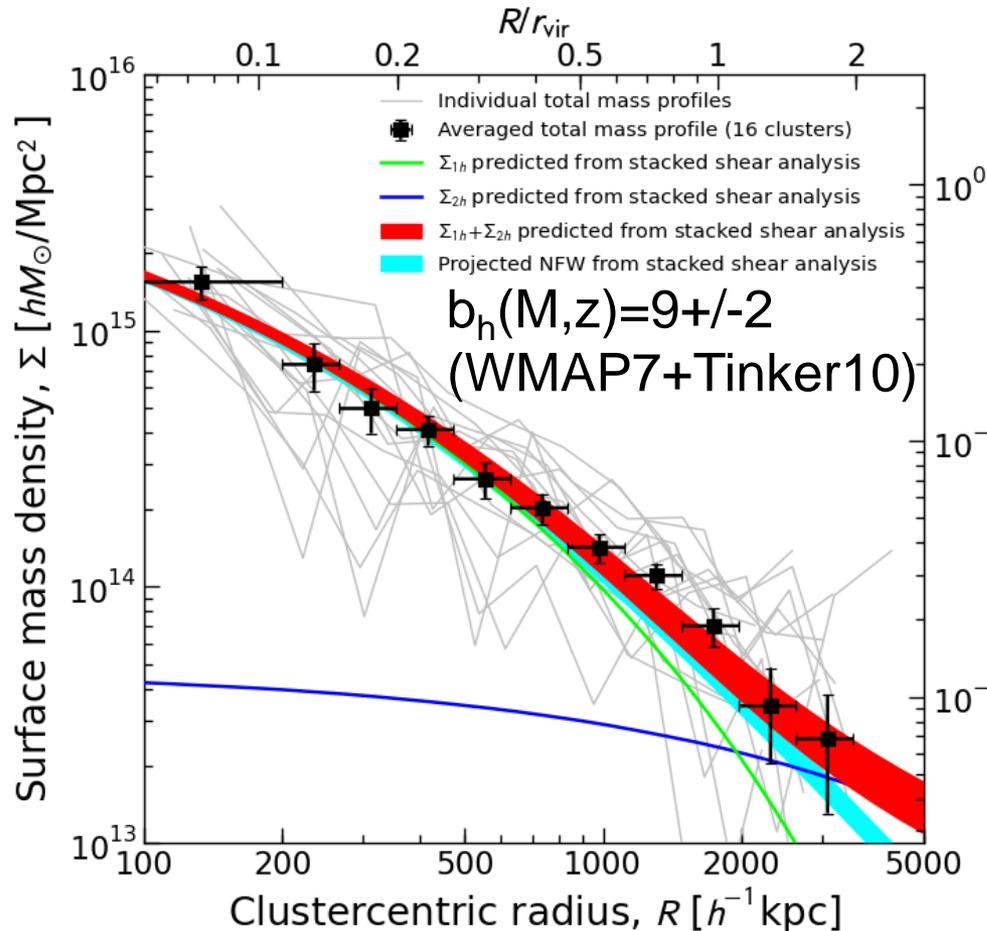
$$\Sigma(R) = \Sigma_{1h}(R) + \Sigma_{2h}(R)$$

of individual total mass profiles of the CLASH X-ray-selected sample (16 clusters) reconstructed from joint shear+magnification analysis

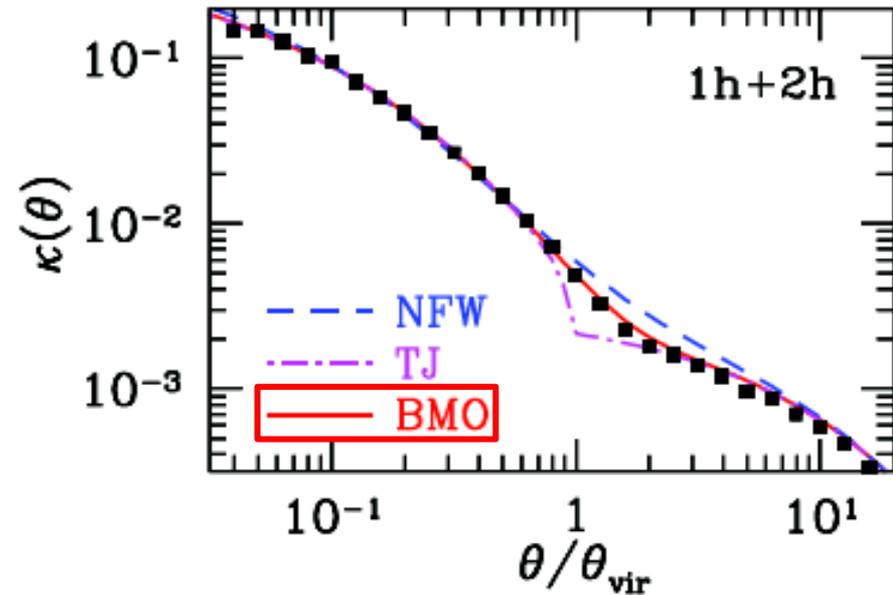


Averaged cluster (1h) + LSS (2h) from combined shear + magnification

CLASH-WL: shear+magnification



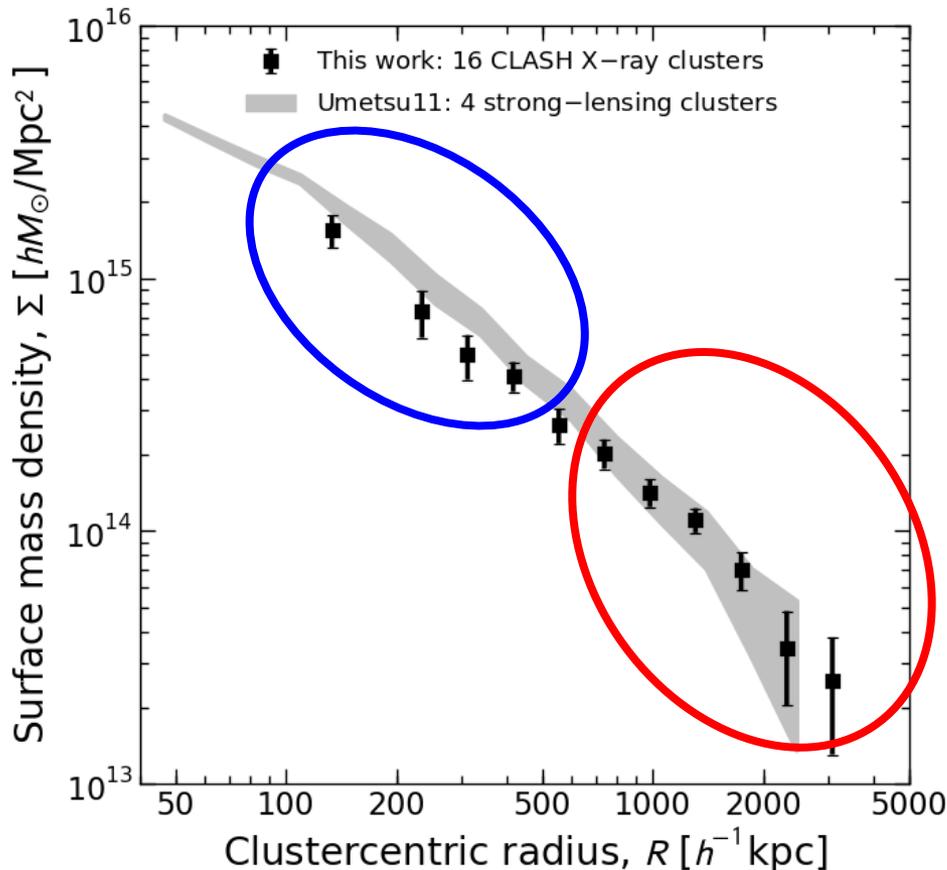
2D halo-model decomposition: truncated NFW (BMO) + LCDM 2h term (Oguri & Hamana 11)



Umetsu+CLASH14

Comparison with pre-CLASH results

- C200 vs θ_E relation, consistent with triaxial CDM halos (Oguri+12)
- **Similar v (MAH), similar Σ in outskirts (Diemer & Kravtsov 14)**
- **Increased c at $R < 0.5 \text{ Mpc}/h$, consistent w orientation bias (Gao+12)**



CLASH X-ray-selected sample

- $M_{200} = 0.9 e^{15} M_{\text{sun}}/h$
- $\underline{c_{200} = 4.0}$
- $\underline{\theta_E \sim 15''}$ ($z_s=2$)
- $\underline{v=3.8}$ ($b \sim 9$)

Umetsu11b sample

- $M_{200} = 1.2 e^{15} M_{\text{sun}}/h$
- $\underline{c_{200} = 6.1}$
- $\underline{\theta_E \sim 36''}$ ($z_s=2$)
- $\underline{v=4.1}$ ($b \sim 11$)



Summary

- Ensemble-averaged halo structure $\Delta\Sigma$ (1h) of X-ray-regular CLASH clusters is consistent with a family of standard (collisionless) DM predictions:
 - Halo mass: $M_{200} = 1.3 \pm 0.1 \cdot 10^{15} M_{\text{sun}}$ at $z=0.35$
 - Einasto (PTE=0.51): degree of curvature, $\alpha = 0.19 \pm 0.07$
 - NFW (PTE=0.66): degree of concentration, $c_{200} = 4.01 (+0.35, -0.32)$
- The measured concentration is in excellent agreement with the theoretical expectation, $c_{200} = 4.15 \pm 0.40$, which takes into account the CLASH selection function and projection effects (Meneghetti+CLASH 14).
- Our c-M results are consistent with the SaWLens analysis of Merten+CLASH 14, demonstrating consistency between results obtained with different lensing methods.

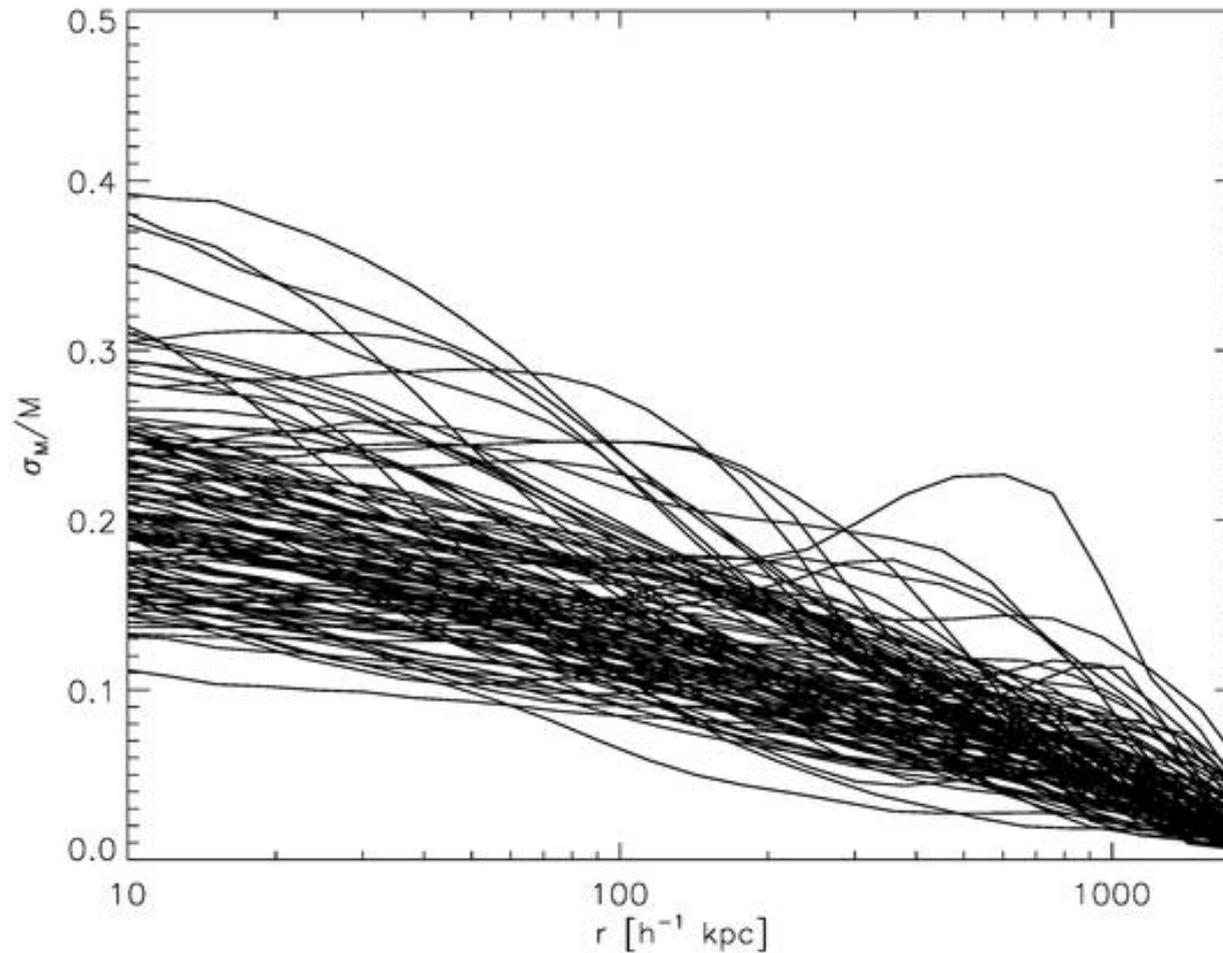


Summary (contd.)

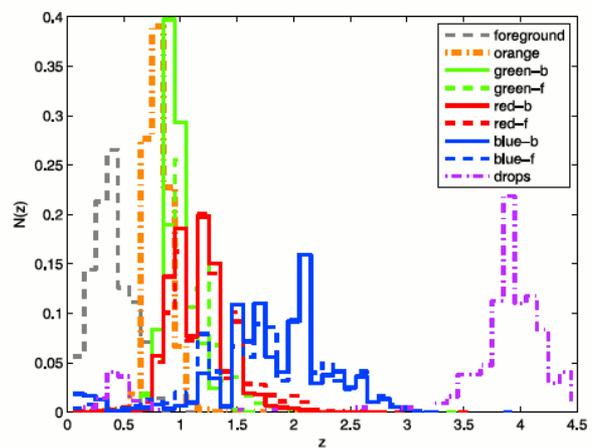
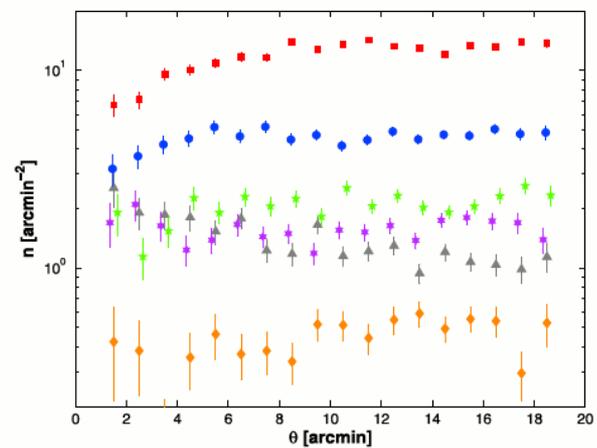
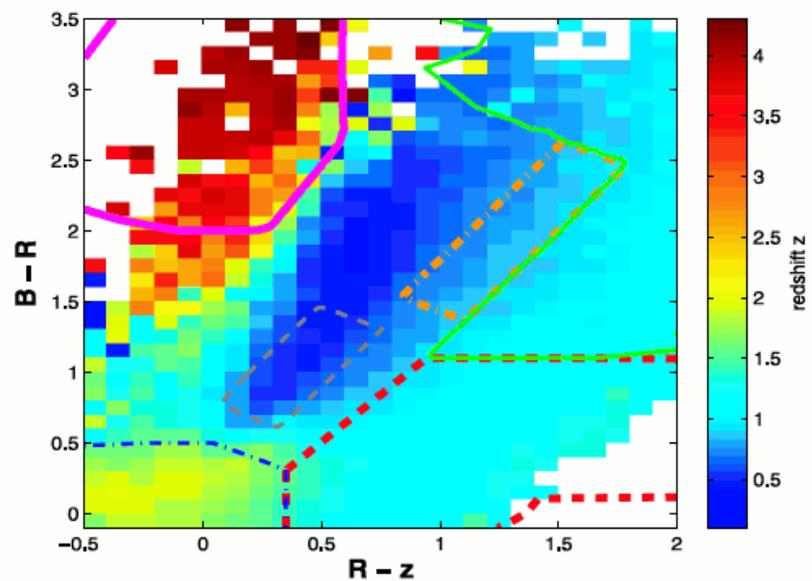
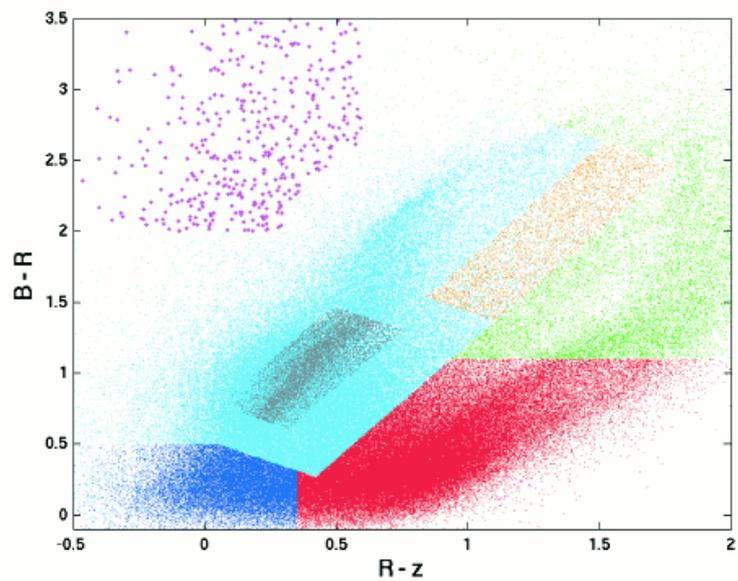
- Cluster masses from CLASH-WL, CLASH-SaW, WtG-WL are in agreement within the uncertainties: $WtG-WL > CLASH-WL > CLASH-SaWLenS$
 - $\langle CLASH-WL / WtG \rangle = 0.91$
 - $\langle SaWLenS / WtG \rangle = 0.88$
 - $\langle SaWLenS / CLASH-WL \rangle = 0.96$
- Total matter distribution Σ (1h+2h) around clusters determined from shear+magnification is consistent with the shear-based halo model predictions, establishing further consistency in the context of LCDM.
 - Large modeling uncertainties in the 1h-2h transition region (Oguri & Hamana 11; Diemer & Kravtsov 14)
- Most of the previous overconcentration problems can be explained by
 - Theoretical predictions were likely underestimated (10-20%) in the high-mass cluster regime, $M_{200} > 5e14 M_{sun}/h$ (σ_8 , resolution, ..)
 - Orientation bias due to halo triaxiality, boosting $\Sigma(R)$ at $R < 500 kpc/h$ (Gao+12), resulting in $\sim +50\%$ bias in c_{200} (Hennawi+07; Oguri+12)

Supplemental Slides

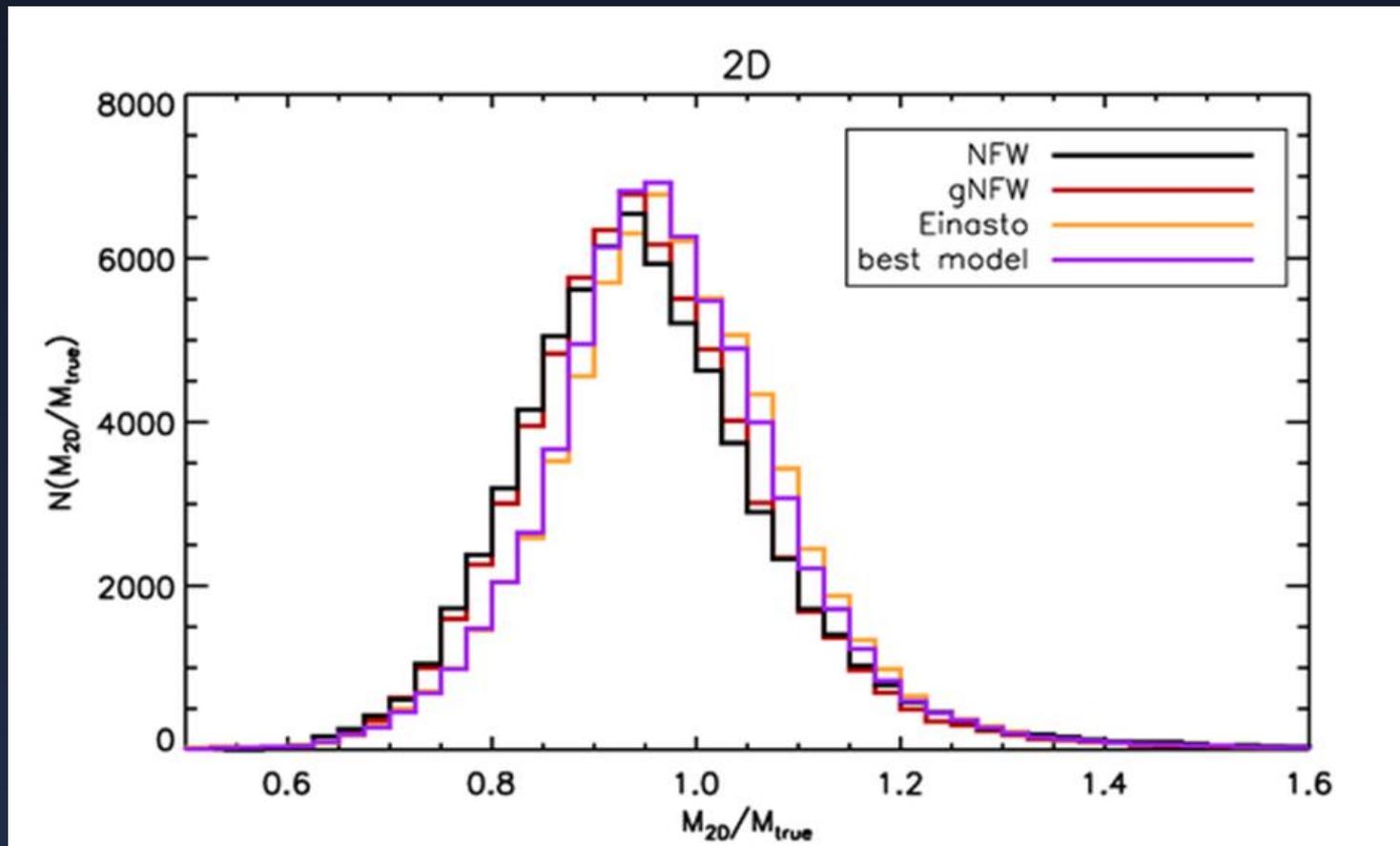
Scatter in $M_{2D}(R)$ by halo triaxiality



MUSIC-2 simulation by Massimo



Cluster masses recovered from lensing analysis

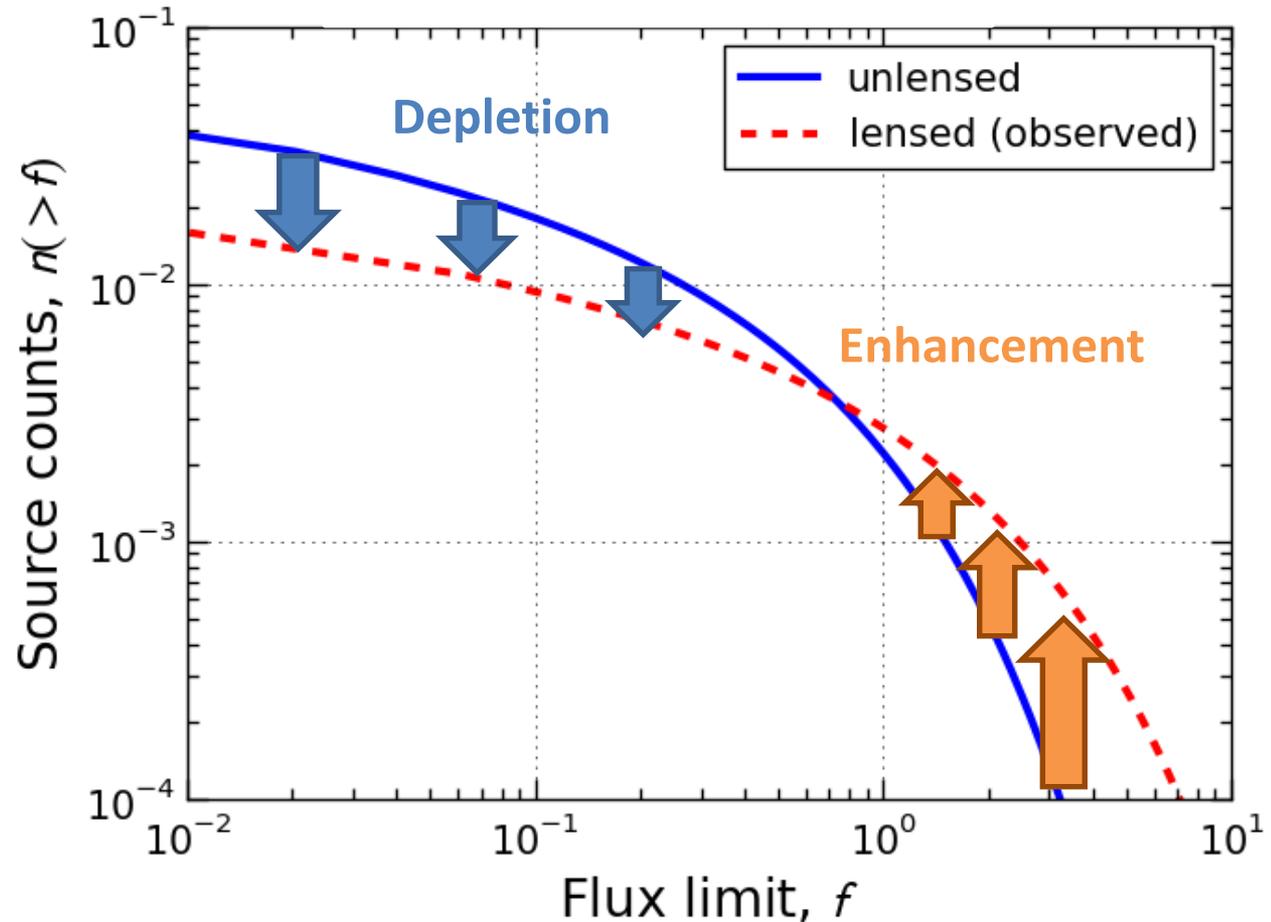


Magnification bias effects

Flux-limited
source counts:

$$n_{\text{obs}}(> f) = \mu^{-1} n(> \mu^{-1} f)$$

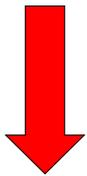
Broadhurst, Taylor &
Peacock 95



Flux amplification



Geometric area
distortion



n/μ