

# Relative fundamental solution to the CR invariant powers of sub-Laplacian and the deformation complex of CR structures

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## Abstract

It is well-known that CR invariant powers of sub-laplacian  $P_k$  of order  $2k$  on  $S^{2n+1}$  has a fundamental solution (and hence  $\ker P_k = \{0\}$ ) if and only if  $k \in \{1, 2, \dots, n\}$ . The critical case  $P_{n+1}$  is studied by Graham and Geller:  $\ker P_{n+1}$  is the space of CR pluriharmonic functions and  $P_{2n+2}$  has a relative fundamental solution. In this talk, I'll give a relative fundamental solutions for higher order  $P_k$  and show that  $\ker P_k$  agree with the kernel of the fist BGG operators. In particular, we observe that  $\ker P_{n+2}$  agrees with the kernel of the first operator of the deformation complex of CR structures. This is a key fact in the study of obstruction flat CR manifolds or strictly pseudoconvex domains with no logarithmic singularity in the Bergman kernel. This is a joint work with Makoto Nakamura at University of Tokyo.